


Relational Algebra

Chapter 4


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Relational Query Languages

- ❖ *Query languages*: Allow manipulation and **retrieval of data** from a database.
- ❖ Relational model supports simple, powerful QLS:
 - Strong formal foundation based on logic.
 - Allows for much optimization.
- ❖ Query Languages **!=** programming languages!
 - QLS not expected to be “Turing complete”.
 - QLS not intended to be used for complex calculations.
 - QLS support easy, efficient access to large data sets.

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Formal Relational Query Languages

- ❖ Two mathematical Query Languages form the basis for “real” languages (e.g. SQL), and for implementation:
 - **Relational Algebra**: More **operational**, very useful for representing execution plans.
 - **Relational Calculus**: Lets users describe what they want, rather than how to compute it. (**Non-operational, declarative.**)

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Preliminaries



- ❖ A query is applied to *relation instances*, and the result of a query is also a relation instance.
 - *Schemas of input* relations for a query are **fixed** (but query will run regardless of instance!)
 - The **schema for the result** of a given query is also **fixed!** Determined by definition of query language constructs.
- ❖ Positional vs. named-field notation:
 - Positional notation easier for formal definitions, named-field notation more readable.
 - Both used in SQL

Example Instances

R1	sid	bid	day
	22	101	10/10/96
	58	103	11/12/96



- ❖ "Sailors" and "Reserves" relations for our examples.
- ❖ We'll use positional or named field notation, assume that names of fields in query results are 'inherited' from names of fields in query input relations.

S1	sid	sname	rating	age
	22	dustin	7	45.0
	31	lubber	8	55.5
	58	rusty	10	35.0

S2	sid	sname	rating	age
	28	yuppy	9	35.0
	31	lubber	8	55.5
	44	guppy	5	35.0
	58	rusty	10	35.0

Relational Algebra



- ❖ Basic operations:
 - **Selection** (σ) Selects a subset of rows from relation.
 - **Projection** (π) Deletes unwanted columns from relation.
 - **Cross-product** (\times) Allows us to combine two relations.
 - **Set-difference** ($-$) Tuples in reln. 1, but not in reln. 2.
 - **Union** (\cup) Tuples in reln. 1 and in reln. 2.
- ❖ Additional operations:
 - Intersection, **join**, division, renaming: Not essential, but (very!) useful.
- ❖ Since each operation returns a relation, **operations can be composed!** (Algebra is "closed".)

Cross-Product



- ❖ Each row of S1 is paired with each row of R1.
- ❖ **Result schema** has one field per field of S1 and R1, with field names `inherited` if possible.
 - **Conflict:** Both S1 and R1 have a field called *sid*.

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	22	101	10/10/96
31	lubber	8	55.5	58	103	11/12/96
58	rusty	10	35.0	22	101	10/10/96
58	rusty	10	35.0	58	103	11/12/96

- **Renaming operator:** $\rho(C(1 \rightarrow sid1, 5 \rightarrow sid2), S1 \times R1)$

Joins



- ❖ **Condition Join:** $R \bowtie_c S = \sigma_c(R \times S)$

(sid)	sname	rating	age	(sid)	bid	day
22	dustin	7	45.0	58	103	11/12/96
31	lubber	8	55.5	58	103	11/12/96

$$S1 \bowtie_{S1.sid < R1.sid} R1$$

- ❖ **Result schema** same as that of cross-product.
- ❖ Fewer tuples than cross-product, might be able to compute more efficiently
- ❖ Sometimes called a **theta-join**.

Joins



- ❖ **Equi-Join:** A special case of condition join where the condition *c* contains only **equalities**.

sid	sname	rating	age	bid	day
22	dustin	7	45.0	101	10/10/96
58	rusty	10	35.0	103	11/12/96

$$S1 \bowtie_{sid} R1$$

- ❖ **Result schema** similar to cross-product, but only one copy of fields for which equality is specified.
- ❖ **Natural Join:** Equijoin on *all* common fields.

Division



- ❖ Not supported as a primitive operator, but useful for expressing queries like:
Find sailors who have reserved **all** boats.
- ❖ Let A have 2 fields, x and y ; B have only field y :
 - $A/B = \{ \langle x \rangle \mid \forall \langle y \rangle \in B \exists \langle x, y \rangle \in A \}$
 - i.e., A/B contains all x tuples (sailors) such that for **every y tuple (boat) in B , there is an xy tuple in A .**
 - Or: If the set of y values (boats) associated with an x value (sailor) in A contains all y values in B , the x value is in A/B .
- ❖ In general, x and y can be any lists of fields; y is the list of fields in B , and $x \cup y$ is the list of fields of A .

Examples of Division A/B



sno	pno	pno	pno	pno
s1	p1	p2	p2	p1
s1	p2	B1	p4	p2
s1	p3		B2	p4
s1	p4			B3
s2	p1	sno		
s2	p2	s1		
s3	p2	s2	sno	
s4	p2	s3	s1	
s4	p4	s4	s4	sno
				s1

A
 $A/B1$
 $A/B2$
 $A/B3$

Expressing A/B Using Basic Operators



- ❖ Division is not essential op; just a useful shorthand.
 - (Also true of joins, but joins are so common that systems implement joins specially.)
- ❖ **Idea:** For A/B , compute all x values that are not 'disqualified' by some y value in B .
 - x value is *disqualified* if by attaching y value from B , we obtain an xy tuple that is not in A .

Disqualified x values: $\pi_x((\pi_x(A) \times B) - A)$

A/B : $\pi_x(A) -$ all disqualified tuples

Find names of sailors who've reserved boat #103

❖ Solution 1: $\pi_{sname}((\sigma_{bid=103} Reserves) \bowtie Sailors)$

❖ Solution 2: $\rho(Temp1, \sigma_{bid=103} Reserves)$

$\rho(Temp2, Temp1 \bowtie Sailors)$

$\pi_{sname}(Temp2)$

❖ Solution 3: $\pi_{sname}(\sigma_{bid=103}(Reserves \bowtie Sailors))$

Find names of sailors who've reserved a red boat

❖ Information about boat color only available in Boats; so need an extra join:

$\pi_{sname}((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$

❖ A more efficient solution:

$\pi_{sname}(\pi_{sid}(\pi_{bid}(\sigma_{color='red'} Boats) \bowtie Res) \bowtie Sailors)$

A query optimizer can find this, given the first solution!

Find sailors who've reserved a red or a green boat

❖ Can identify all red or green boats, then find sailors who've reserved one of these boats:

$\rho(Tempboats, (\sigma_{color='red' \vee color='green'} Boats))$

$\pi_{sname}(Tempboats \bowtie Reserves \bowtie Sailors)$

❖ Can also define Tempboats using union! (How?)

❖ What happens if \vee is replaced by \wedge in this query?

Find sailors who've reserved a red and a green boat

- ❖ Previous approach won't work! Must identify sailors who've reserved red boats, sailors who've reserved green boats, then find the intersection (note that *sid* is a key for Sailors):

ρ (Tempred, $\pi_{sid}((\sigma_{color='red'} Boats) \bowtie Reserves)$)

ρ (Tempgreen, $\pi_{sid}((\sigma_{color='green'} Boats) \bowtie Reserves)$)

$\pi_{sname}((Tempred \cap Tempgreen) \bowtie Sailors)$

Find the names of sailors who've reserved all boats

- ❖ Uses division; schemas of the input relations to / must be carefully chosen:

ρ (Tempsids, $(\pi_{sid,bid} Reserves) / (\pi_{bid} Boats)$)

$\pi_{sname}(Tempsids \bowtie Sailors)$

- ❖ To find sailors who've reserved all 'Interlake' boats:

..... / $\pi_{bid}(\sigma_{bname='Interlake'} Boats)$

Summary

- ❖ The relational model has rigorously defined query languages that are simple and powerful.
- ❖ Relational algebra is more operational; useful as internal representation for query evaluation plans.
- ❖ Several ways of expressing a given query; a query optimizer should choose the most efficient version.
