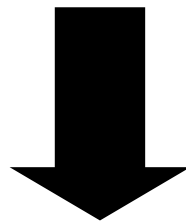


1. Introduction

Background

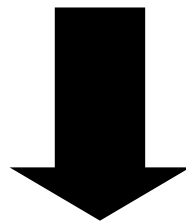
Frequency is a fundamental physical quantity of electromagnetic wave

Maintenance of THz frequency metrology is required for various THz applications



Advent of practical CW-THz sources (THz-QCL, UTC-PD, RTD, etc)

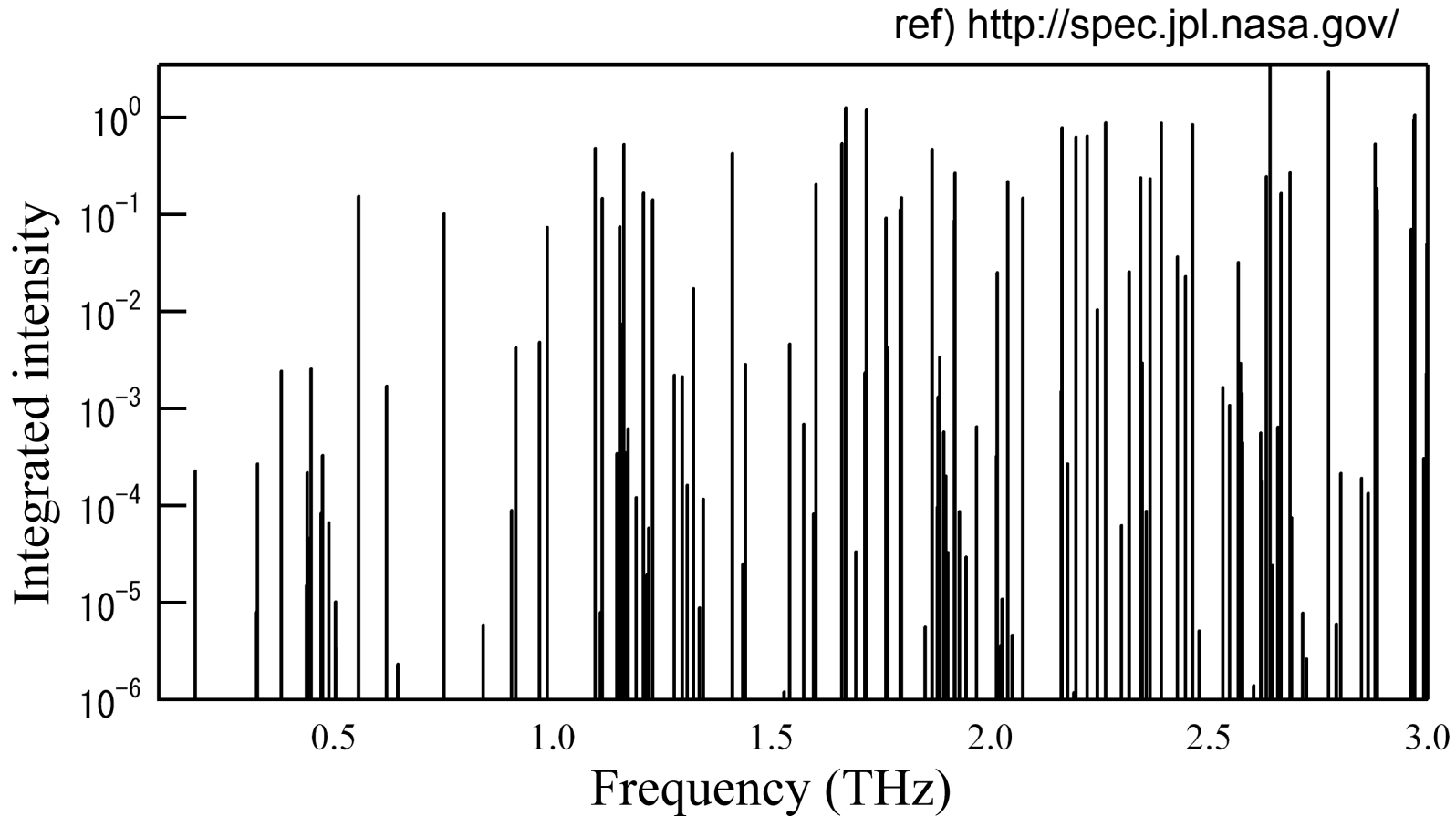
Precise frequency measurement of CW-THz wave is required!



However, techniques of frequency measurement in THz region have been underdeveloped yet.

Conventional method (1)

Frequency calibration based on water vapor absorption

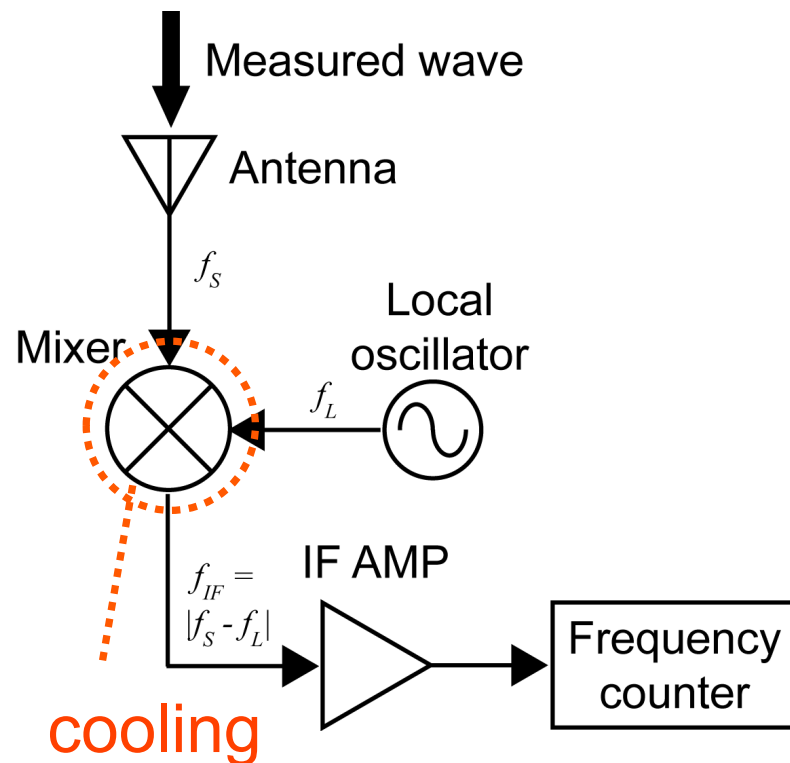


Simple

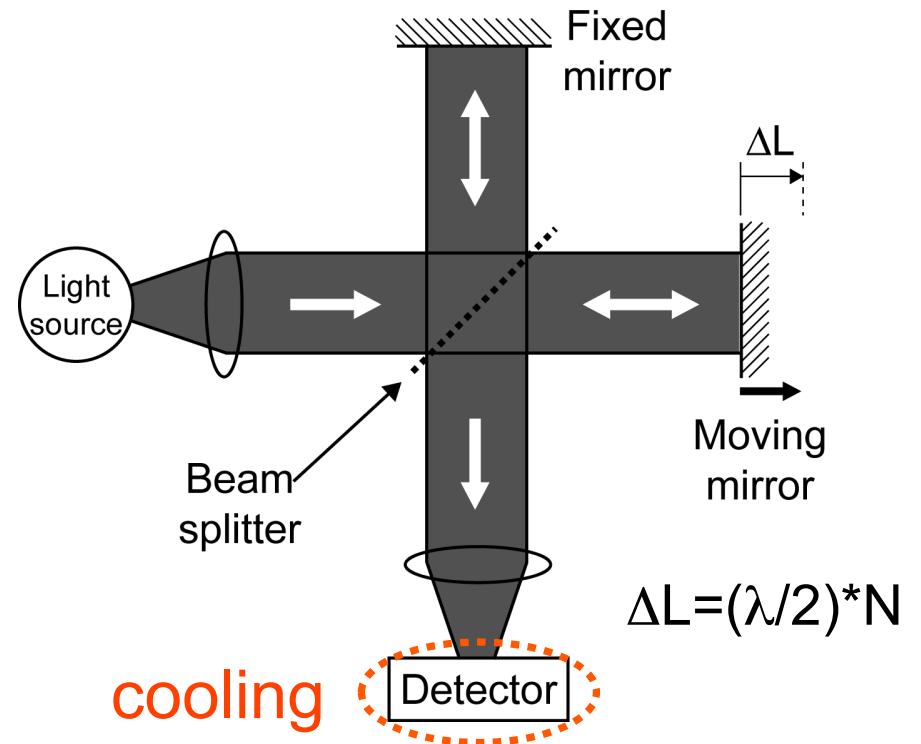
Pressure broadening of absorption line, discrete distribution

Conventional method (2)

Electrical heterodyned method

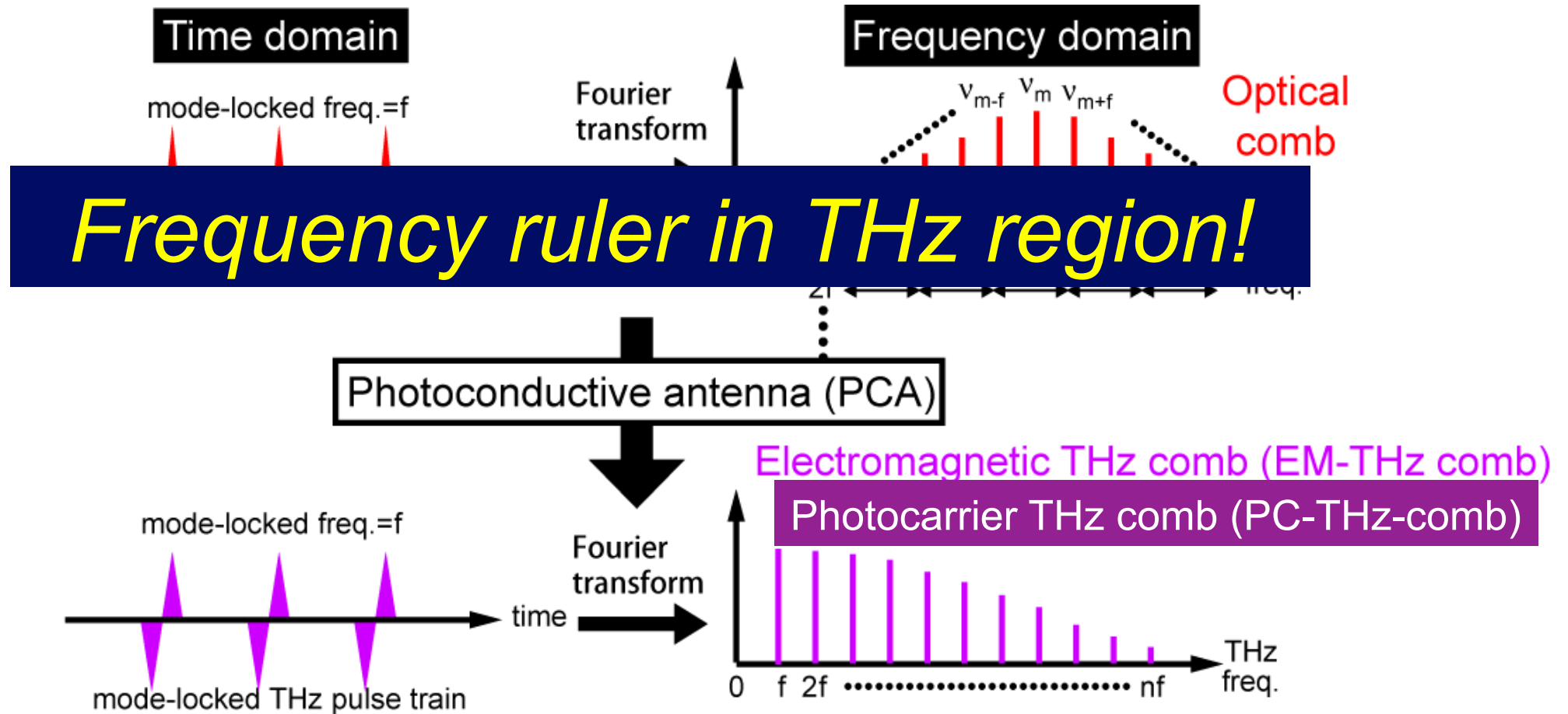


Optical interferometric method



Difficult to cover all frequency region of THz wave (0.1~10THz)
 → Requirement of new method optimized for THz wave!

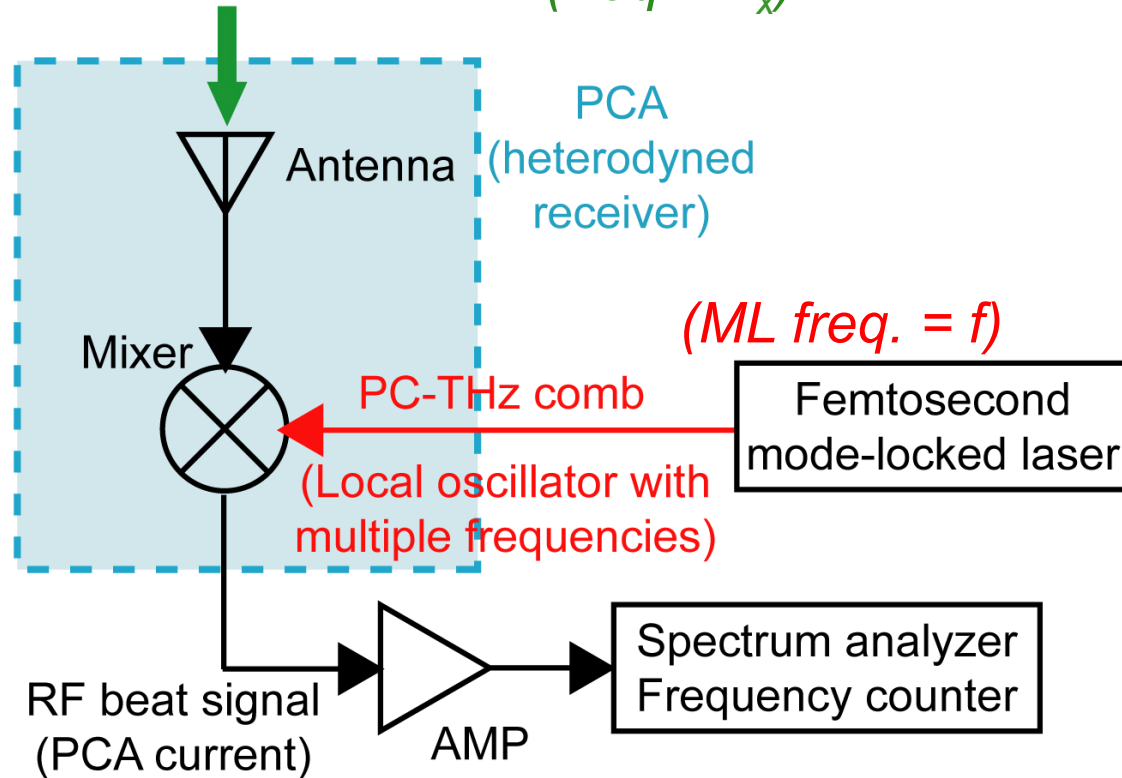
Optical comb and THz comb



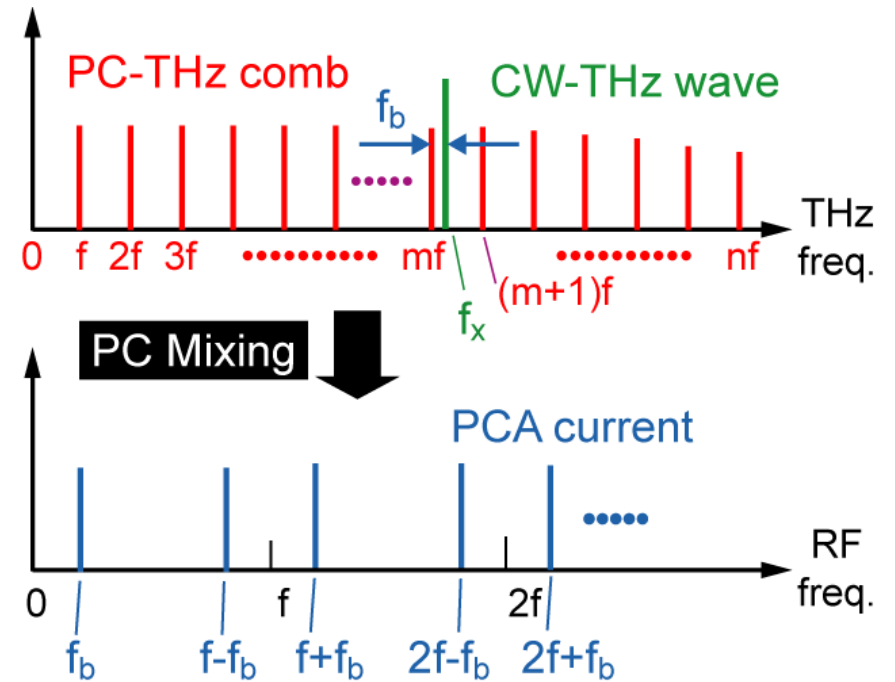
Accurate, stable, broadband selectivity, high spectral purity, and absolute frequency calibration

Principle

Measured CW-THz wave (f_x)



Freq. domain



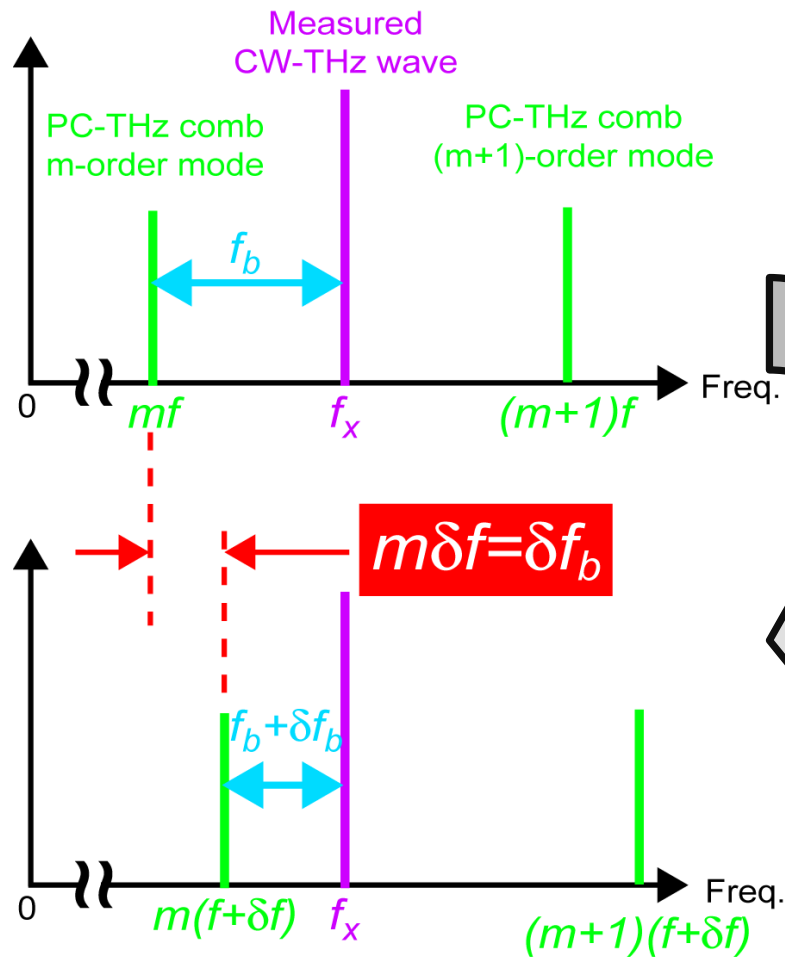
measure

$$f_b = |f_x - mf|$$

sign

m : order of comb mode
 f : ML freq.
 f_b : beat freq.

Determination of order of m



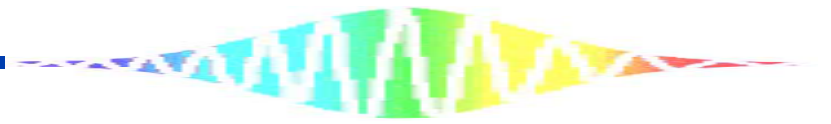
Shift of ML freq. by δf
($f \text{ @ } f+\delta f$)

$$m = \frac{|\delta f_b|}{|\delta f|}$$

Change of beat freq. by δf_b
($f_b \text{ @ } f_b + \delta f_b$)

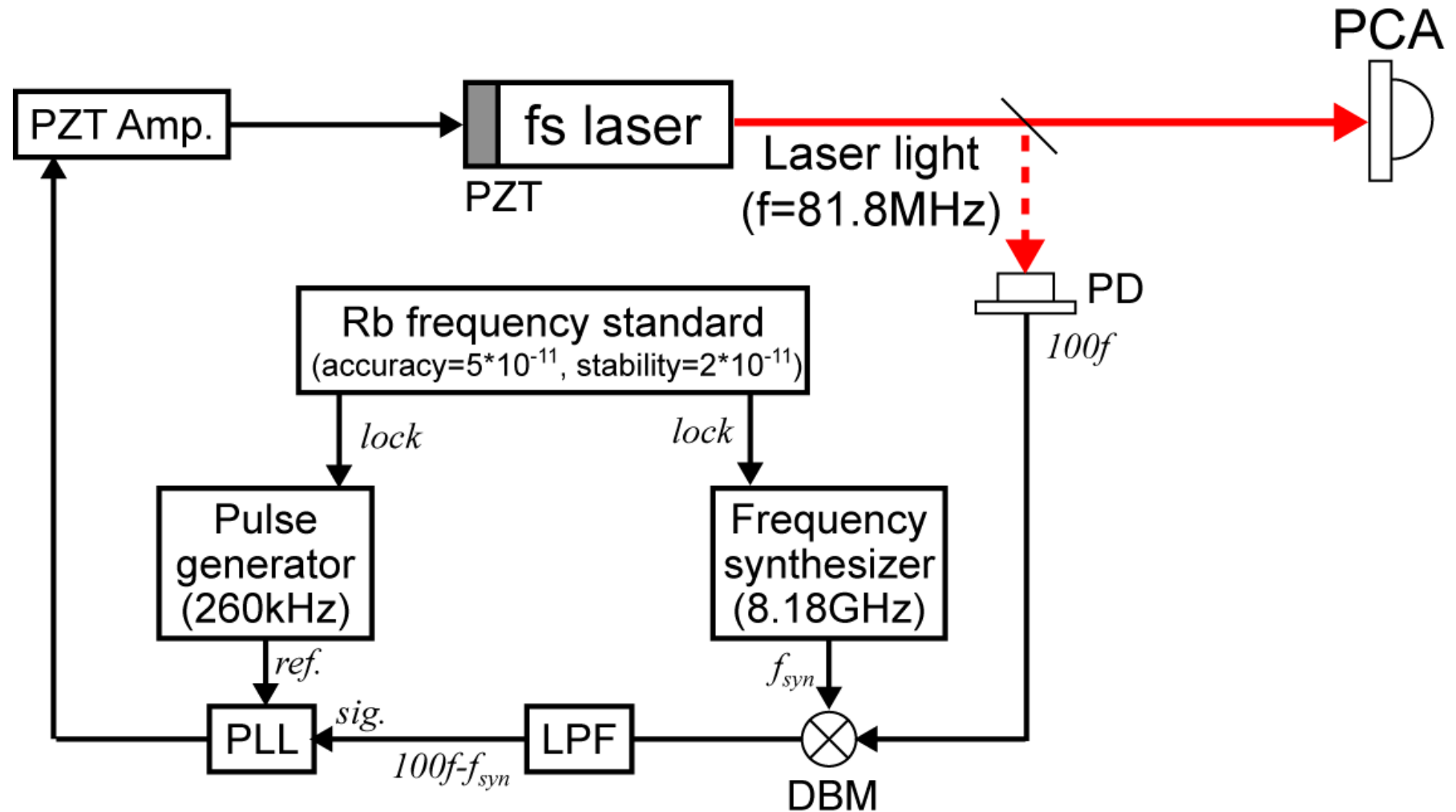
$$f_x = mf - f_b \quad (\delta f_b / \delta f > 0)$$

$$f_x = mf + f_b \quad (\delta f_b / \delta f < 0)$$

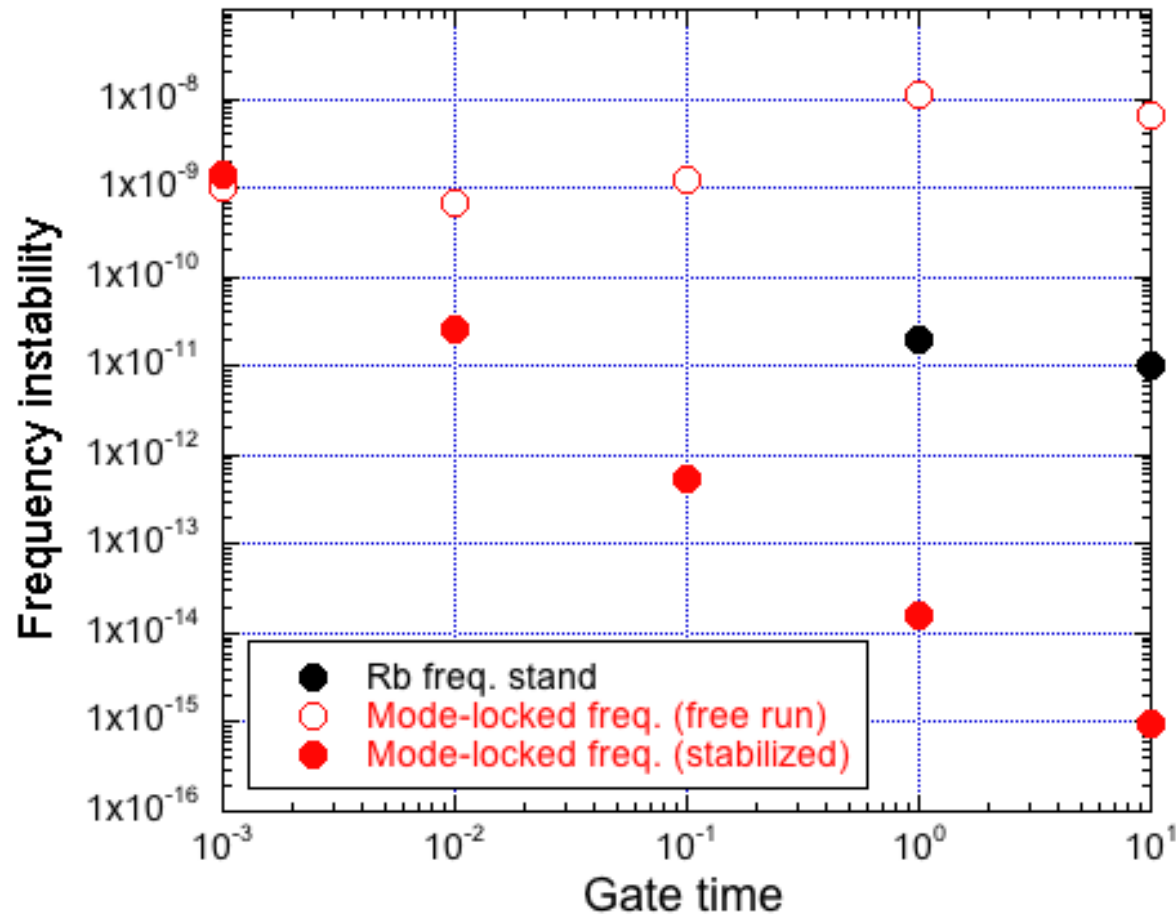


2. Ti:S-laser-based THz spectrum analyzer

Laser source for PC-THz comb

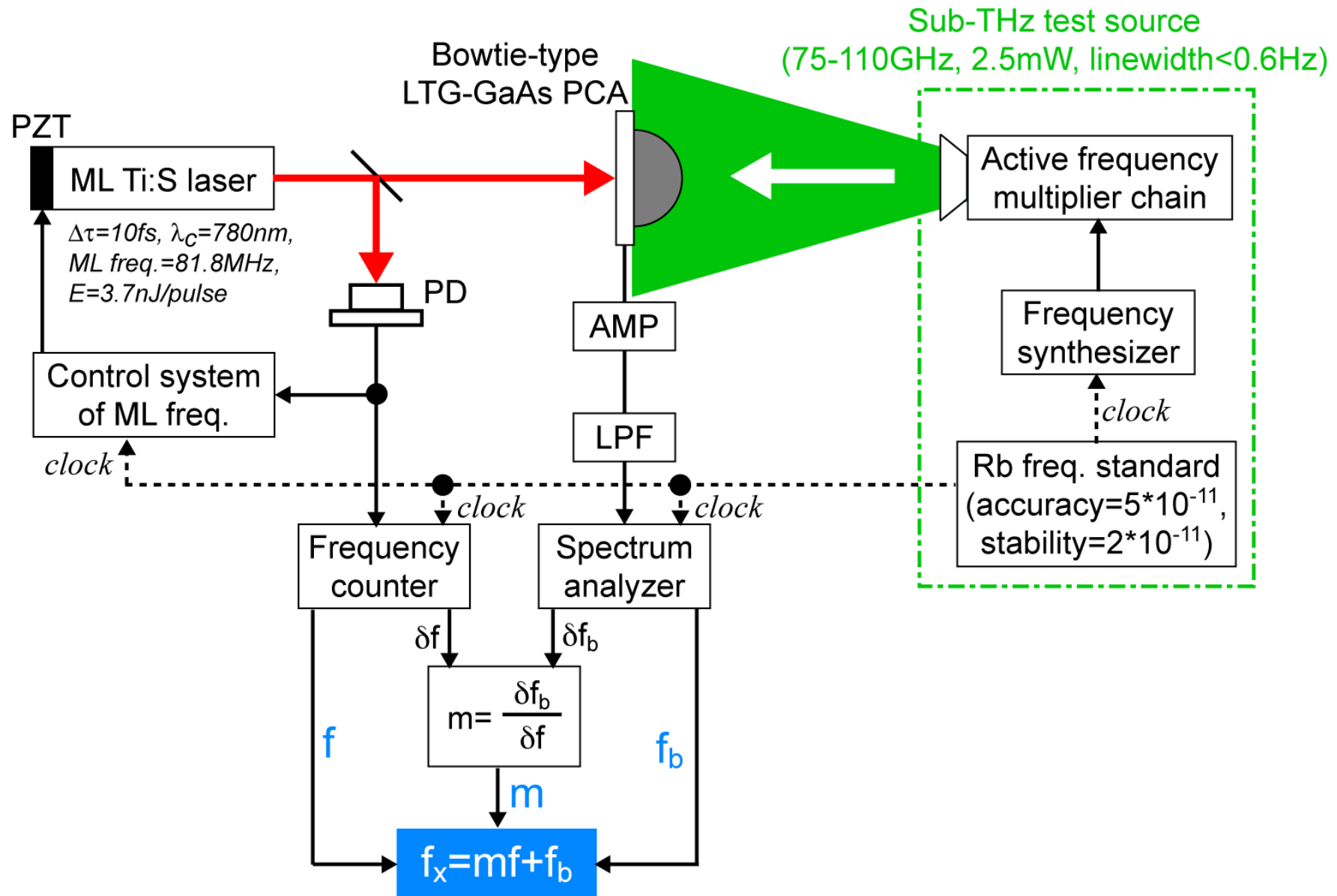


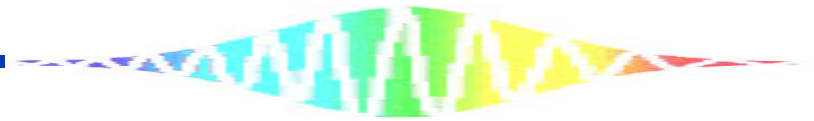
Stability of mode-locked frequency



Stability and accuracy of PC-THz comb is equal to those of Rb freq. standard

Experimental setup

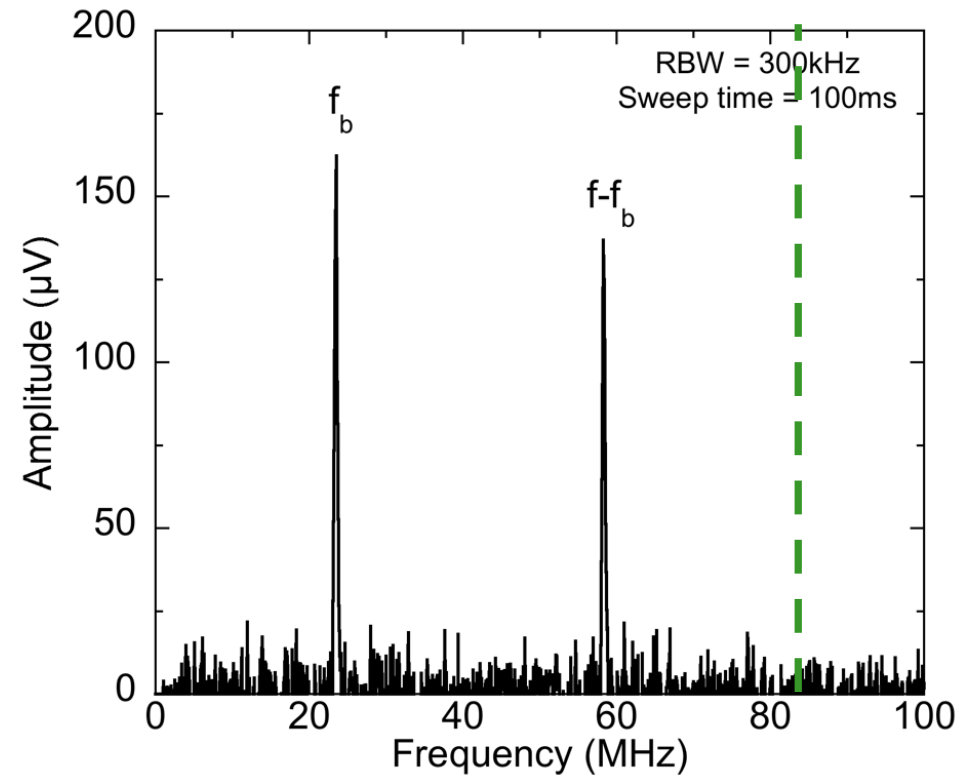
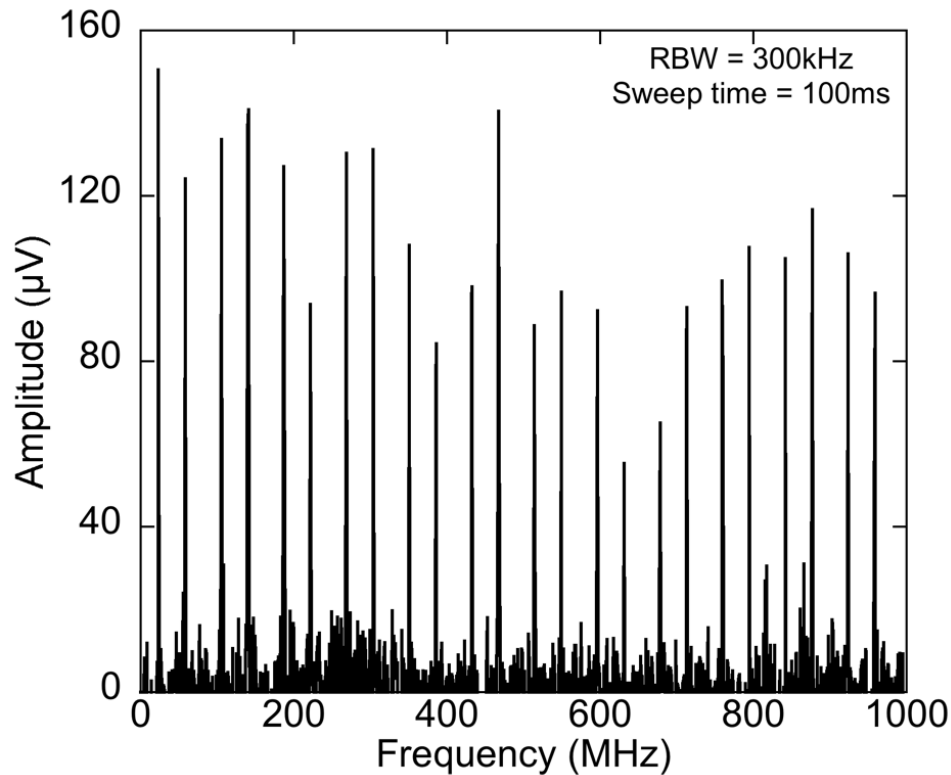




Observation of beat signal (1)

(90GHz freq. multiplier source)

$f=81.6\text{MHz}$

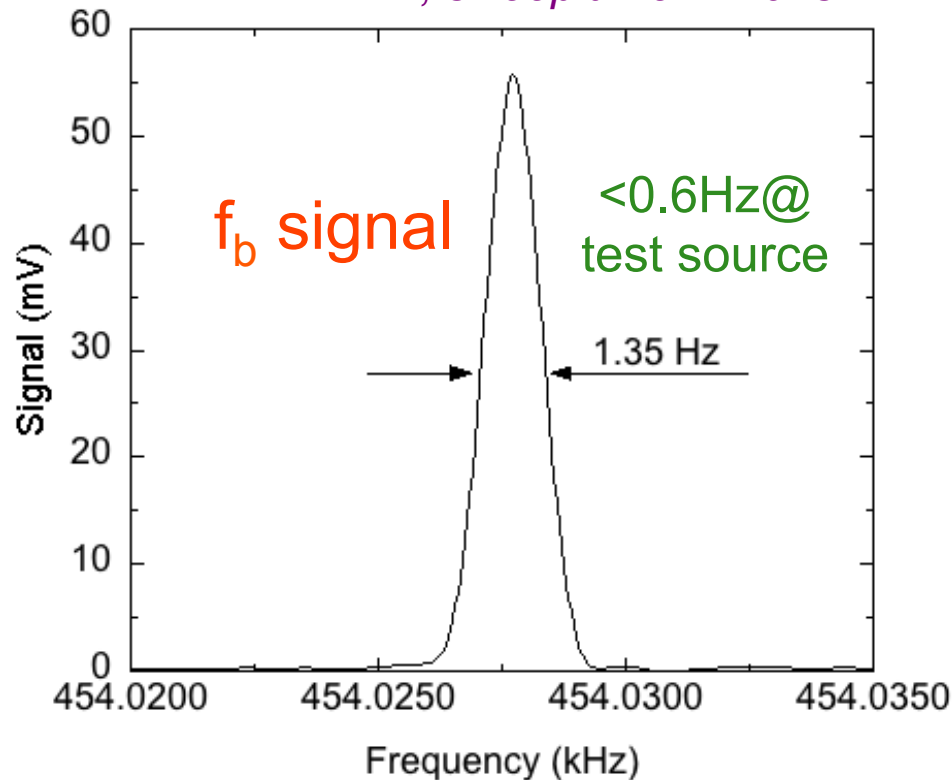


Observation of beat signal (2)

(90GHz freq. multiplier source)

Linewidth

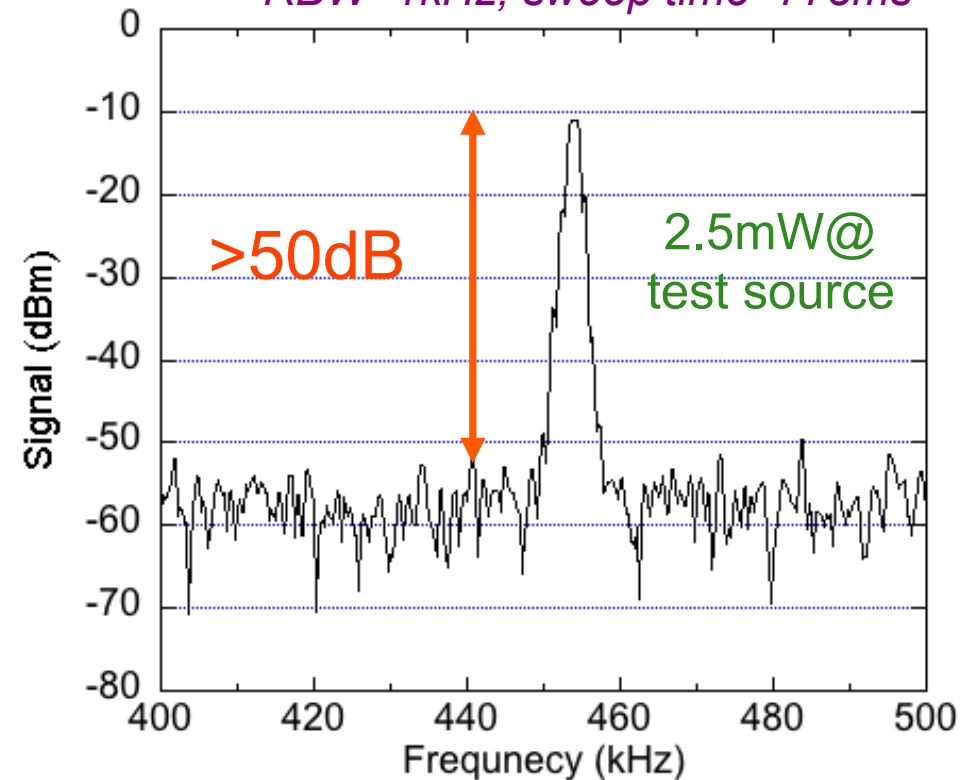
RBW=1Hz, sweep time=2.294s



Linewidth $< 1\text{Hz}$

Signal-to-noise ratio

RBW=1kHz, sweep time=773ms



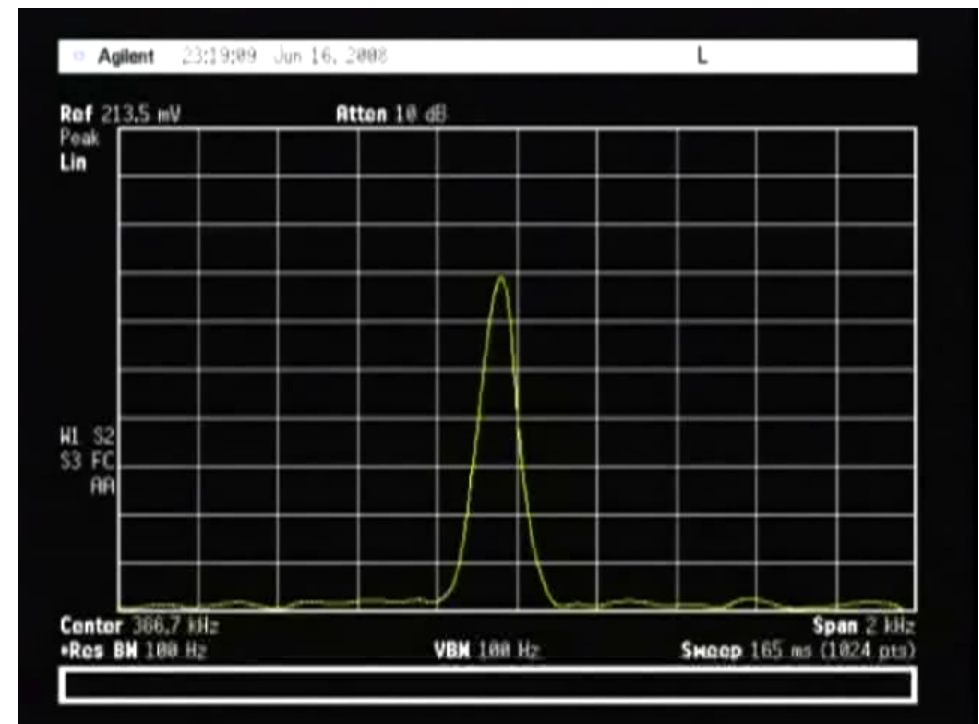
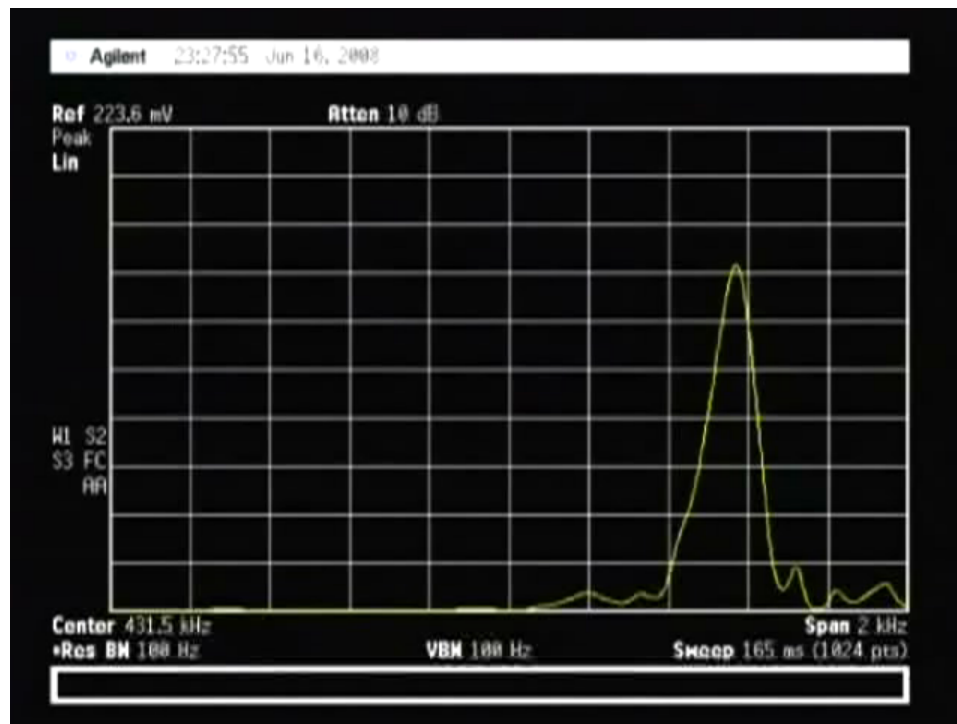
Detection limit = 25nW

Observation of beat signal (3)

(90GHz freq. multiplier source)

Laser control : OFF

Laser control : ON

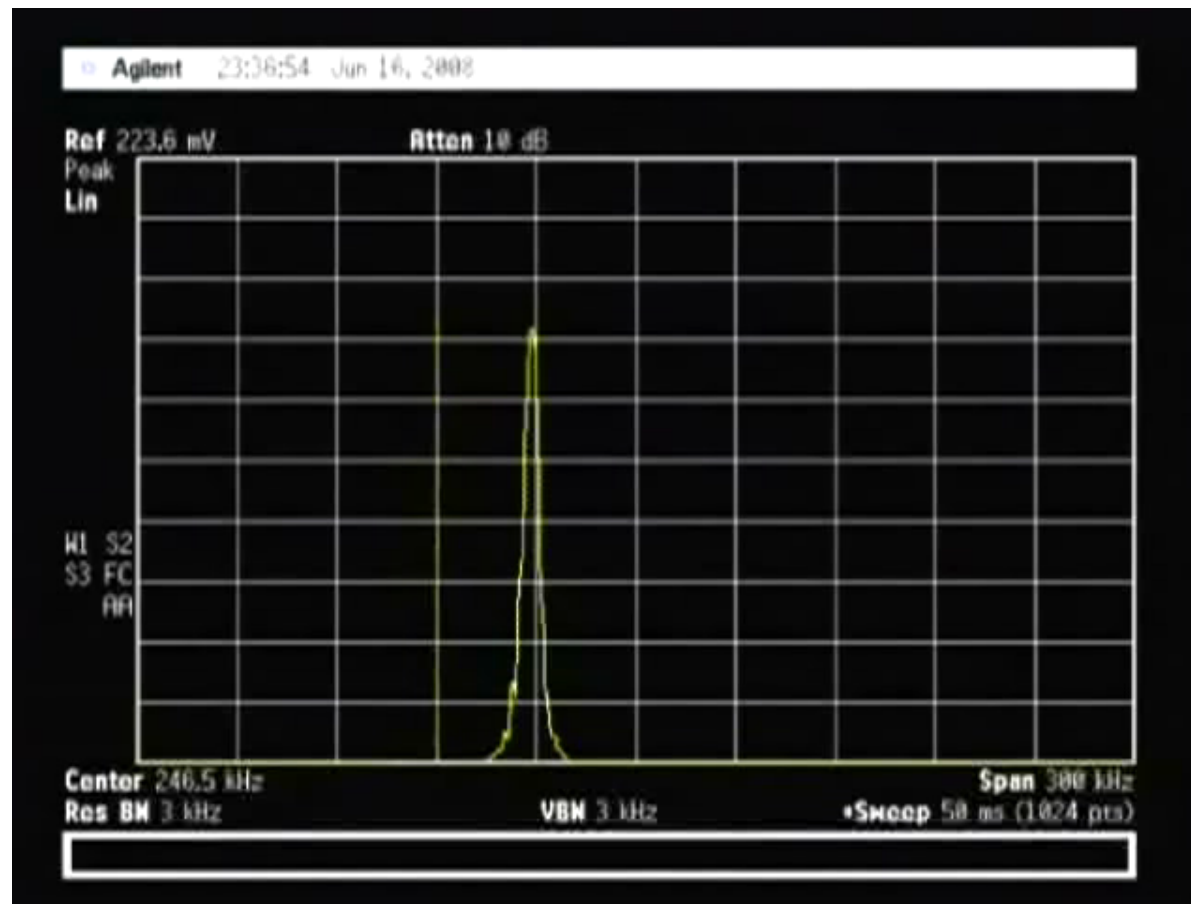


RBW=100Hz, sweep time=165ms, full span=2kHz

Observation of beat signal (4)

(freq. multiplier source wave)

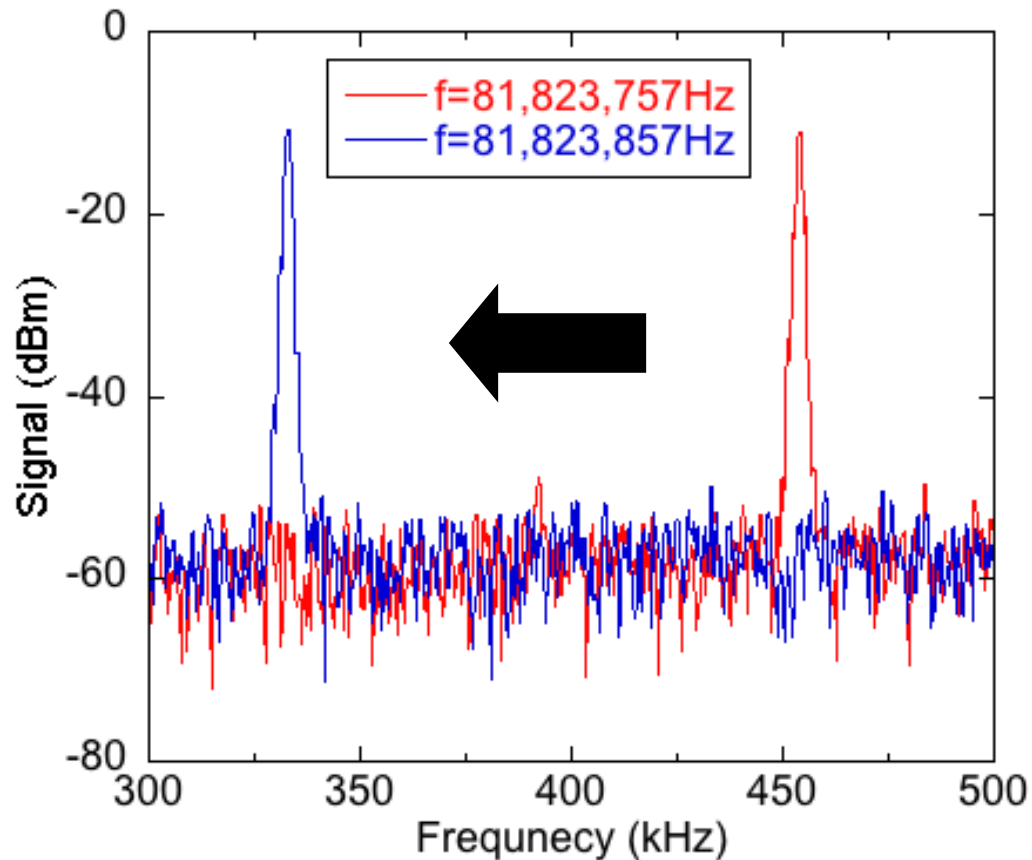
Freq. modulation of test source($100\text{GHz} \pm 87.6\text{kHz} @ 0.5\text{Hz}$)



RBW=3kHz, sweep time=50ms, full span=300kHz

Determination of absolute frequency

~Shift of ML frequency by 100Hz~



$$m = \frac{\delta f_b}{\delta f}$$

$$= \frac{454,027.976 - 333,027.731}{81,823,857 - 81,823,757}$$

$$= 1210.00245$$

$$f_x = mf + f_b$$

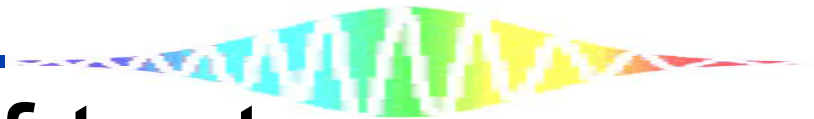
$$= 1210 * 81,823,757 + 454,027.976$$

$$= \underline{99,007,119,997.976 \text{ Hz}}$$

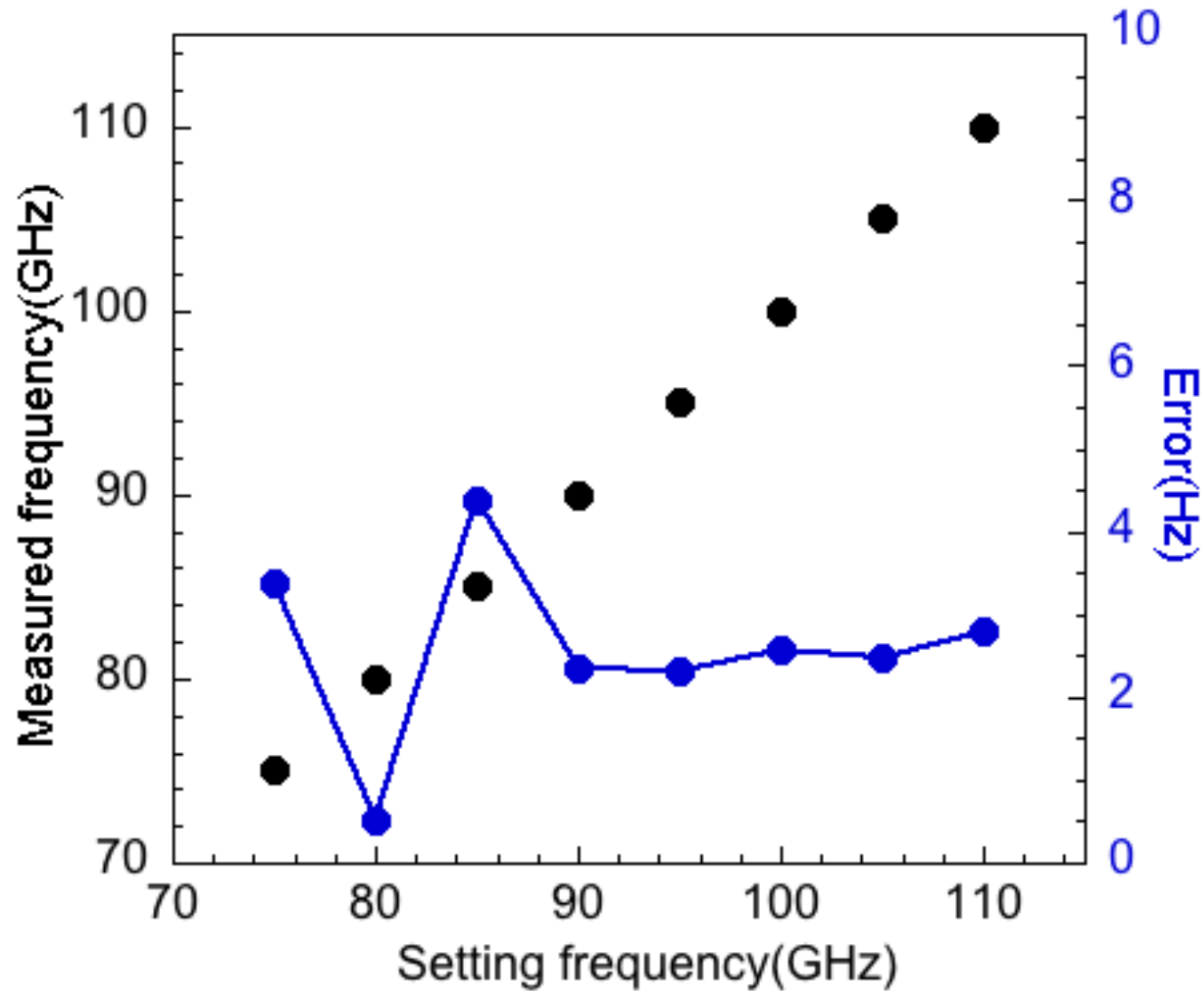


error=2.004Hz

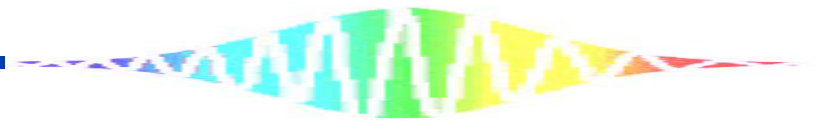
Setting freq. of test source=99,007,200,000 Hz



Frequency tuning of test source



Precision = 2.8×10^{-11}

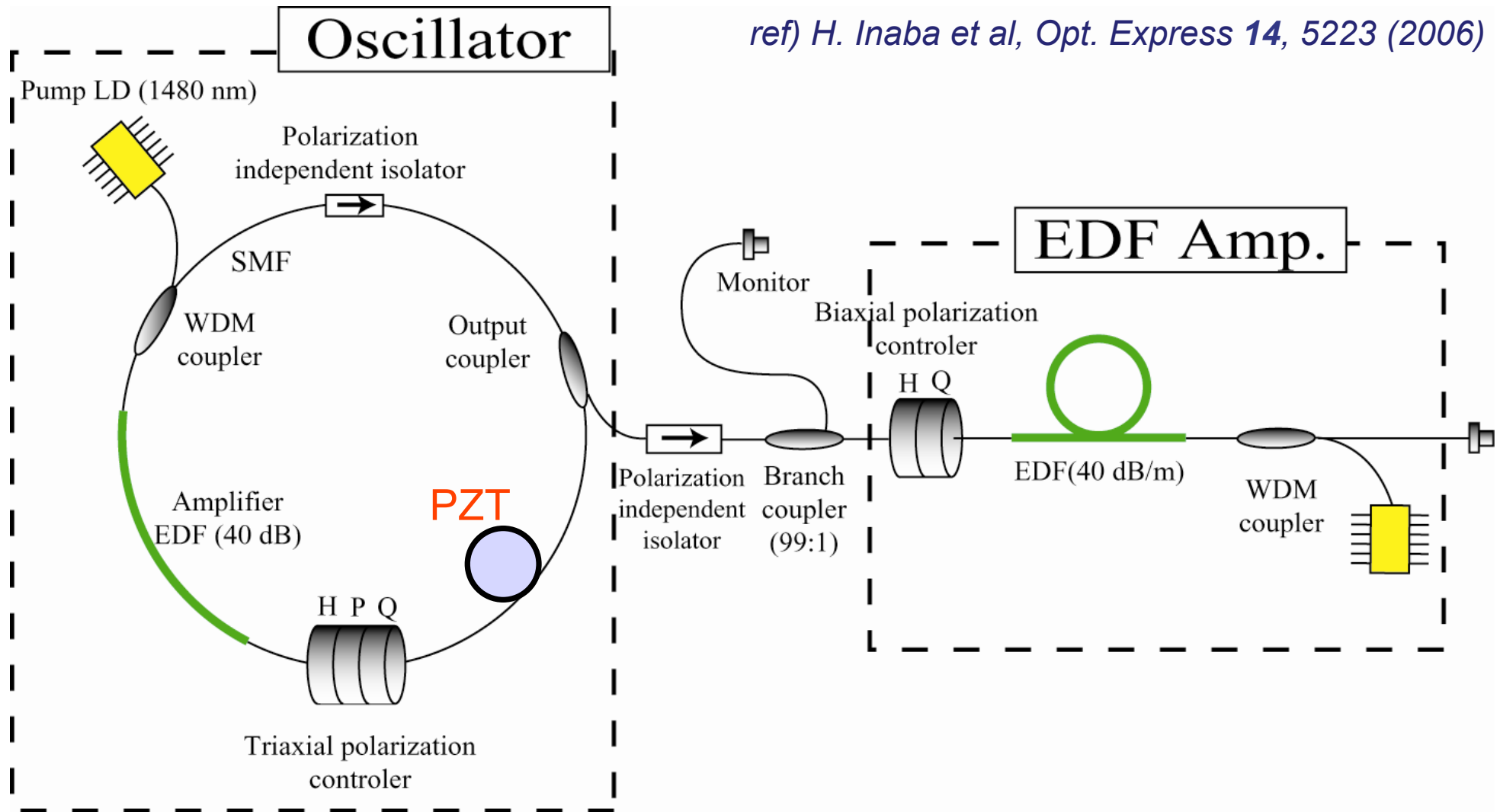


3. Fiber-laser-based THz spectrum analyzer

~simple, compact, inexpensive,
and robust system~

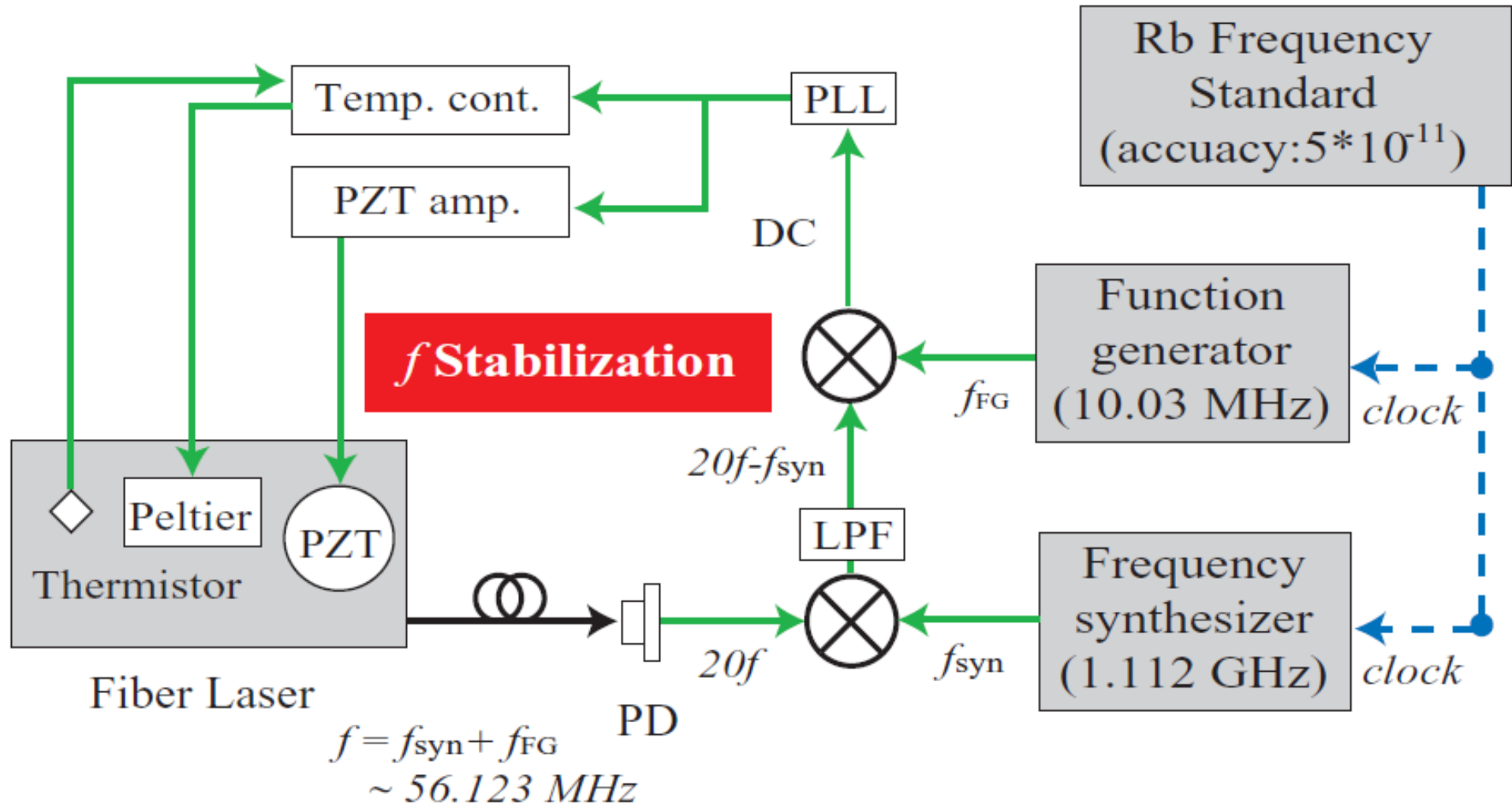
Er-doped fiber laser

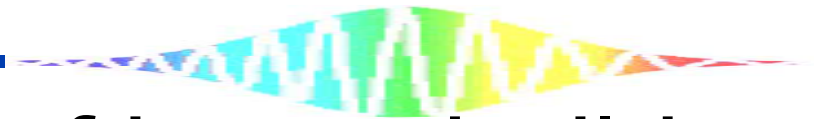
ref) H. Inaba et al, Opt. Express 14, 5223 (2006)



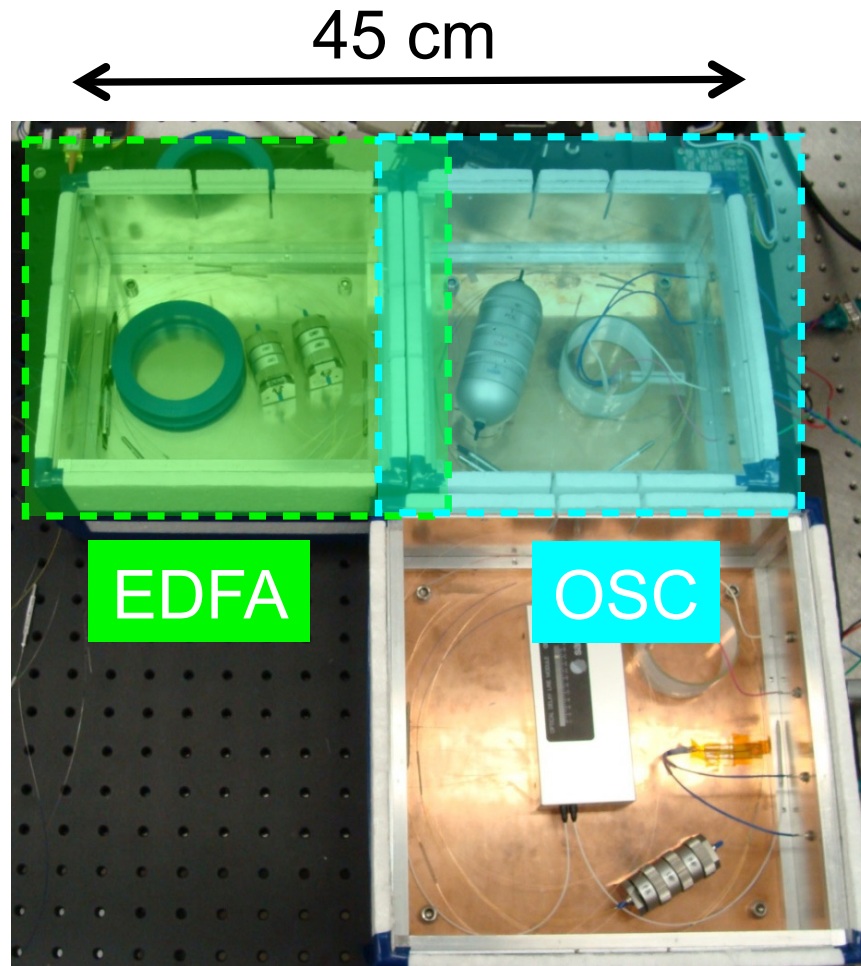
Temp. control (Peltier)

Stabilization system of ML frequency

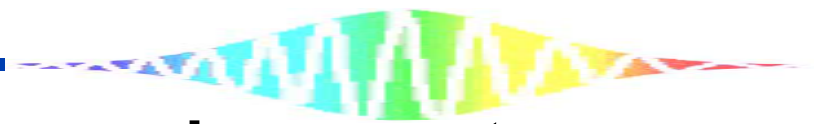




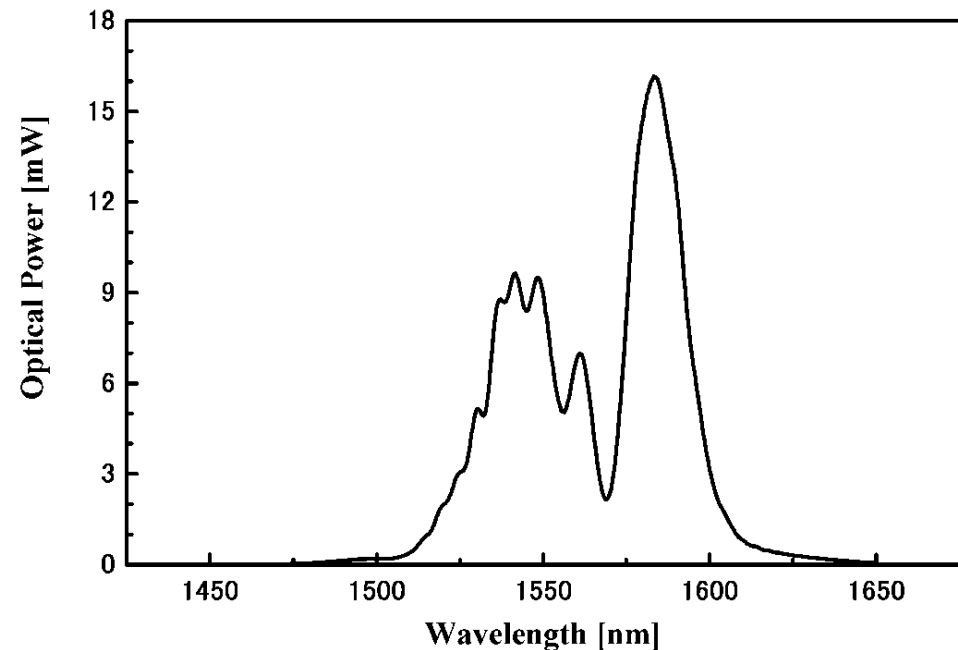
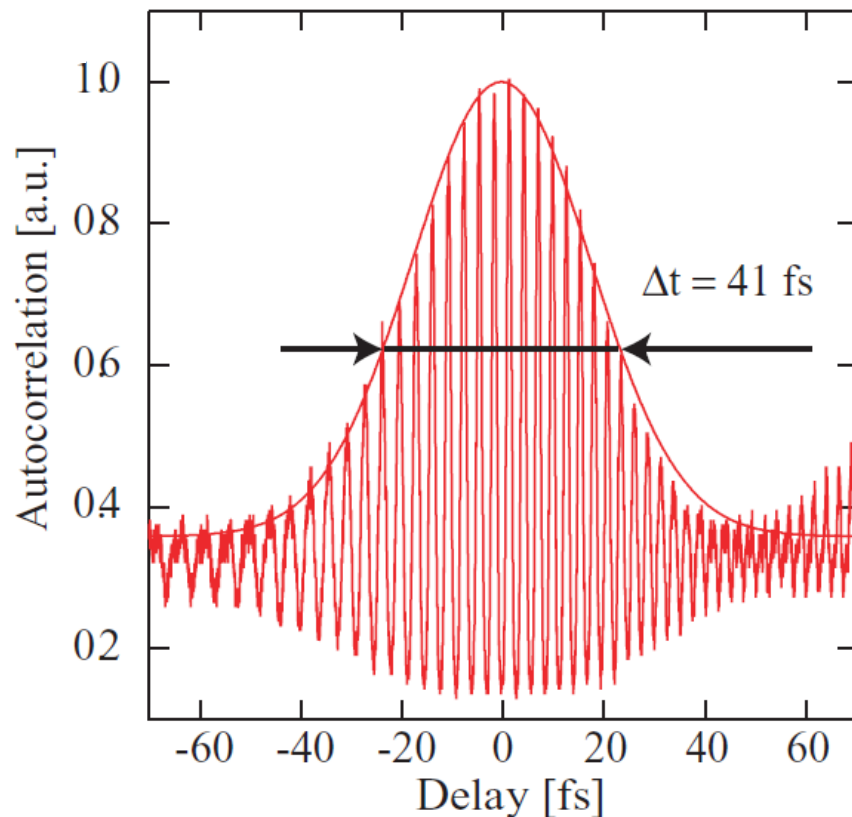
Photograph and cost of home-build fiber laser



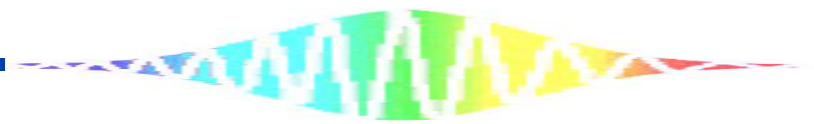
COST	
OSC	¥ 700,000
EDFA	¥ 650,000
Control electronics	¥ 400,000



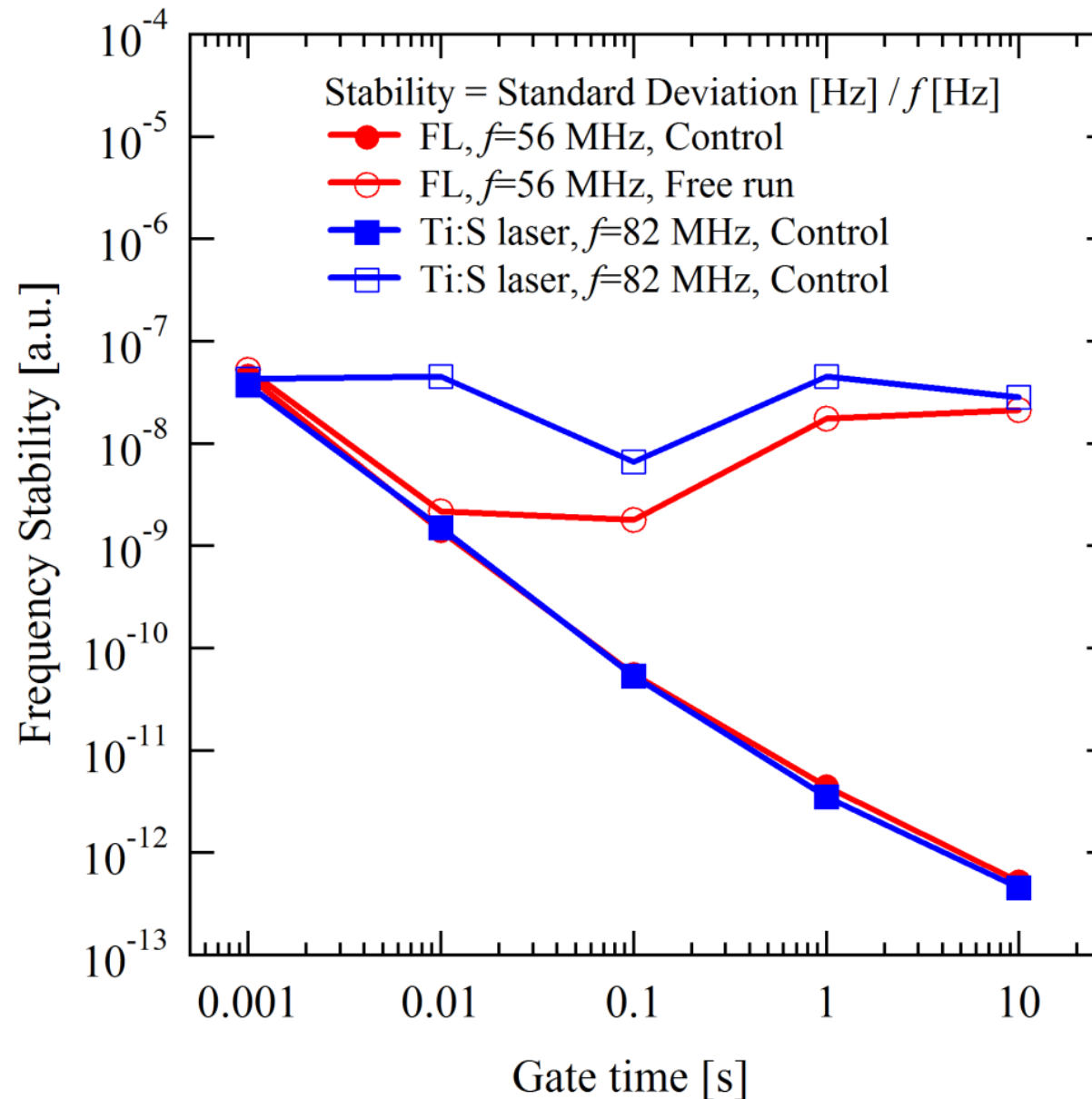
Autocorrelation signal and spectrum



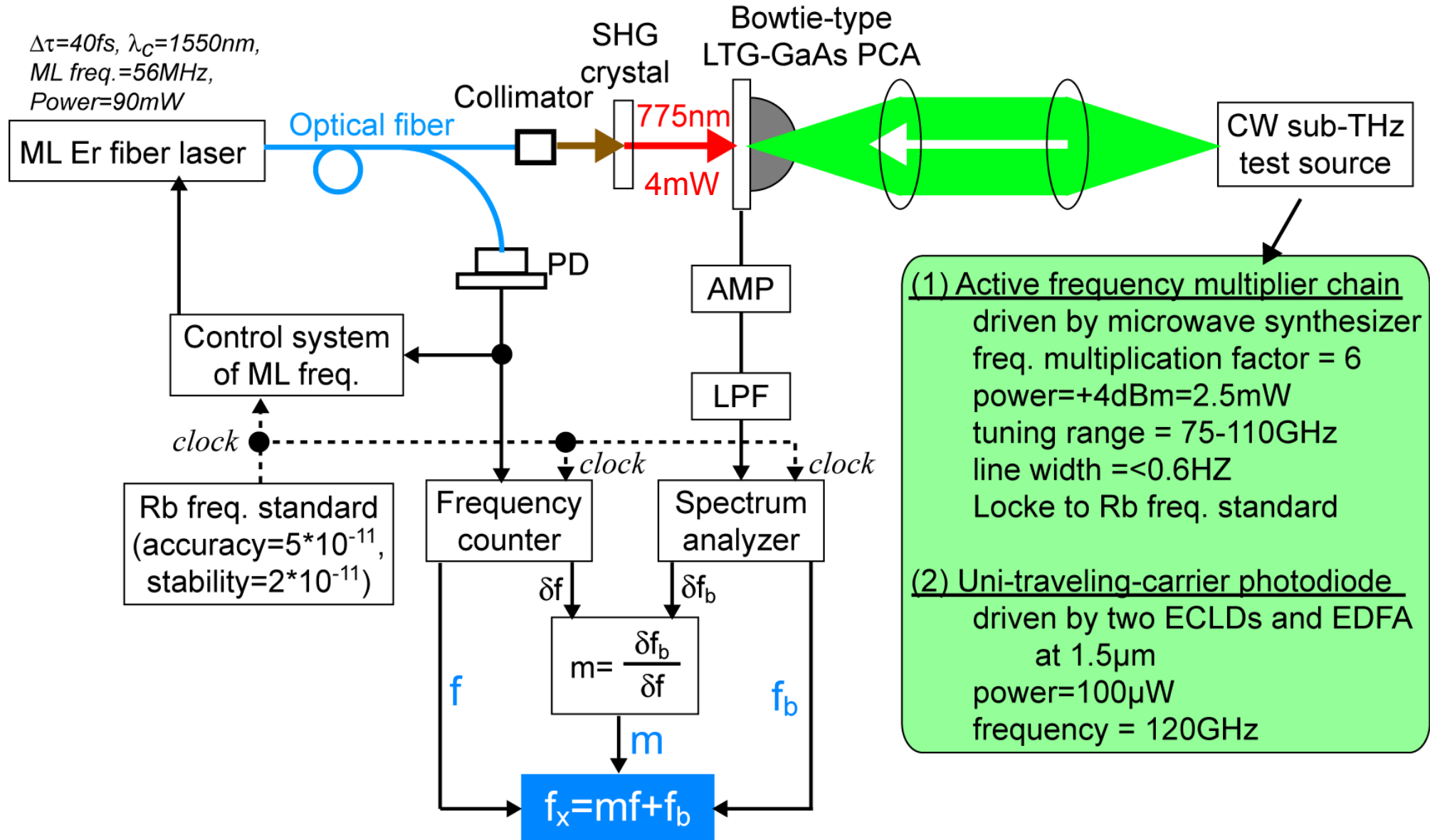
Average power = 90mW@1550nm or 10mW@775nm
Mode-locked frequency = 56MHz



Stability of ML frequency of fiber laser



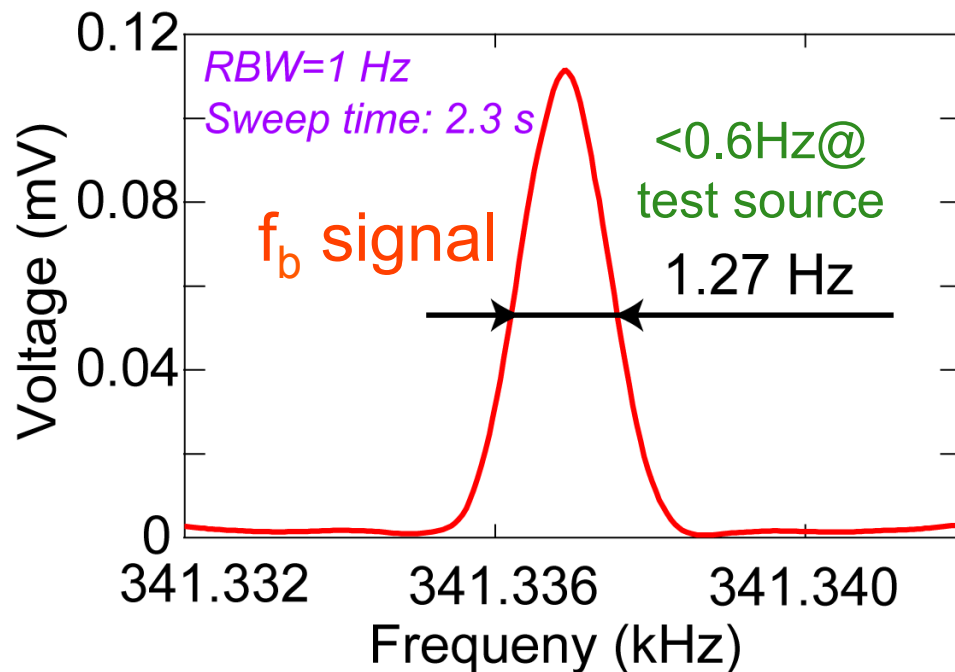
Experimental setup



Observation of beat signal (1)

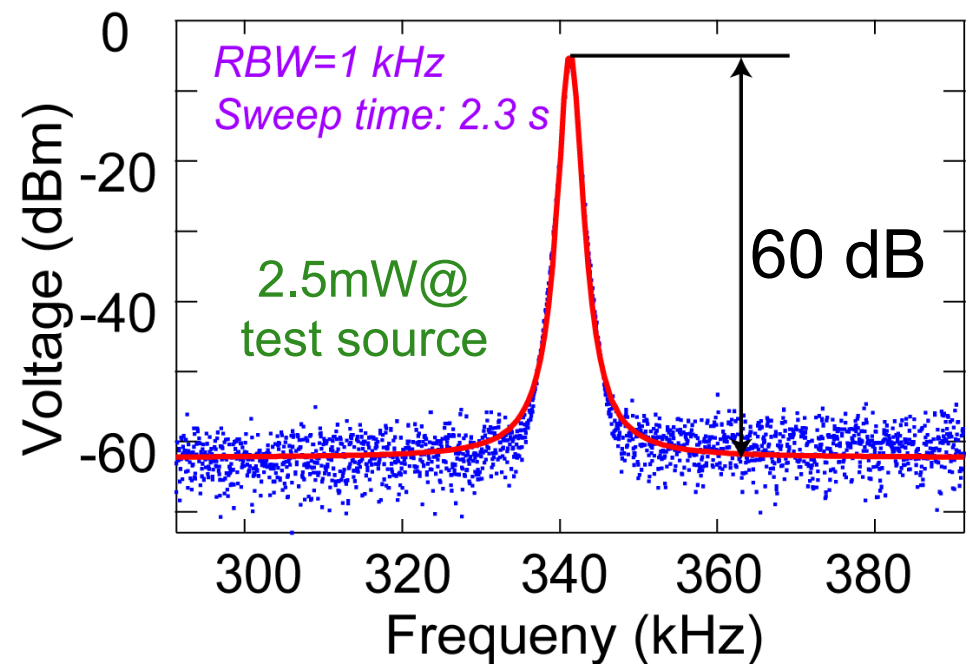
(80GHz active frequency multiplier)

Linewidth



Linewidth $< 1\text{Hz}$

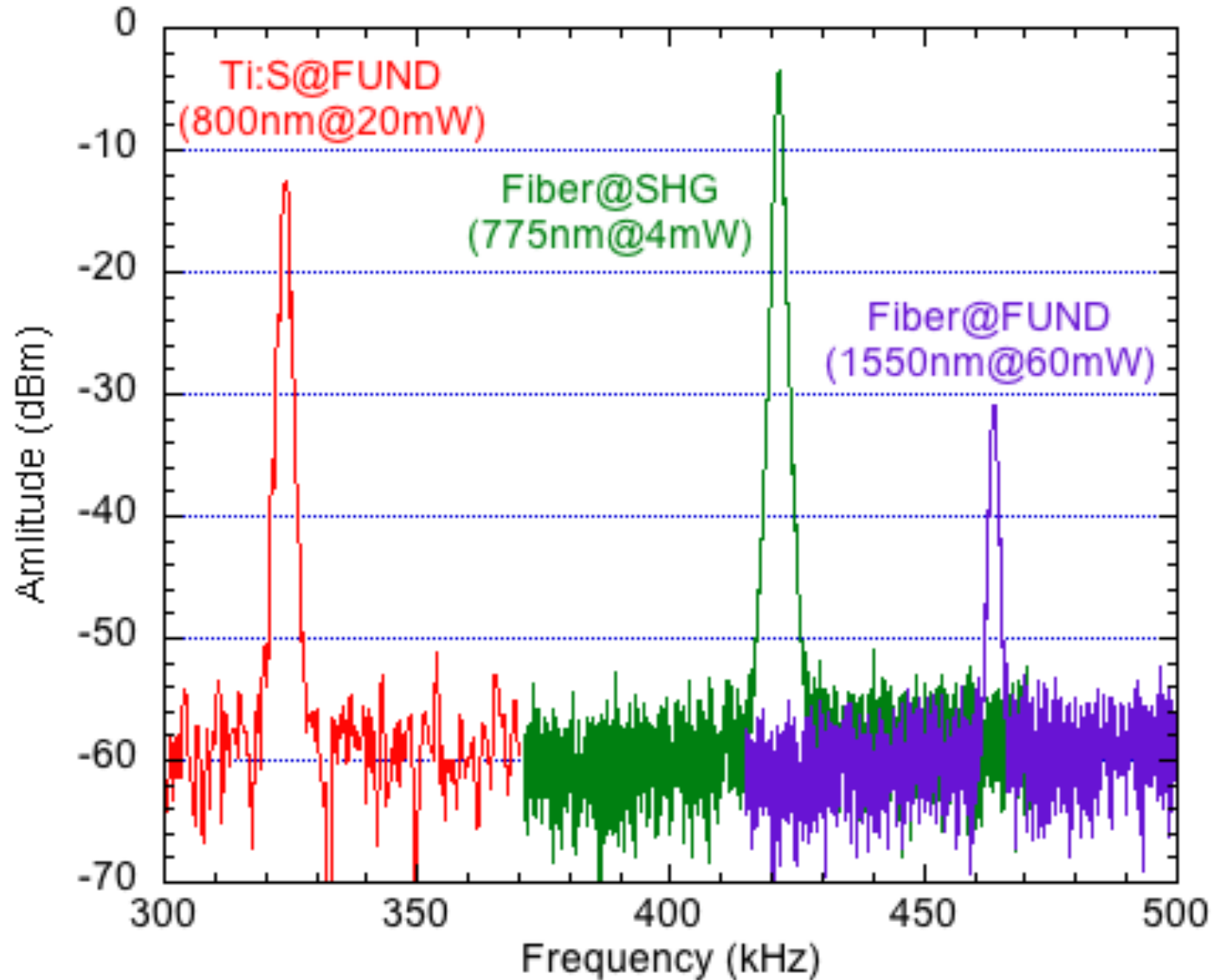
Signal-to-noise ratio



Detection limit = 2.5nW

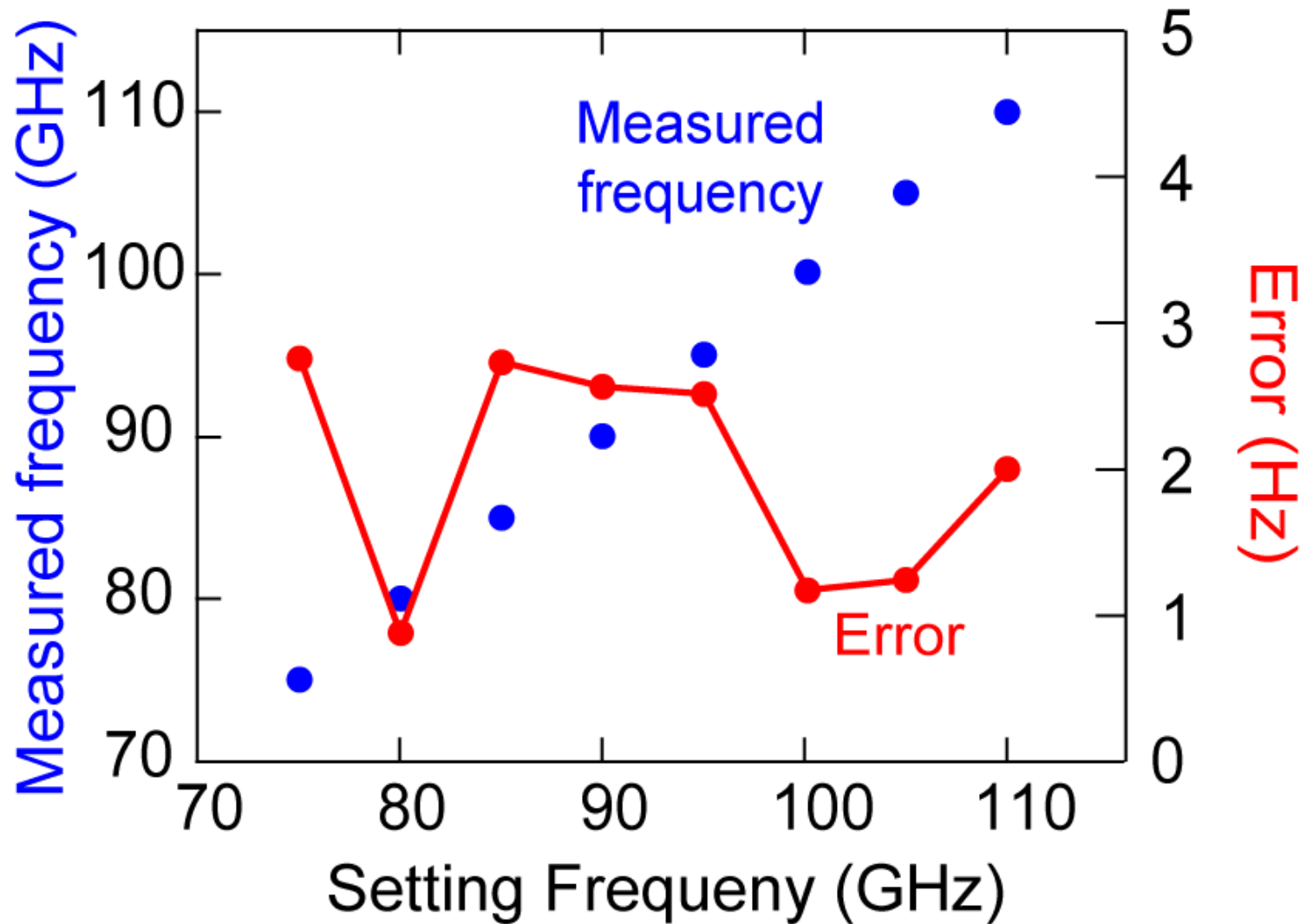
Comparison of f_b beat signal

Bowtie-type LTG-GaAs PCA



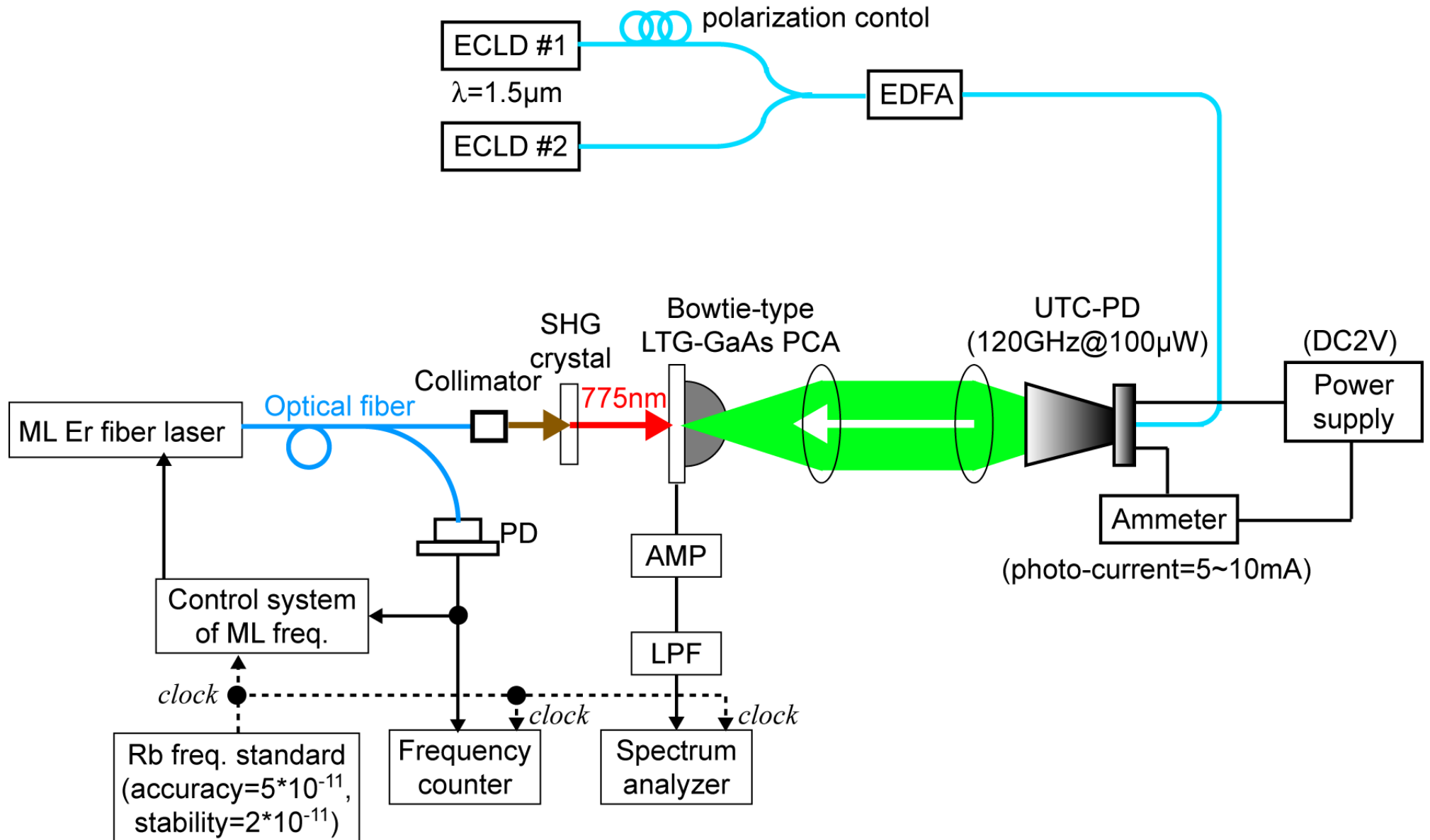
Frequency tuning of test source

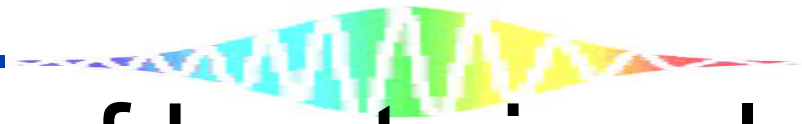
(active frequency multiplier)



Mean precision= 2.2×10^{-11}

Experimental setup for UTC-PD





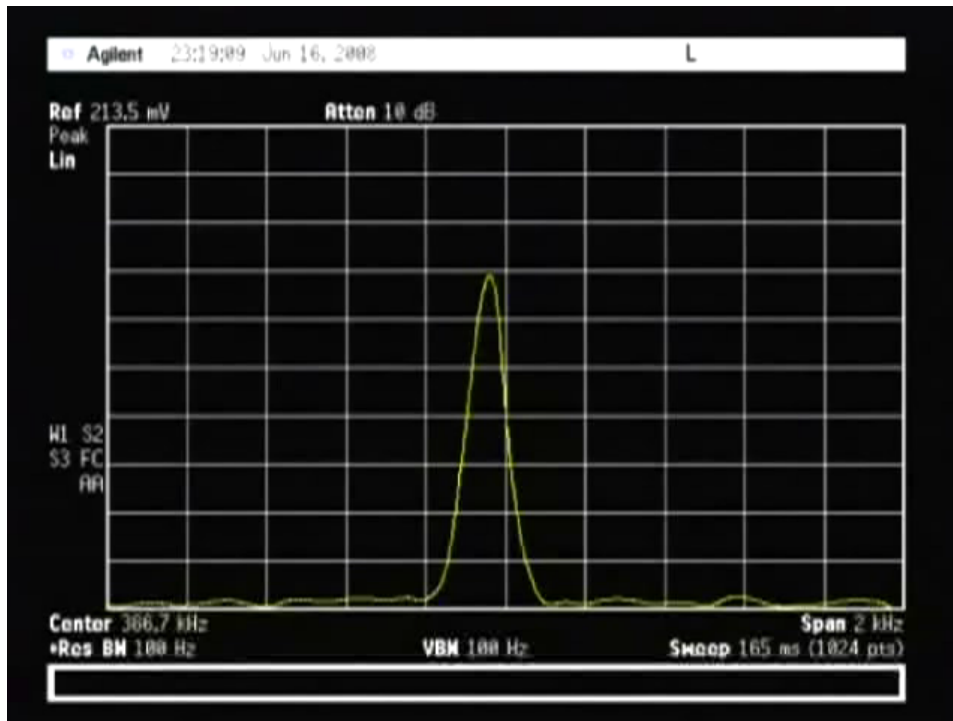
Real-time monitoring of beat signal

80GHz active freq. multiplier
(2.5 mW)

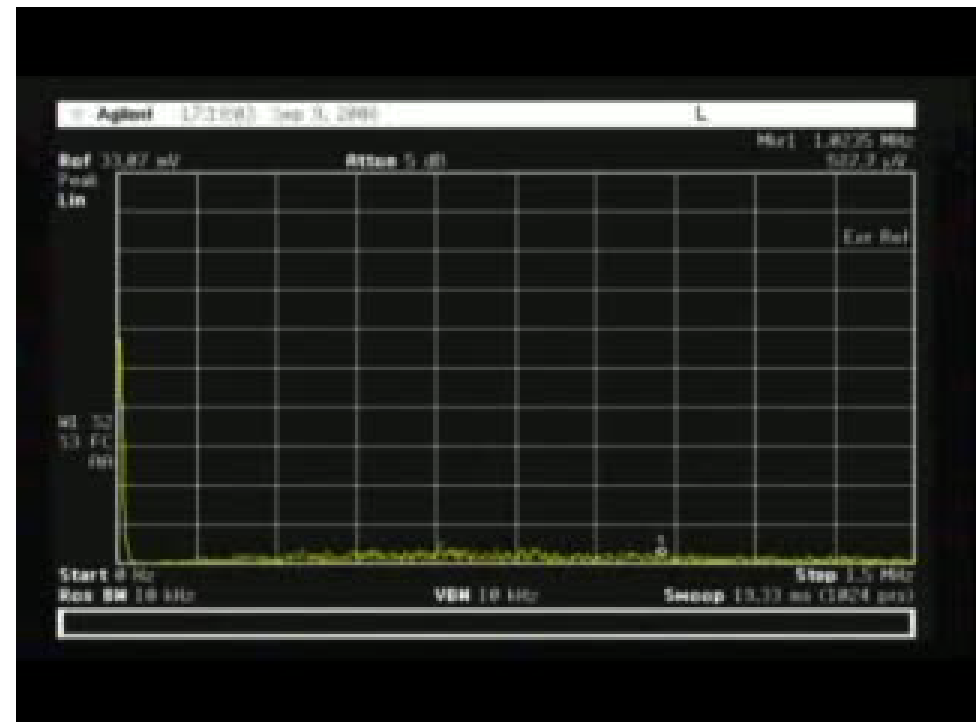
120GHz UTC-PD
(0.1 mW)

← Freq. span = 2 kHz →

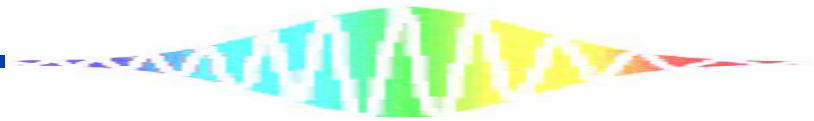
← Freq. span = 1.5 MHz →



Sweep time=165 ms, RBW=100 Hz



Sweep time=20 ms, RBW=10 kHz



Comparison with conventional method

	Conventional methods		Proposed method
	Heterodyning method	Interferometric method	
Principle	Electric heterodyning	Optical Interferometry	PC-THz comb
Range	< 2THz	>several THz	0.1THz~10 THz
Frequency accuracy	10^{-11} (depending on local oscillator)	10^{-9} (depending on interferometry)	10^{-11} (depending on PC-THz comb)
Detector	Antenna	Bolometer (cooling)	PCA
Mixer	SIS, bolometer, etc (cooling)	Beamsplitter	
Apparatus	Complicated	Complicated	Simple