

Diffusion and Relaxation Probed by Mobile NMR



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RWTH Aachen University, Germany



The Menu

Preface

Introduction

Magnets and applications

Summary

MS Thesis



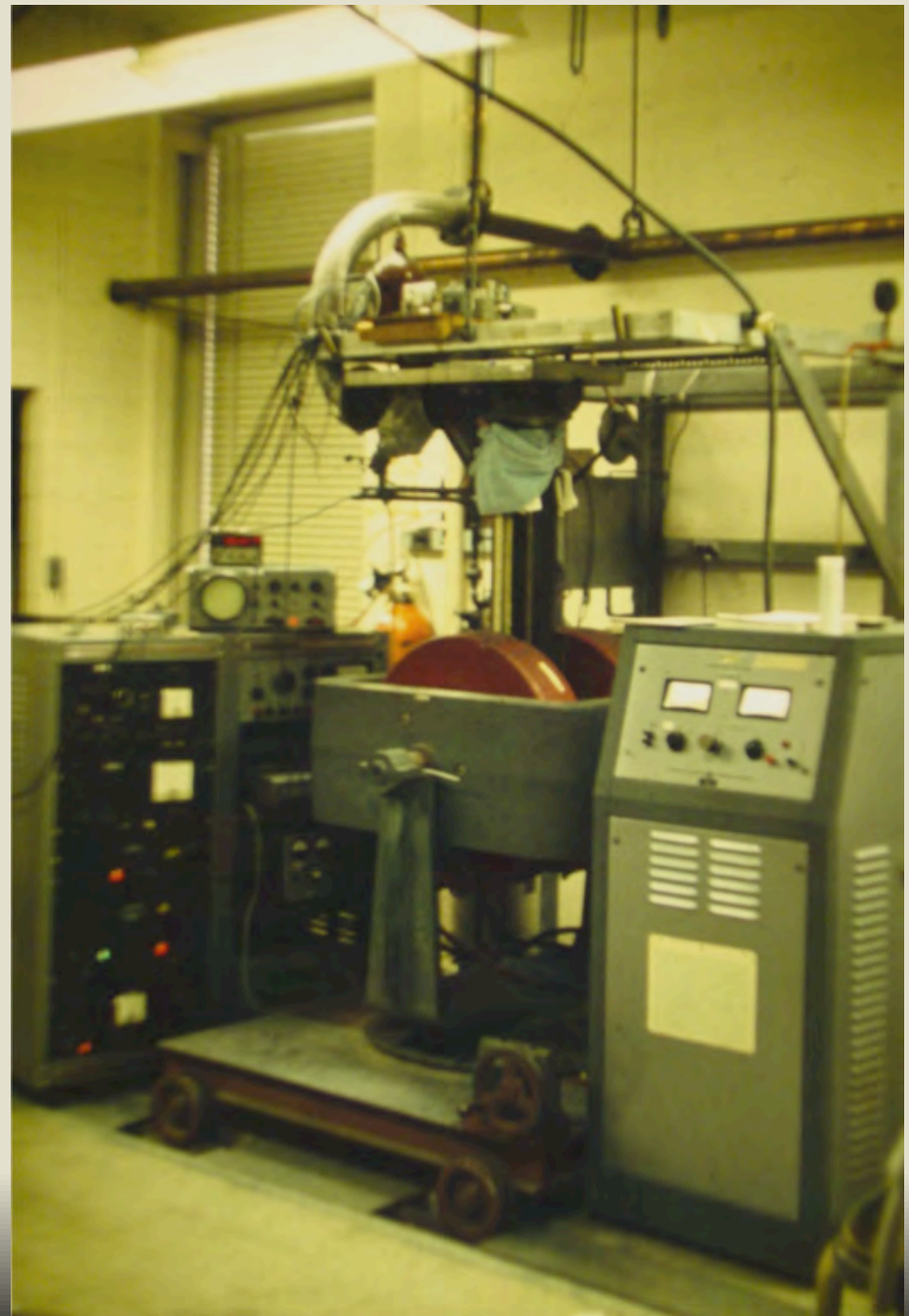
P. A. Casabella



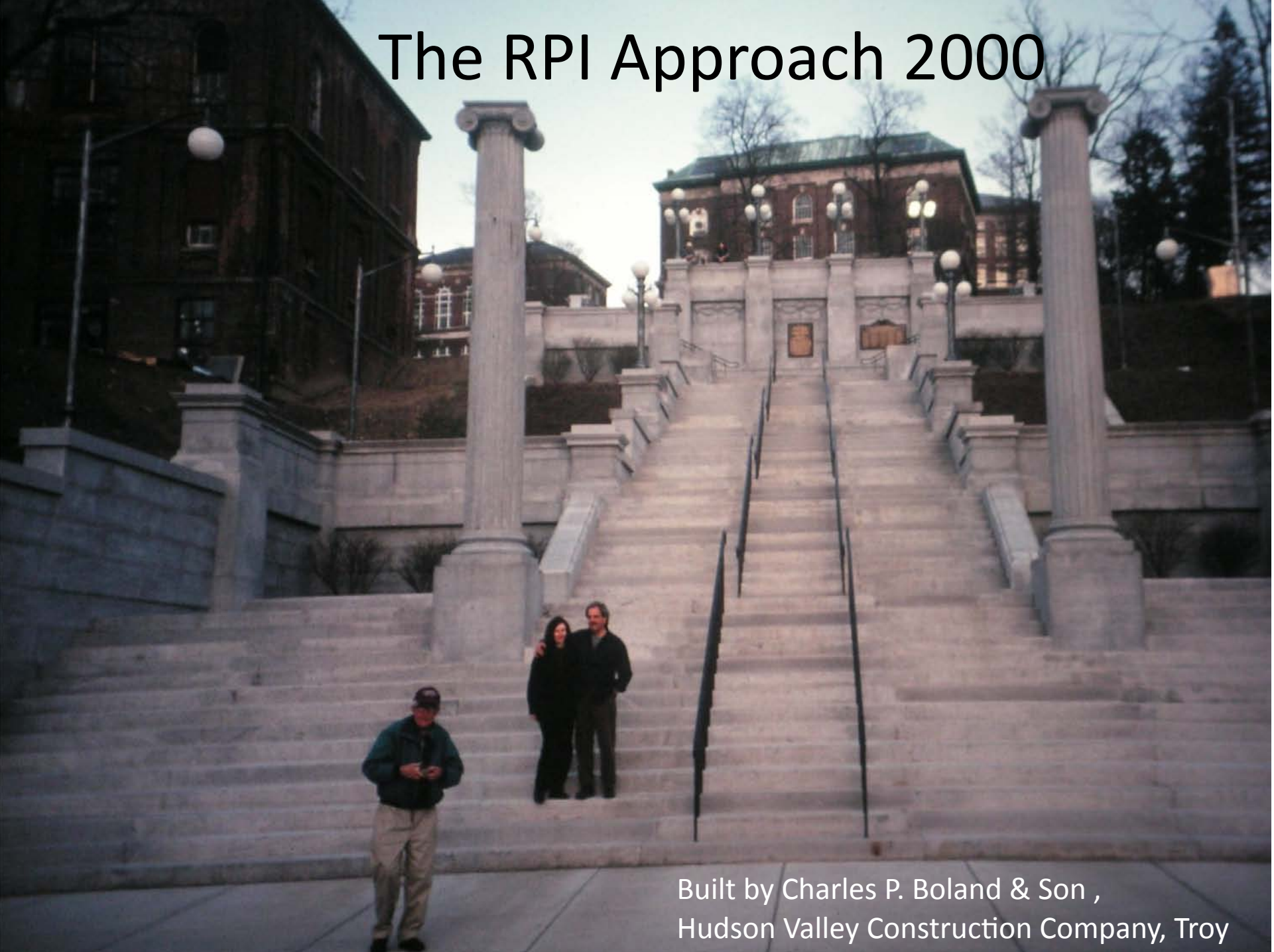
Gerhard Salinger



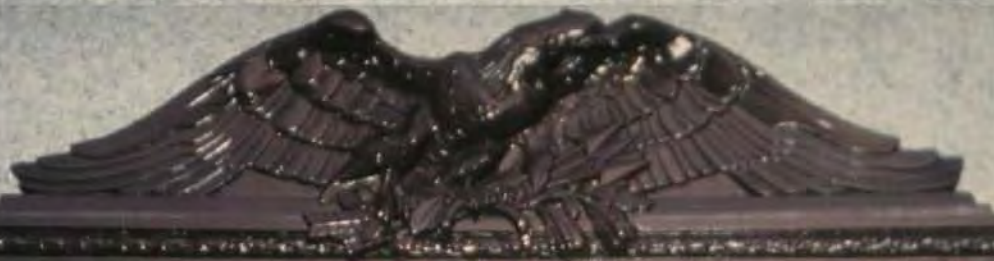
NMR Investigation of Al^{27} in
Rogers and Williamson
Glass, RPI, February, 1976



The RPI Approach 2000



Built by Charles P. Boland & Son ,
Hudson Valley Construction Company, Troy



ROLL OF HONOR

IN MEMORY OF RENSSELAER MEN WHO GAVE THEIR LIVES
IN THE ARMED FORCES SERVING OUR COUNTRY
DURING THE SECOND WORLD WAR 1941-1945



MAURICE P. ALGER, JR.
ARTHUR F. AMADON, JR.
ELLSWORTH B. ATWOOD
JOHN J. AVIZA
ALBERT K. BACK
LEONARD F. BARRY
ROBERT J. BARTLEY, JR.
HILAND G. BACHELLER, JR.
LESTER R. BESSELL, JR.
HOWARD J. BLIND
HARRY A. BOLLES
JAMES D. BONNYMAN
WILLIAM E. BOULEY, JR.
GEORGE W. BRADLEY
H. GUYON BRIGHTLY
ROBERT P. BROWN
WALTER BROWN, JR.
RICHARD M. BUCK, JR.
JAMES E. BUCKLEY
EDWARD R. BUDZ
ROBERT CAMPBELL, JR.
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JACK S. COLLINS
JAMES F. CONWAY
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HUGH W. CURTIS
STEPHEN H. CURTIS, JR.
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FREDERICK S. D. BENEDETTO
W. WILLIAM DEBENHAM
DAVID O. DEVLIN
HOWARD H. DISBROW
PAUL A. DOCKLER
GORDON L. DOCKSTADER
FRANK A. DOLE, JR.
WILLIAM D. DUCHARME
EDWARD H. ENNERS, III
CHARLES W. ERICHSEN
J. DONALD FINDLAY
F. GURNEY FINE, JR.
ROBERT S. FINK
GEORGE S. FITCH

RALPH N. FOUNTAIN
GERALD A. FRANKENSTEIN
AUGUST GBIB, JR.
DONALD F. GILBERT
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HAROLD E. GUNDEL
RALPH I. GUNDEL
JOHN R. HADLEY
JAMES D. HANCOCK
MEERILL A. HANCOCK
HENRY F. HARRIS
DAVID B. HIGGINS
ROBERT W. HINE
HENRY D. HUDSON
ERNEST KERTSCHER, JR.
NORMAN H. KIBB, JR.
ELMER KUPSENEL
C. WILLIAM LAW
ROY F. LAYER
WILLIAM M. LICKEL

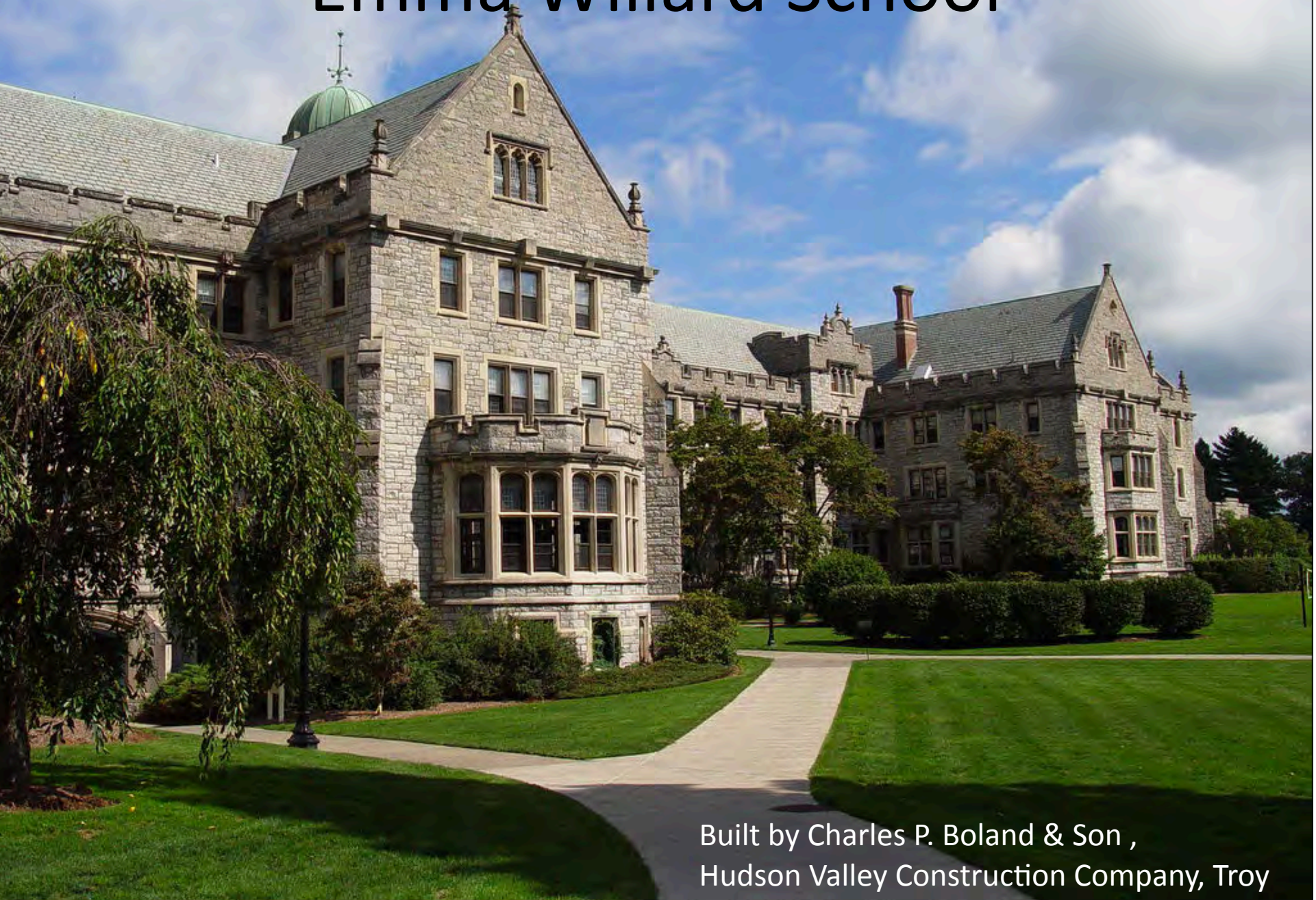
ISAAC M. LOBELL
ARTHUR H. MAKI
JOHN MCBRIDE, JR.
WILLIAM S. McHENRY, JR.
F. TYLER MORRISON, JR.
FRANK A. MURPHY
ALFRED R. NEWBERG
FRANK M. NUENENT
FRANK C. PAGE
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JACOB M. PROSTUPAK
FRANK W. PRESCOTT, JR.
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WALTER H. REICHHOLD
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JOSEPH M. ROCHE
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FRANK K. SEIDEL, JR.
H. OAKLEY SHARP, JR.

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CARL M. THOMAJAN
ROGER S. THOMAS
LEONARD H. THORNTON
TORAEF TORIASEN
ROBERT V. TURCHETTO
RICHARD M. VAN GALDER
IGOR V. VASSILIEFF
RICHARD G. VILLOCHI
JAMES M. WALLACE
WILLIAM A. WALSH
WILLIAM J. WALSH
DONALD M. WILKIE
JOHN H. WINSCHUH
JOHN A. ZIMMERMANN



Built by Charles P. Boland & Son ,
Hudson Valley Construction Company, Troy

Emma Willard School



Built by Charles P. Boland & Son ,
Hudson Valley Construction Company, Troy



McCarthy Building

The **McCarthy Building** is located on River Street on the west side of Monument Square in [Troy](#), New York, United States. It was built in 1904, and remains in use as a commercial building. In 1970 it was added to the [National Register of Historic Places](#) in 1970, along with the nearby [Cannon Building](#). Since 1986 it has also been a [contributing property](#) to the [Central Troy Historic District](#).

Charles P. Boland,
Hudson Valley Construction Company, Troy

Proctor's Theatre



Troy



Schenectady

Troy: It cost \$325,000[3] to construct, and when it opened in 1914 it became the largest theater in the state and was praised as "a structure ranking foremost in American theatrical circles".



Stairs of the NY State Capitol

Built by Charles P. Boland & Son , Hudson Valley Construction Company, Troy

The D&H Building (SUNY administration)



Built by Charles P. Boland & Son ,
Hudson Valley Construction Company, Troy

Conventional NMR Magnets

The object is enclosed by the magnet



Electromagnet from Königsberg / Jena



High-field NMR at RWTH Aachen University

State-of-the-Art NMR Instrumentation

Small-scale NMR

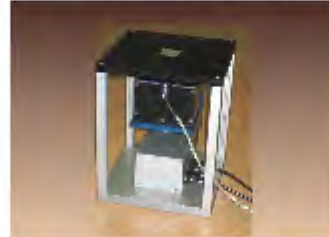
Large-scale NMR

Nobel prizes

Closed magnets

Open magnets:
NMR-MOUSE

Relaxometry



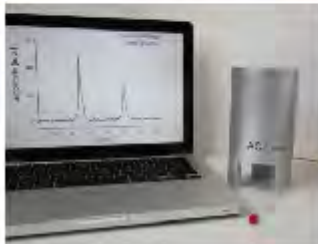
1952 Nobel prize in Physics:
Edward Purcell, Felix Bloch
... for measuring NMR ...

Tomography



2003 Nobel prize in medicine:
Paul Lauterbur, Peter Mansfield
... discovery of NMR tomography...

Spectroscopy



1991 Nobel prize in Chemistry:
Richard Ernst
... high-resolution NMR spectroscopy...
2002 Nobel prize in Chemistry:
Kurt Wüthrich
... NMR of biological macromolecules...

Basic NMR Methods

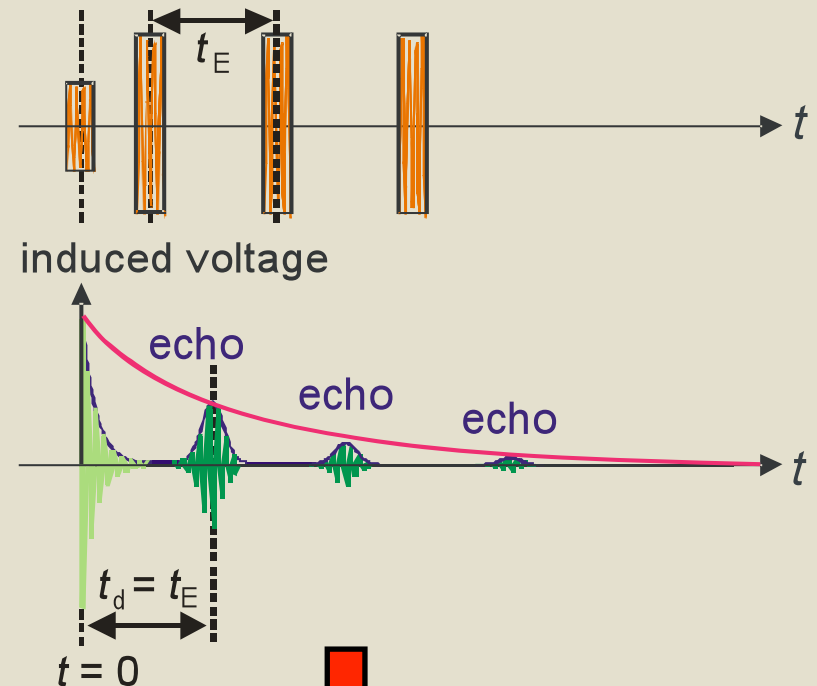
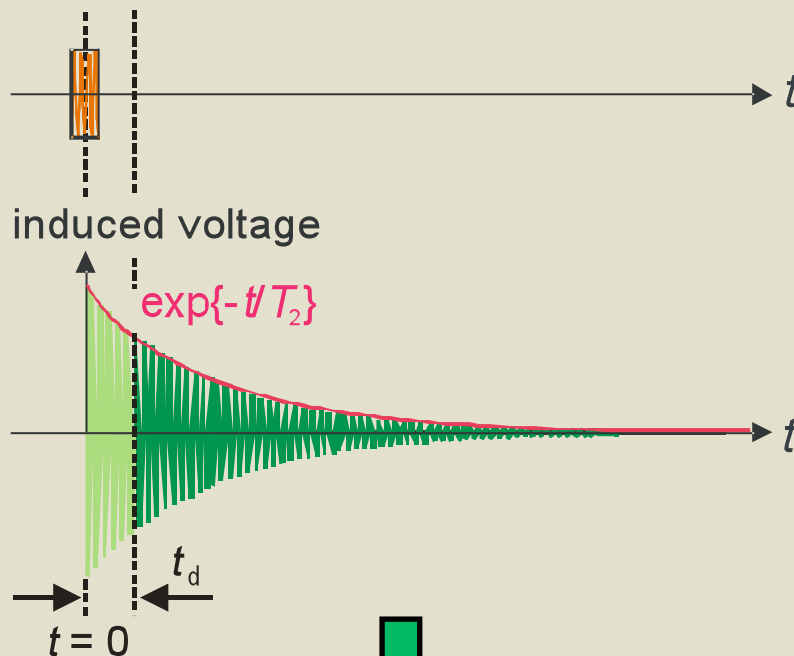
pulsed excitation

homogeneous magnetic field

inhomogeneous magnetic field

rf excitation impulse

rf excitation impulses



Fourier transformation

Laplace transformation

frequency distributions: spectrum, image

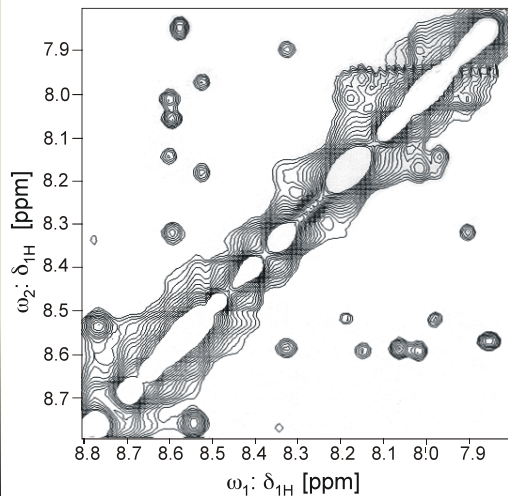
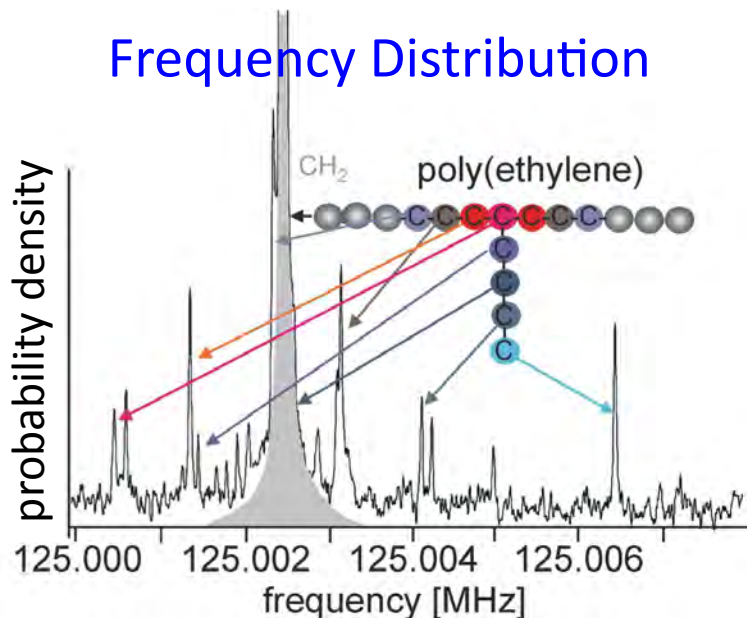
relaxation-time distributions

Fourier and Laplace NMR

Fourier NMR: Spectroscopy, Imaging

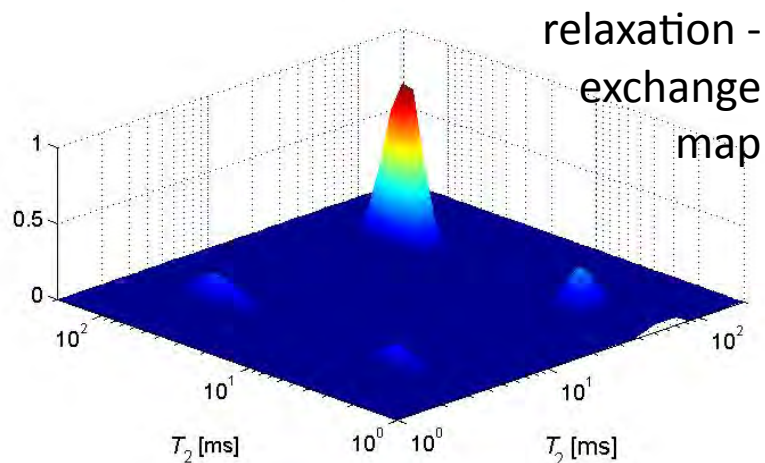
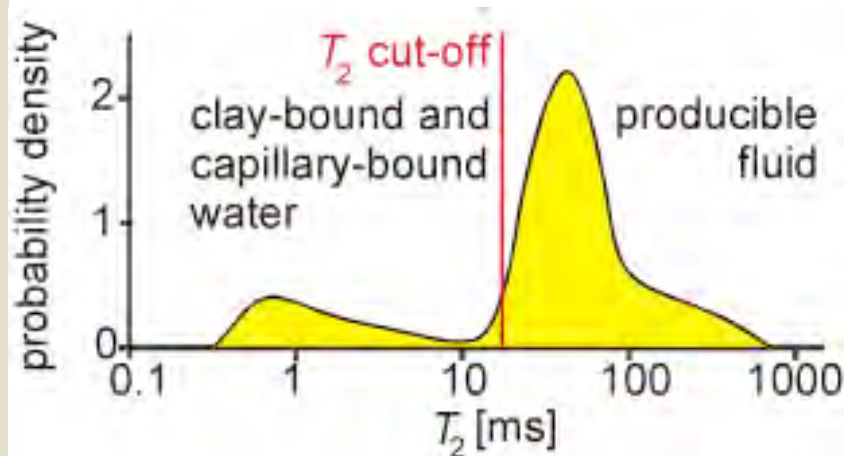
Laplace NMR: Material Properties

Frequency Distribution



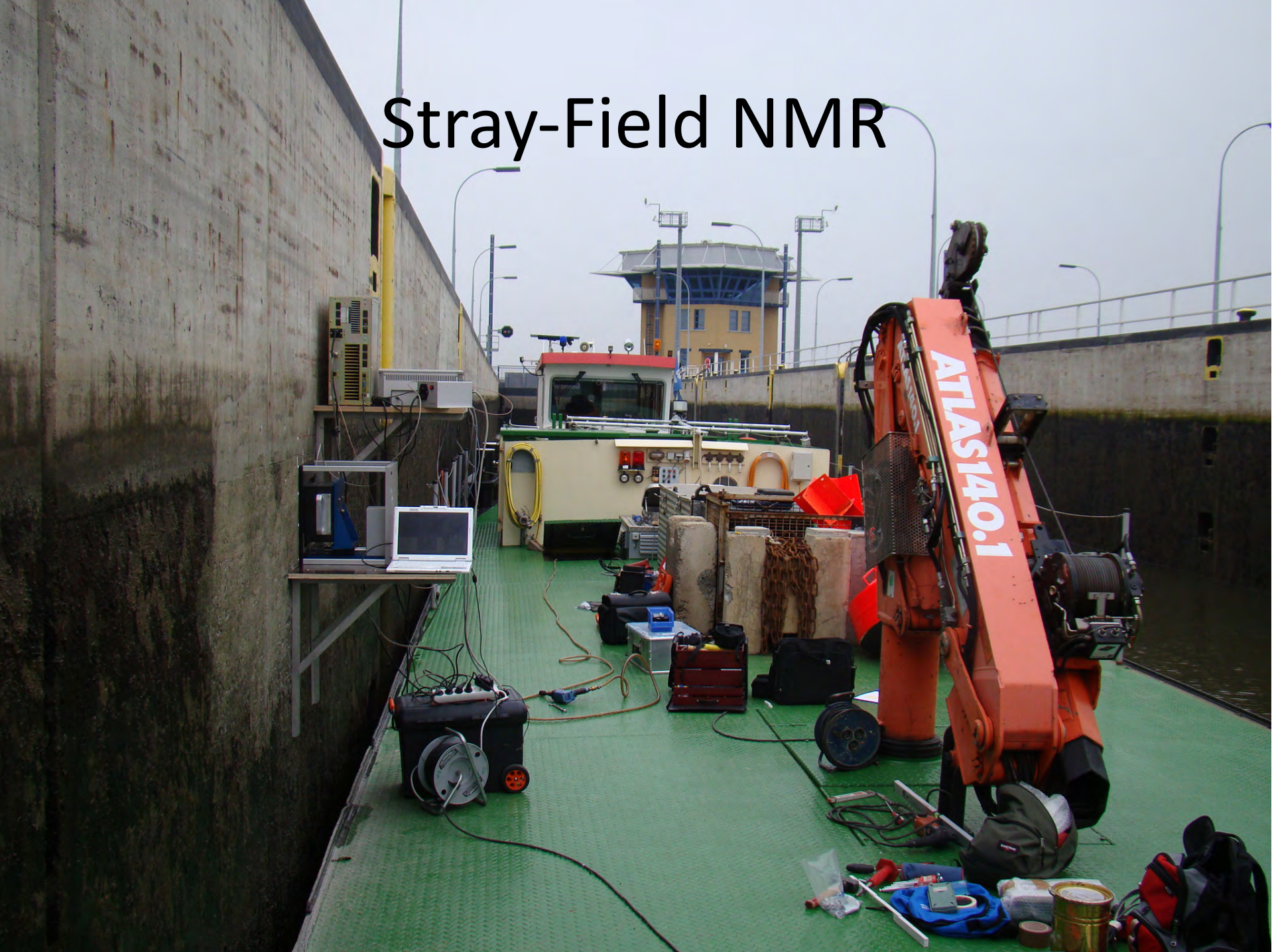
chemical structure and conformation

Relaxation-Time Distribution

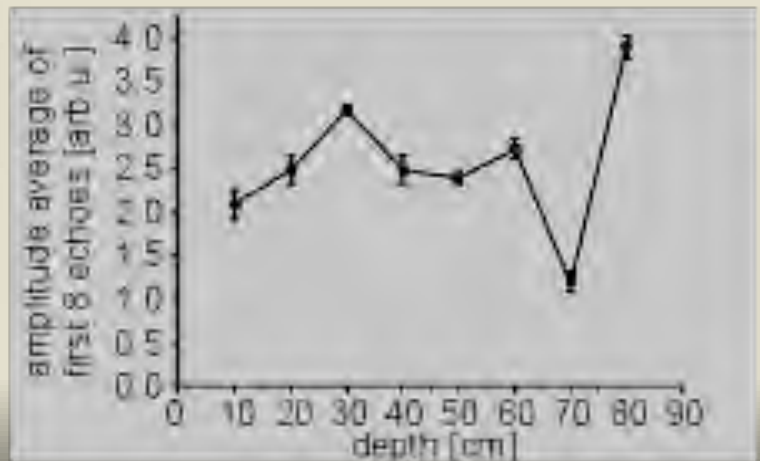
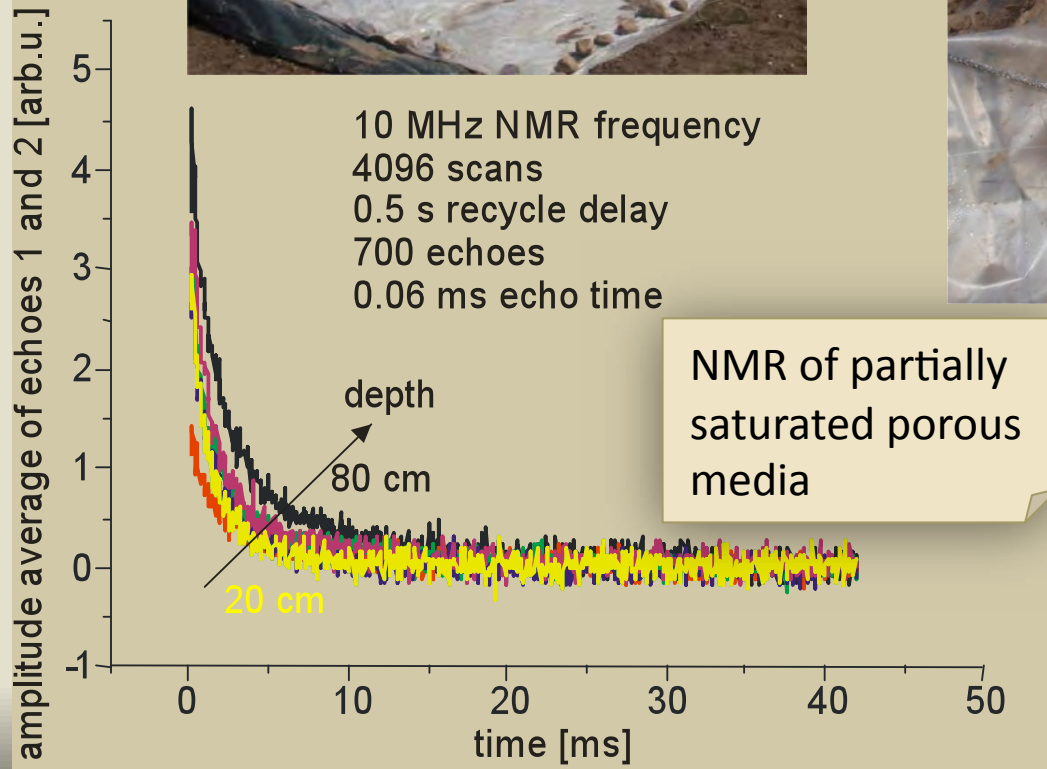
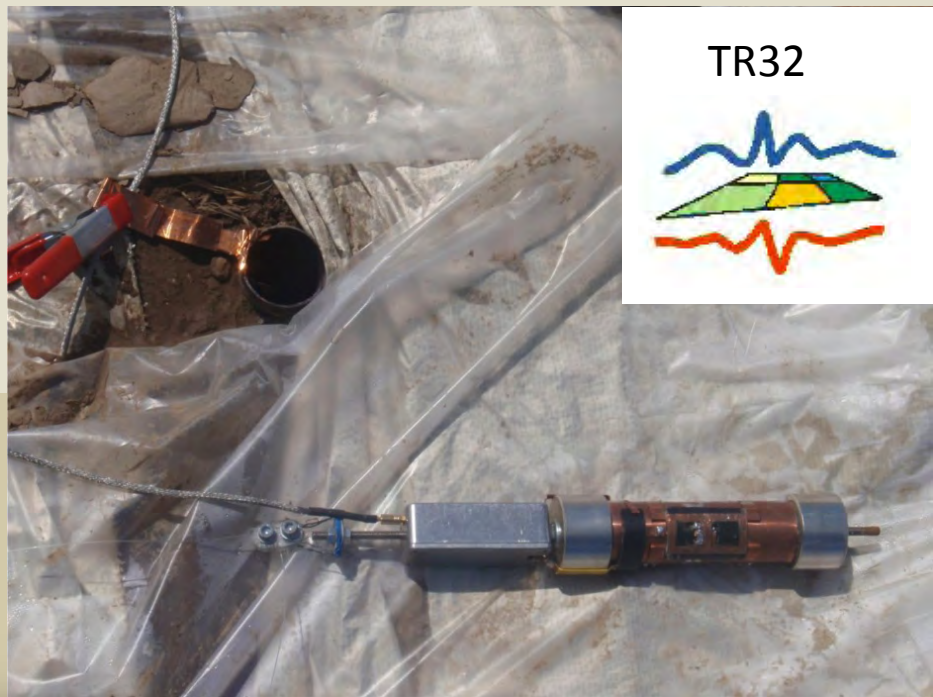


relaxation - exchange map

Stray-Field NMR

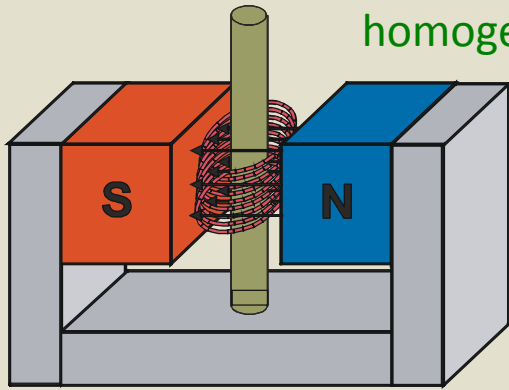


Slim-Line Tool for Soil Moisture Logging



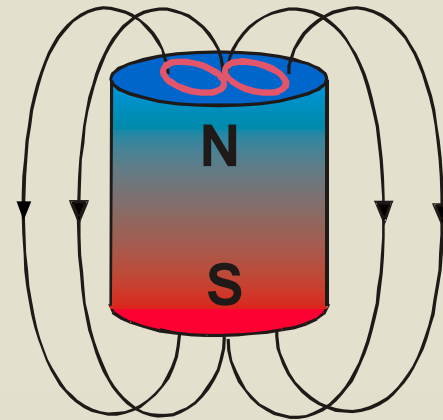
Magnets

homogeneous B_0



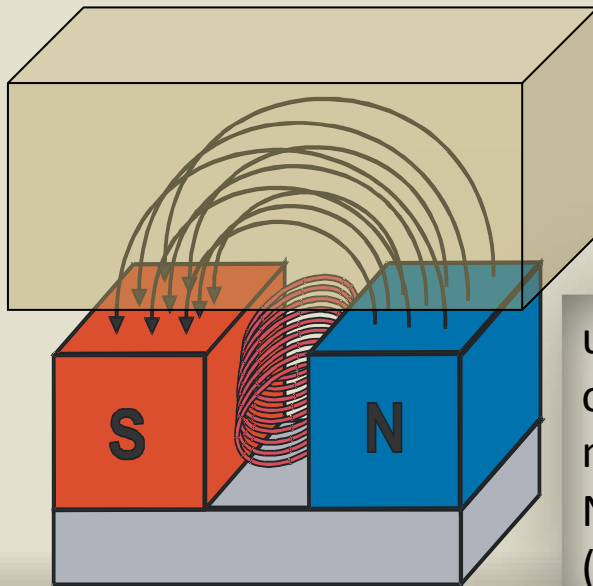
conventional
NMR (1945):
object inside
magnet

inhomogeneous B_0



the most simple
NMR-MOUSE
(2002)

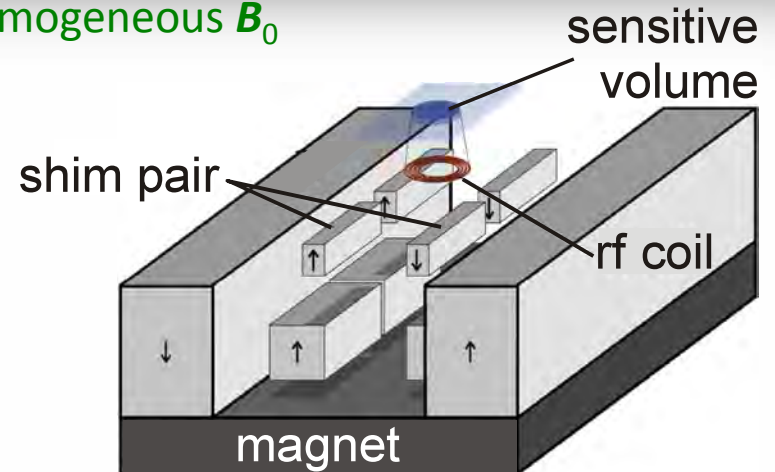
inhomogeneous B_0



well logging,
inside-out NMR
(1980)

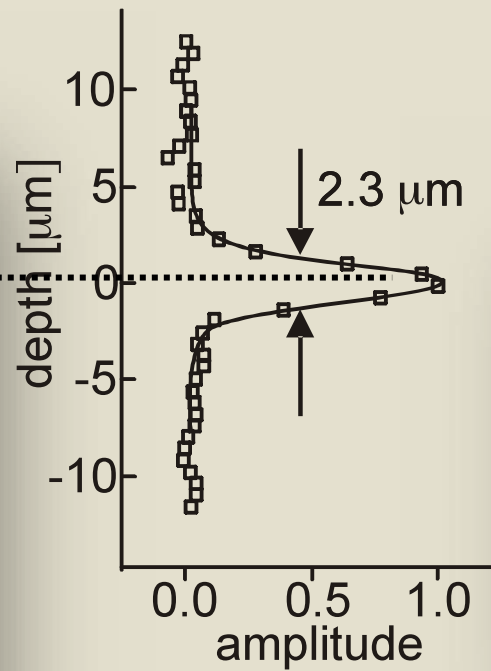
unilateral NMR:
object outside
magnet;
NMR-MOUSE
(1995)

homogeneous B_0

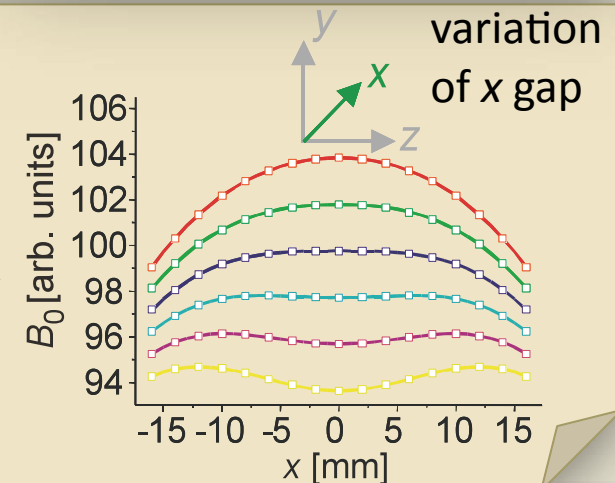
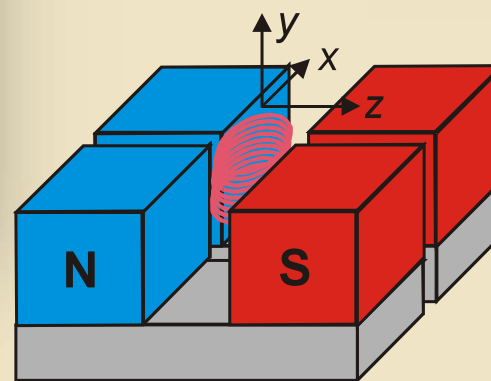


the most sophisticated NMR-MOUSE
(2007): shimming the stray field

The Profile NMR-MOUSE[®]

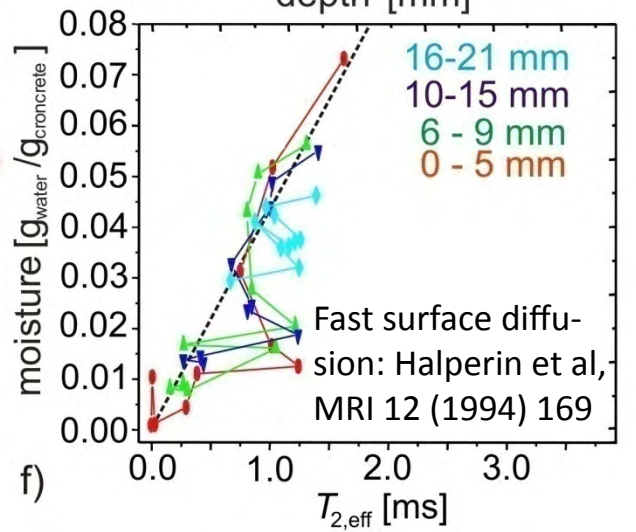
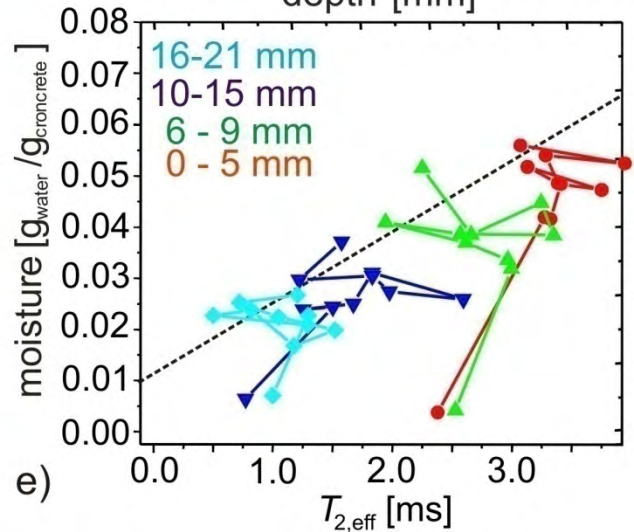
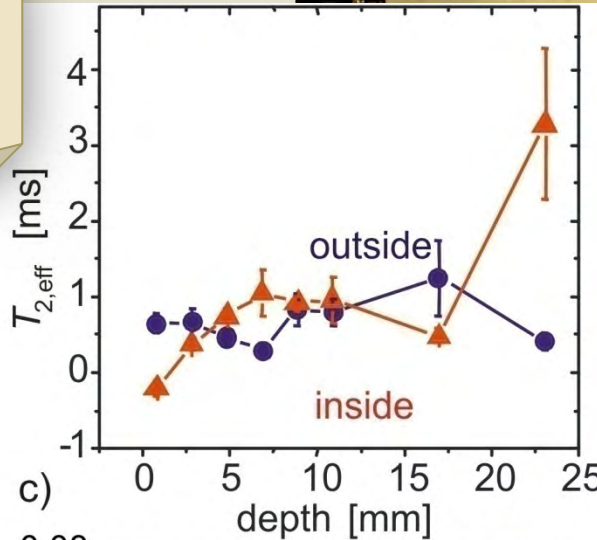
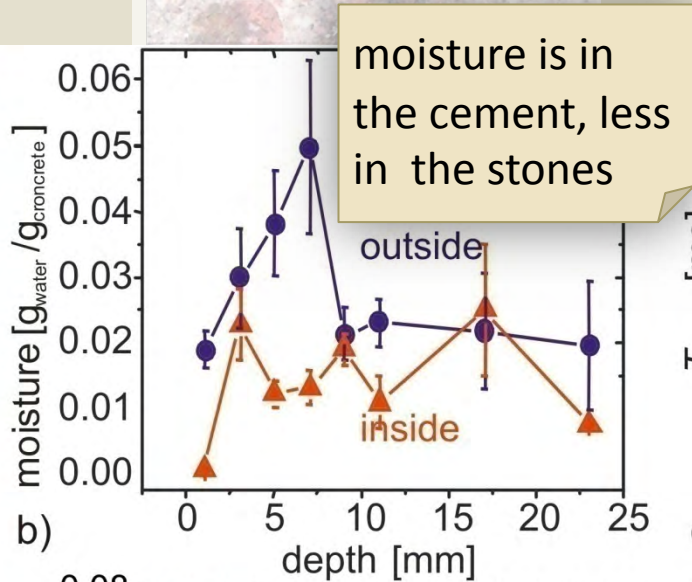
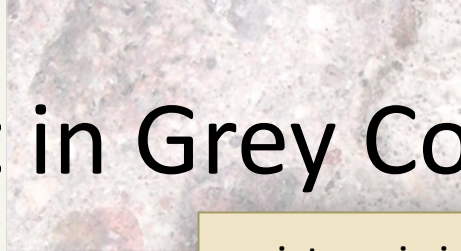


schematic drawing



J. Perlo, F. Casanova, B. Blümich, *Profiles with microscopic resolution by single-sided NMR*, *J. Magn. Reson.* **176** (2005) 64–70; B. Blümich, F. Casanova, J. Perlo, F. Presciutti, C. Anselmi, B. Doherty, *Noninvasive Testing of Art and Cultural Heritage by Mobile NMR*, *Acc. Chem. Res.* **6** (2010) 761 – 770

Moisture Content in Grey Concrete

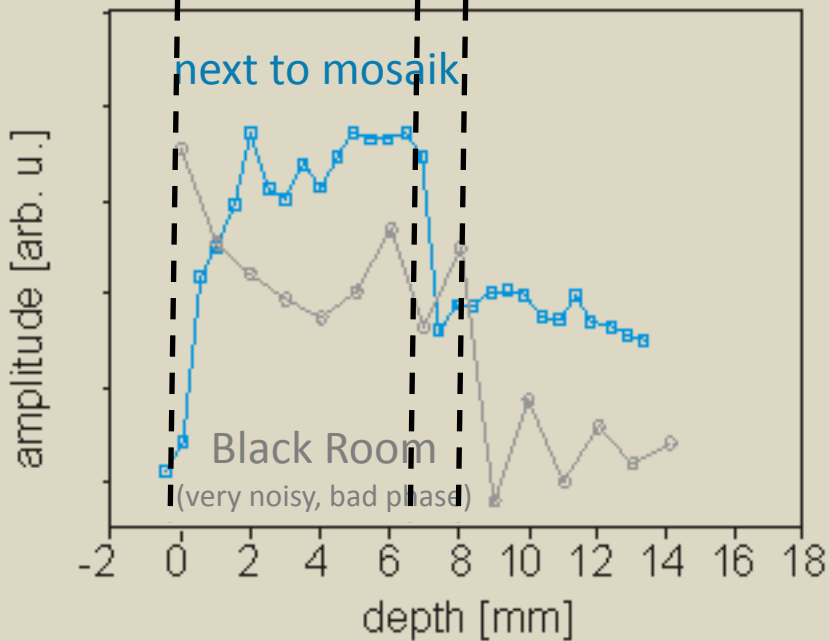
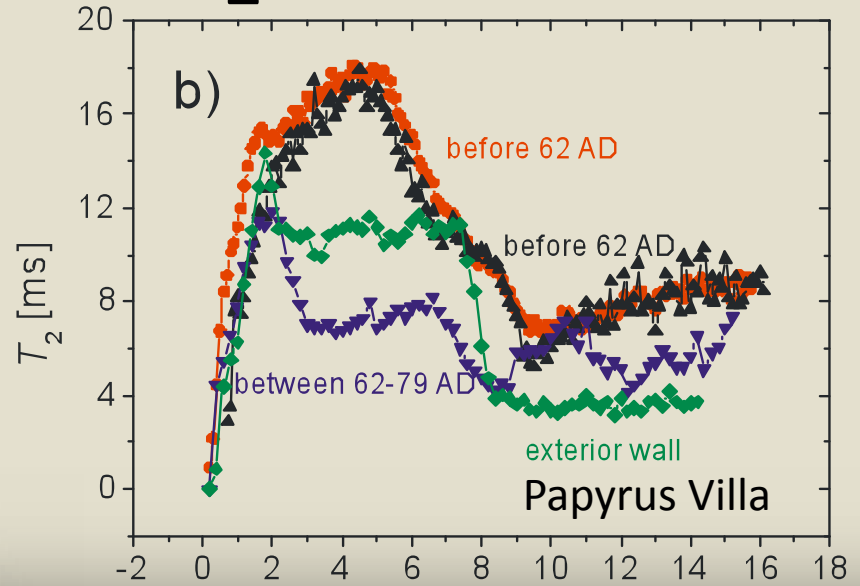
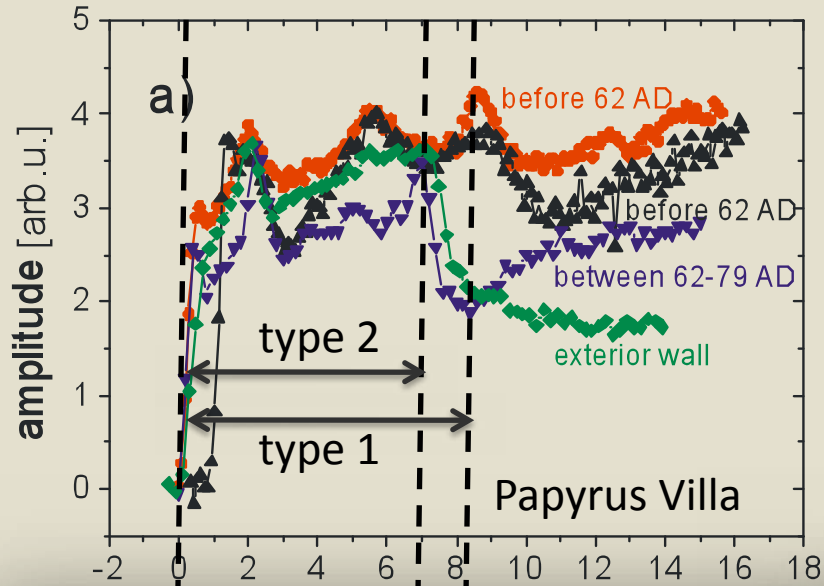


Papyrus Villa in Herculaneum

Earthquake: 62 AD
Eruption of Vesuvius: 79 AD



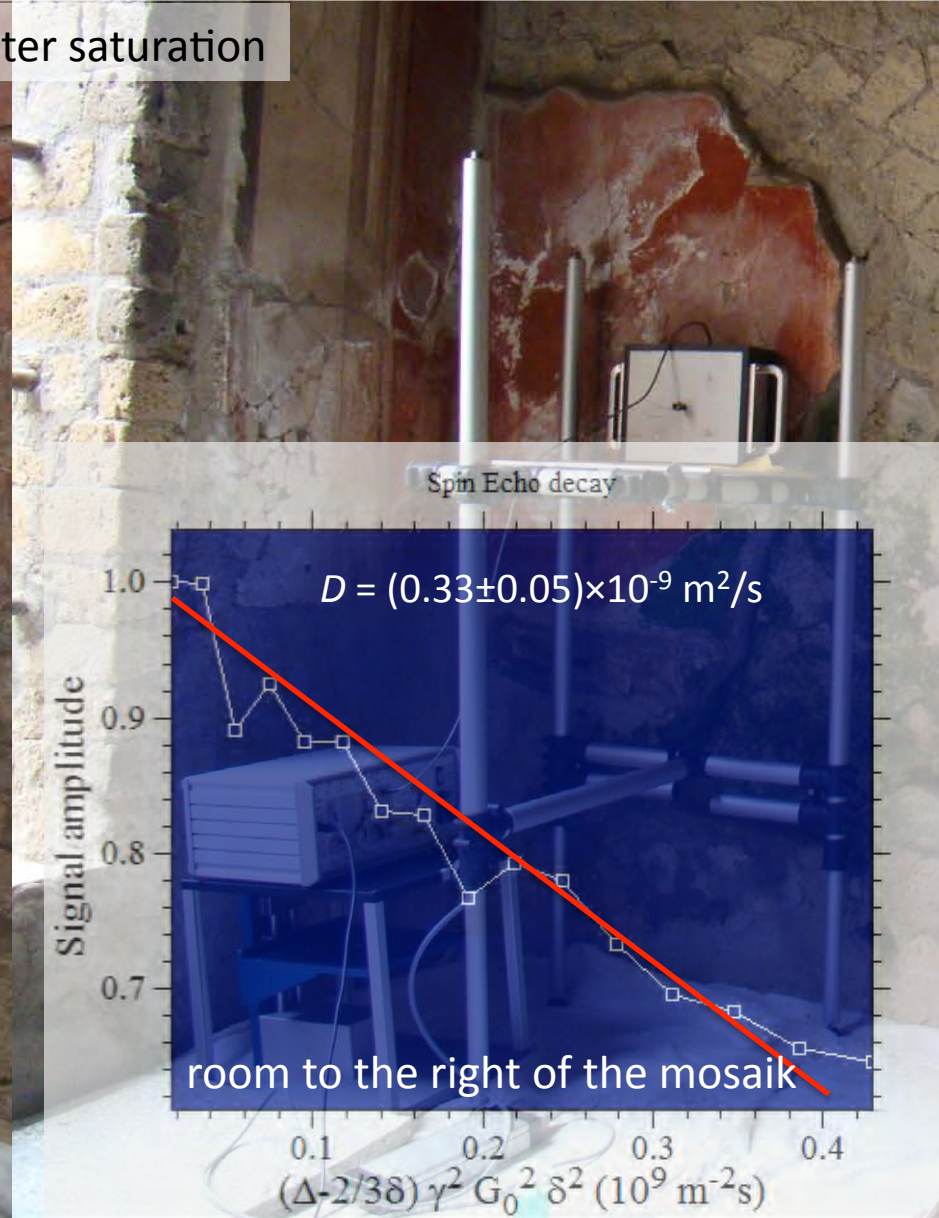
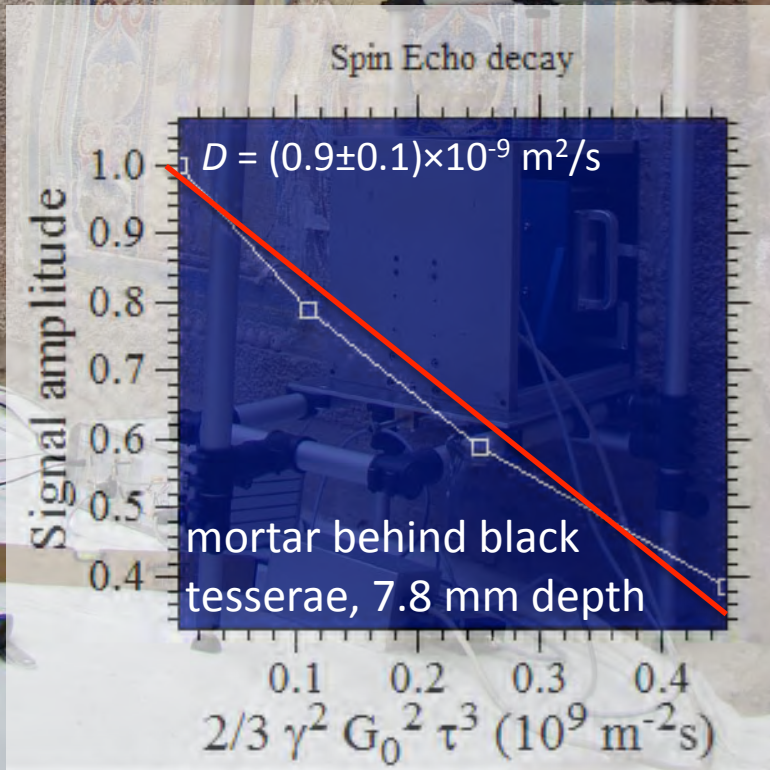
Amplitude and T_2 Profiles



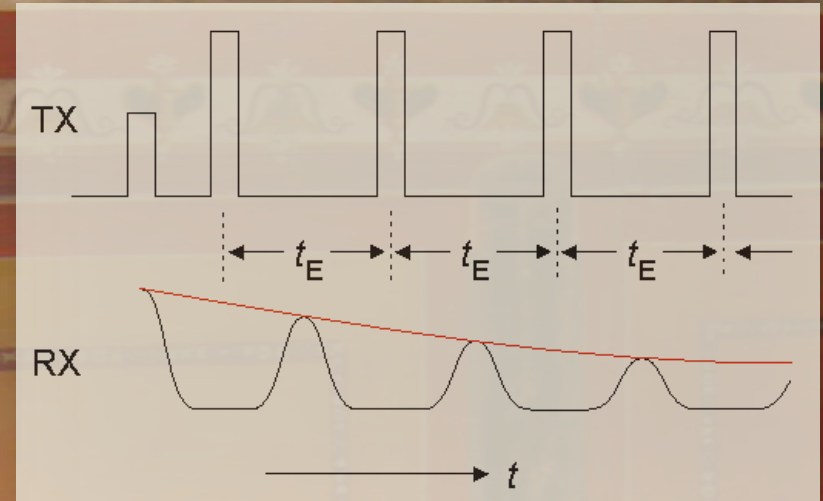
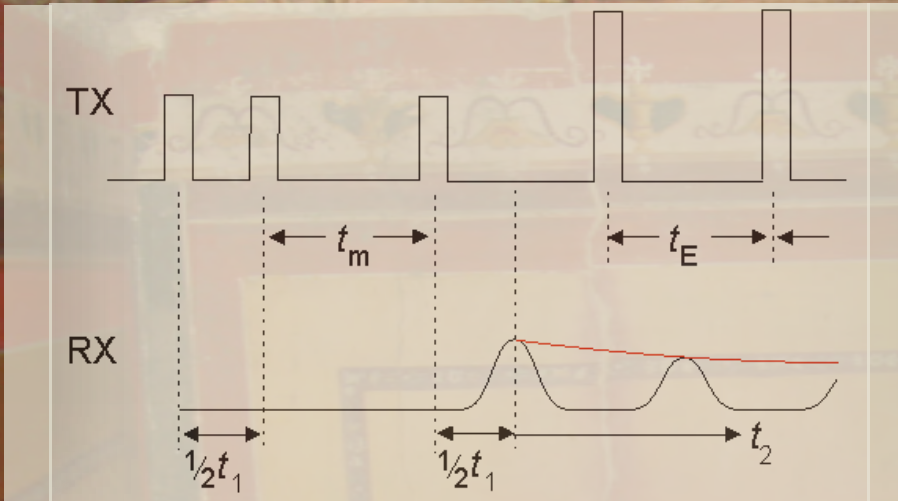
Marcus Vitruvius Pollio, De Architectura, L. VII, c. III 7, 33 – 20 A C: „ita com tribus coriis harenae et item marmoris solidati parietes fuerint, neque rimas neque aliud vitium in se recipere poterunt. sed et baculorum subactionibus fundata solidate marmorisque candore firmo levigata, coloribus cum politionibus inductis nitidos experiment splendores.“

In Situ Measurement of Diffusion

partial water saturation



Correlation of Relaxation and Diffusion

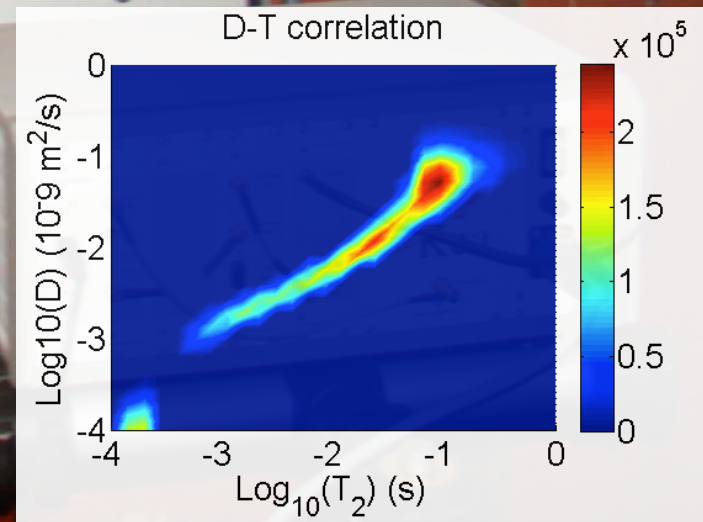


$$s(t_1, t_2) = s(0) \exp\left\{-\left(\frac{1}{T_{2,\text{bulk}}} + \rho_2 \frac{S}{V}\right) t_1 - \frac{D (\gamma G t_1)^2}{4} \left(t_m + \frac{1}{3} t_1\right)\right\}$$

$$\times \exp\left\{-\left(\frac{1}{T_{1,\text{bulk}}} + \rho_1 \frac{S}{V}\right) t_m\right\}$$

$$\times \exp\left\{-\left(\frac{1}{T_{2,\text{bulk}}} + \rho_2 \frac{S}{V} + \frac{D (\gamma G t_E)^2}{12}\right) t_2\right\}$$

$$s(t) = s(0) \exp\left\{-\underbrace{\left(\frac{1}{T_{2,\text{bulk}}} + \rho_2 \frac{S}{V}\right)}_{\propto t} + \underbrace{\frac{D (\gamma G t_E)^2}{12}}_{\propto t_E^2 t}\right\} t$$



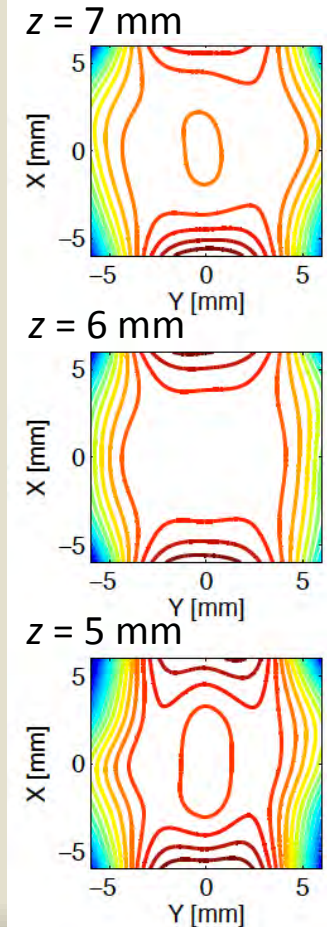
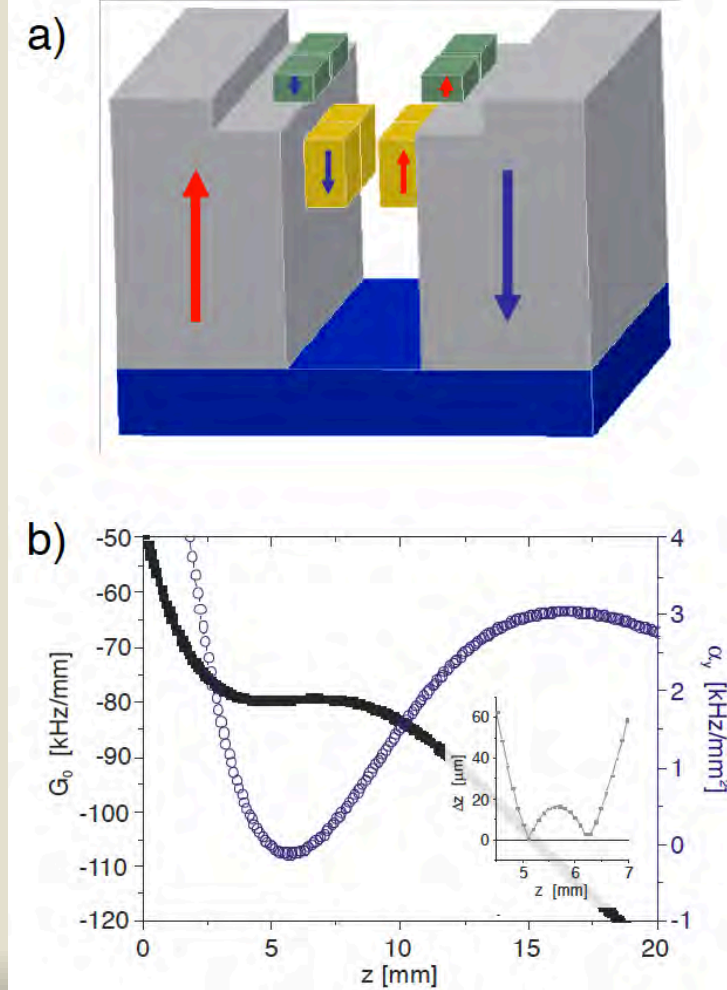
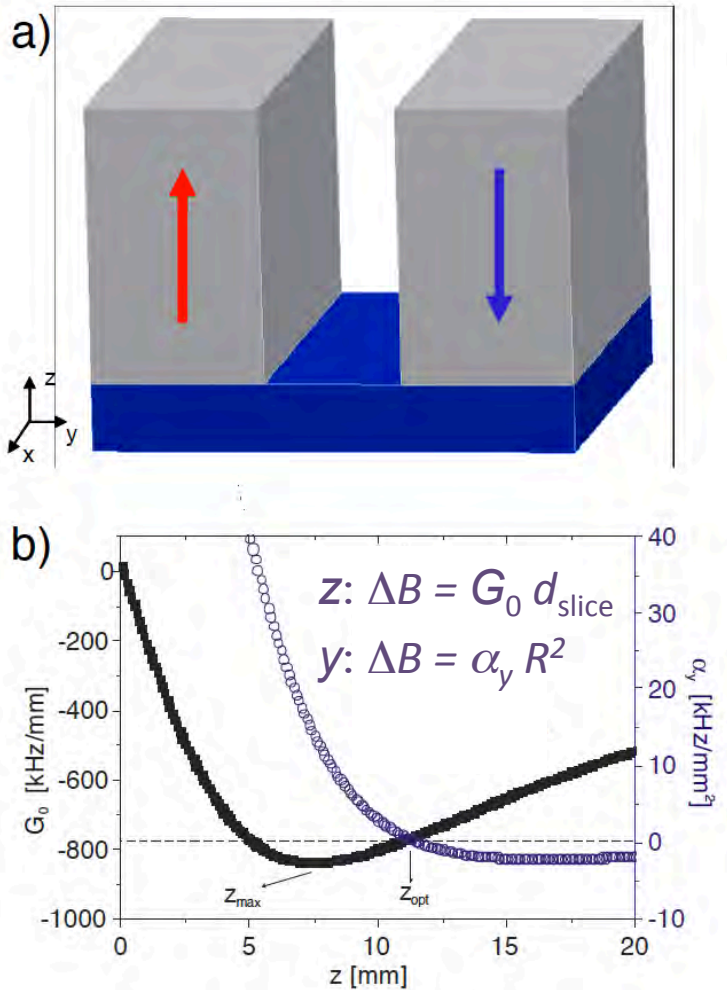
D.G. Rata, F. Casanova, J. Perlo, D.E. Demco, B. Blümich, Self-diffusion measurement by a mobile single-sided NMR sensor with improved magnetic field gradient, J. Magn. Reson. 180 (2006) 229 – 235

The Fourier NMR-MOUSE

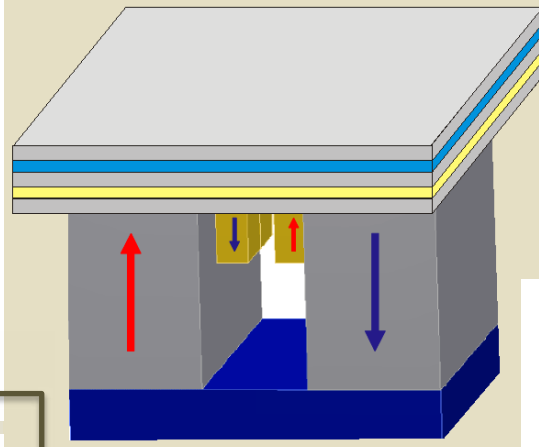
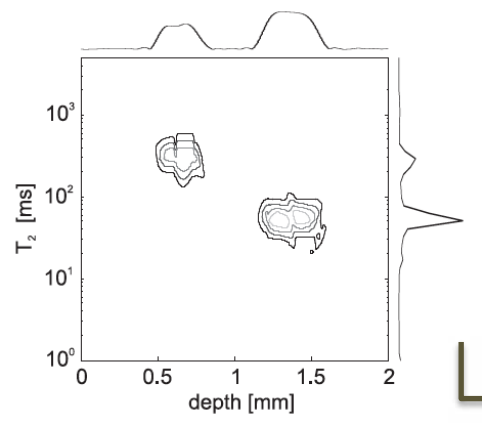
U-shaped NMR-MOUSE

Fourier NMR-MOUSE

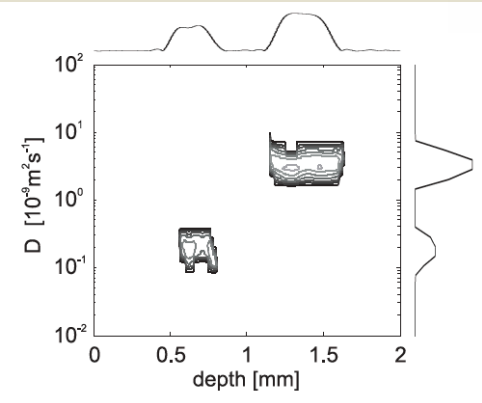
Measured field maps



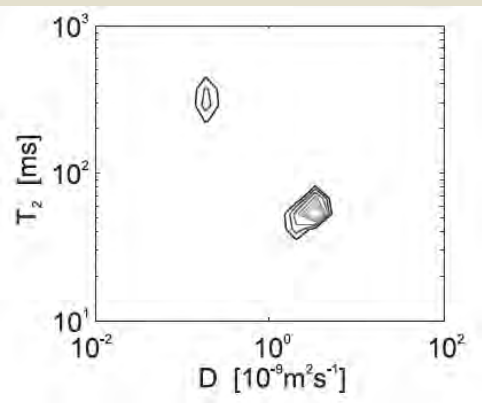
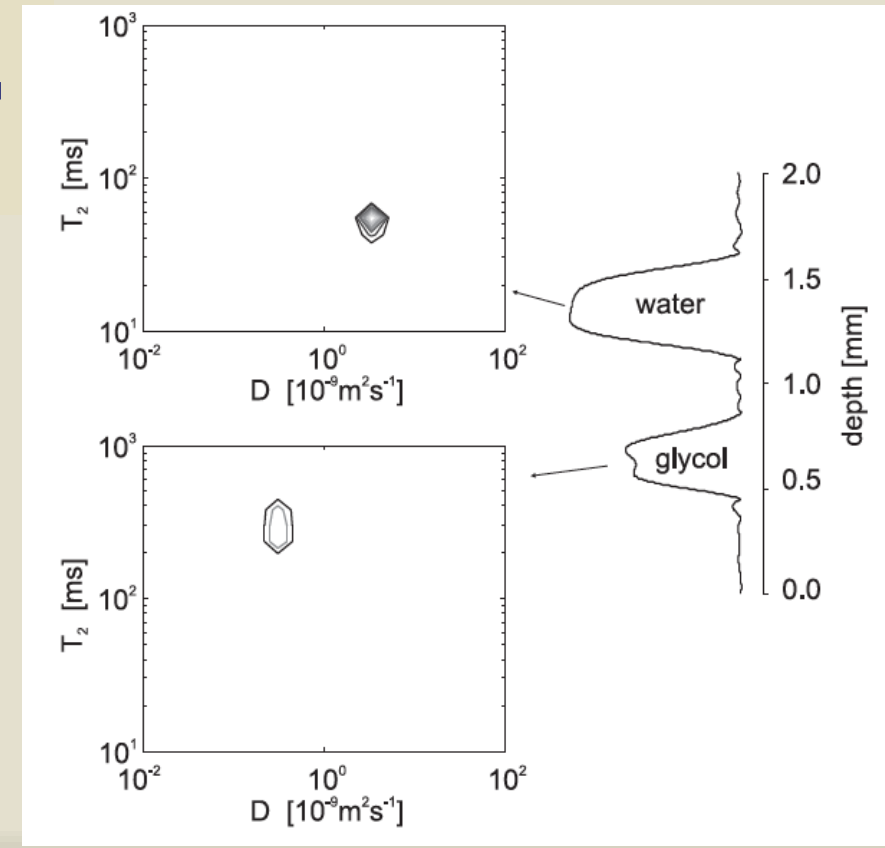
2D / 3D Distributions from Bilayer Phantom



Glass
Water
Glass
Glycol



$T_{acq} = 17 \text{ min}$



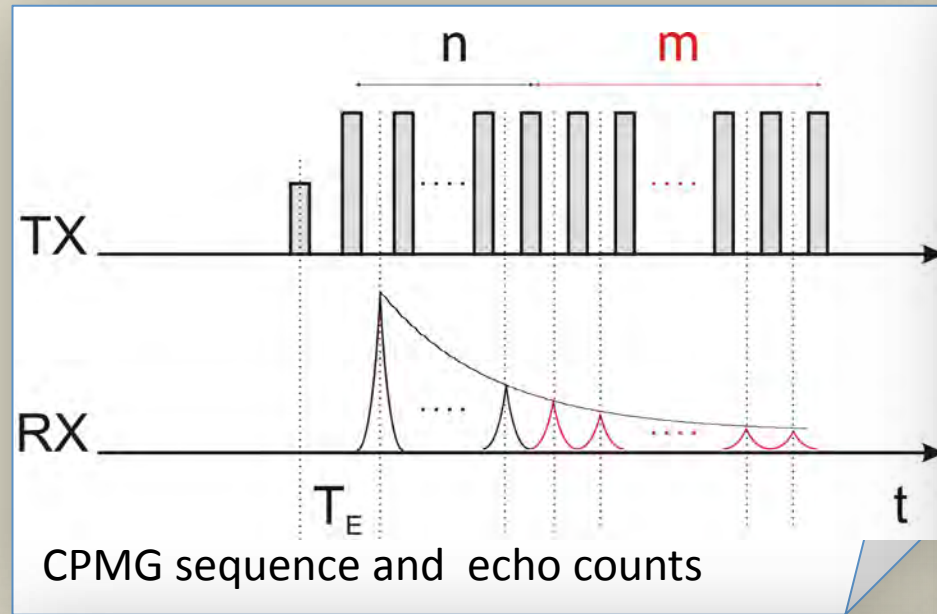
$T_{acq} = 12 \text{ min}$

$T_{acq} = 7 \text{ h}$

$T_{acq} = 25 \text{ min}$

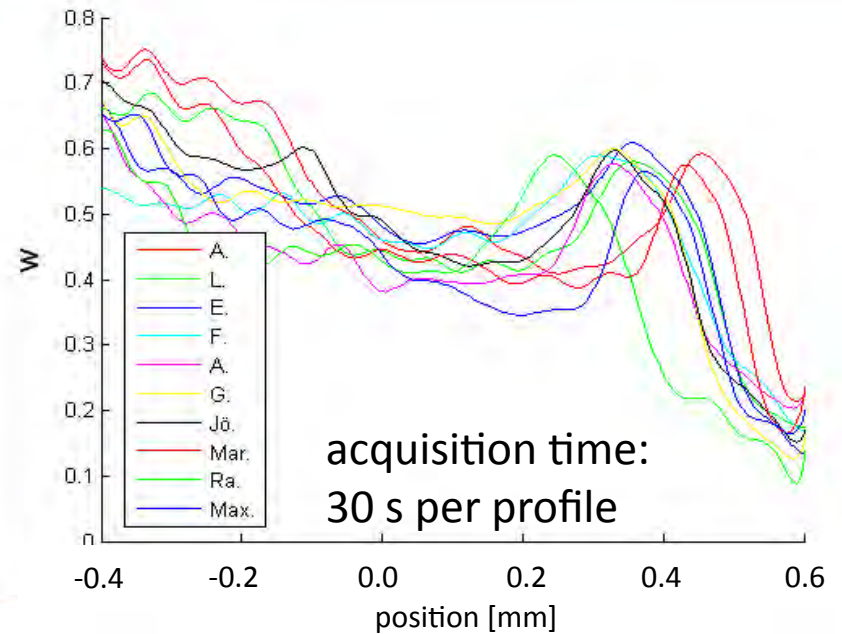
M. Van Landeghem, E. Danieli, J. Perlo, B. Blümich, F. Casanova, Single-sided NMR sensor for depth profiling human skin tissue, manuscript in preparation

1D Profiles of the Palm of the Hand



$$W = \frac{\sum_{m=m_i}^{m_f} s(m T_E)}{\sum_{n=n_i}^{n_f} s(n T_E)}$$

Definition of relaxation weighed amplitudes w

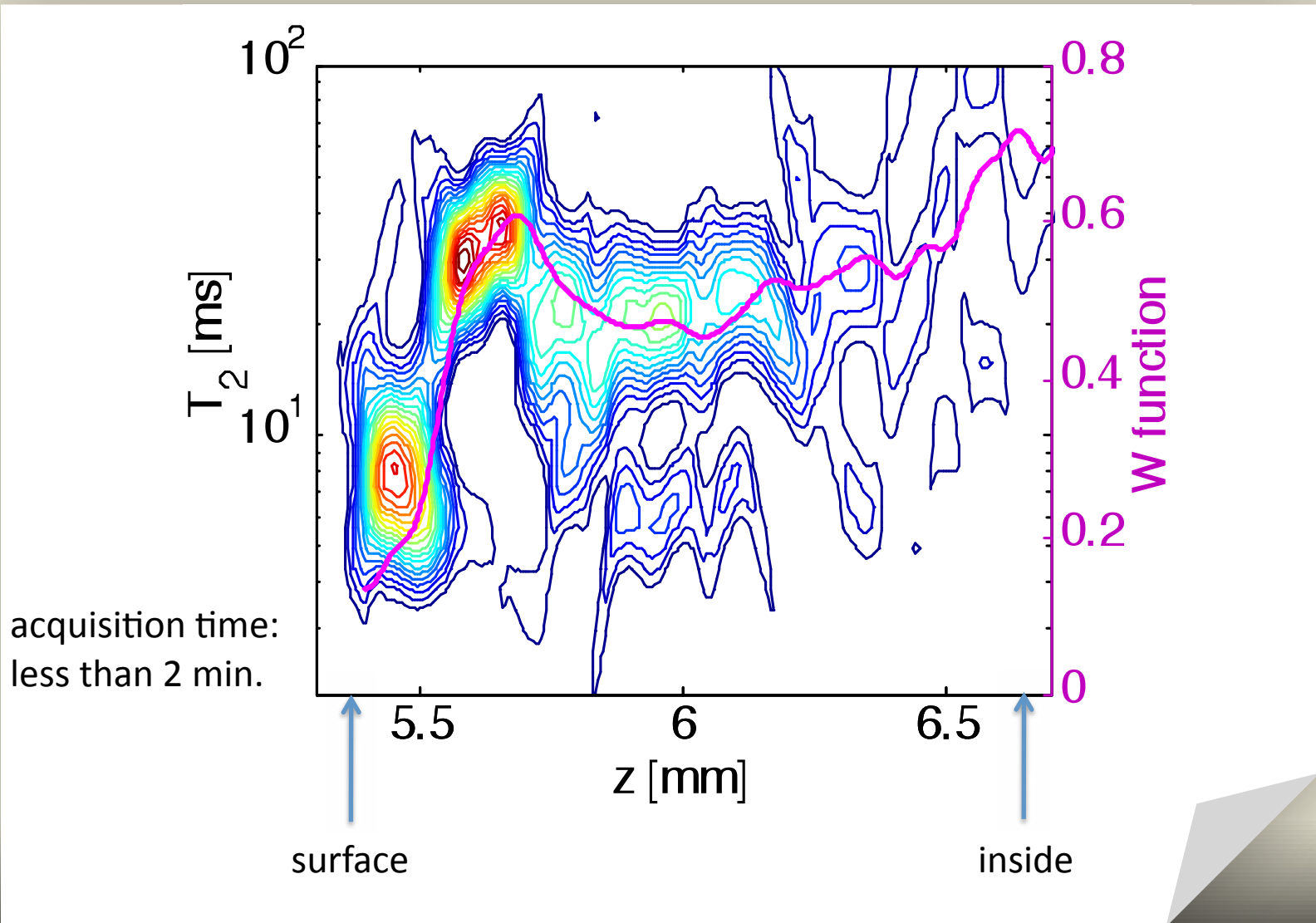


↑
inside

↑
surface

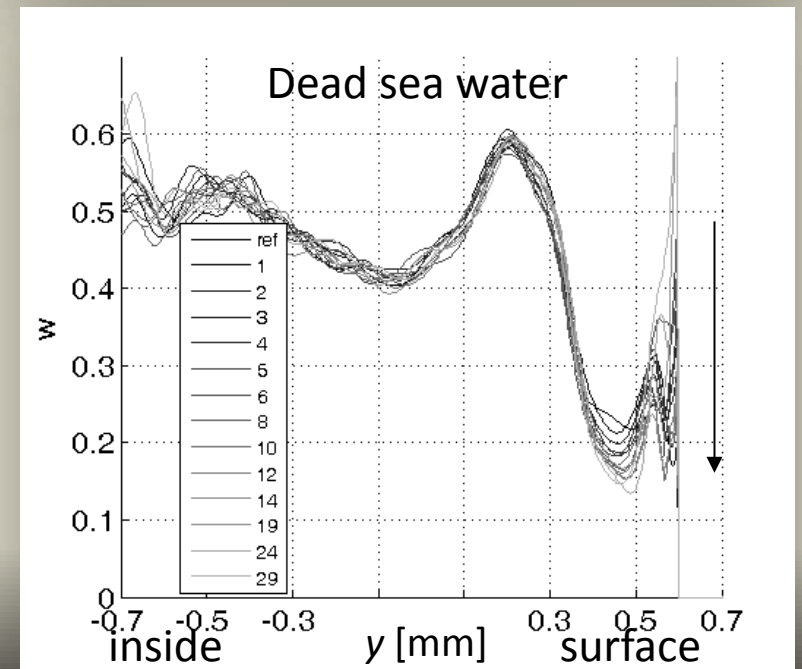
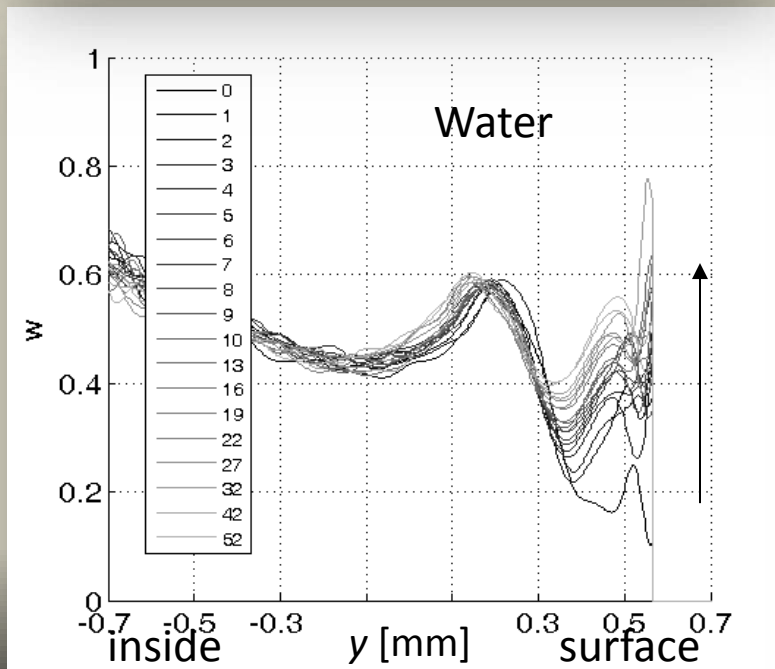
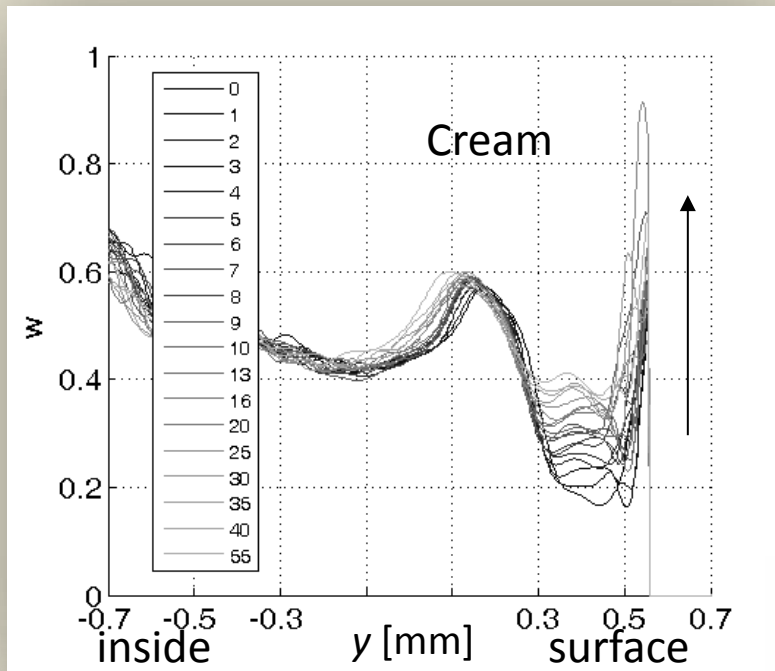
Different individuals have different skin profiles

Depth-Resolved T_2 distributions versus the w function

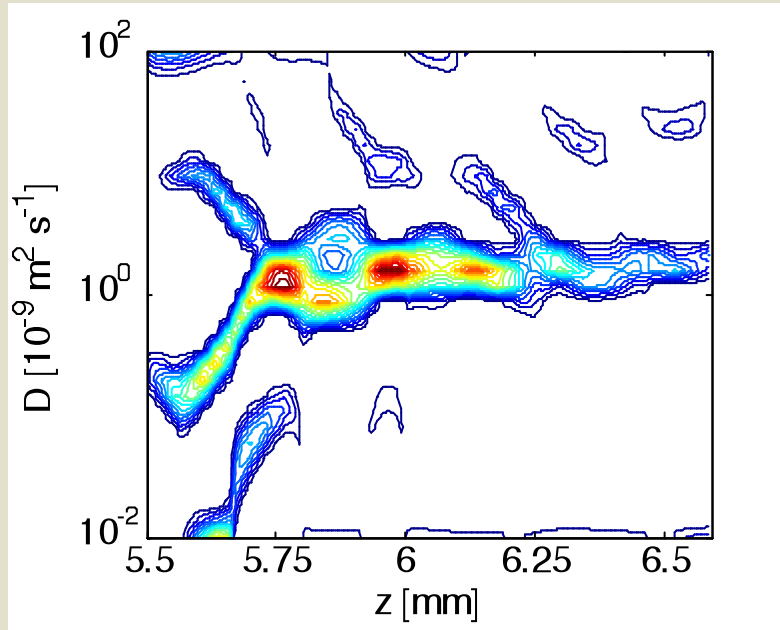


Functional Analysis of The Skin With the Fourier NMR-MOUSE

- Gradient 10 times smaller: 80 kHz/mm
- Single-shot profiles across 1 mm depth
- 30 s acquisition time per profile



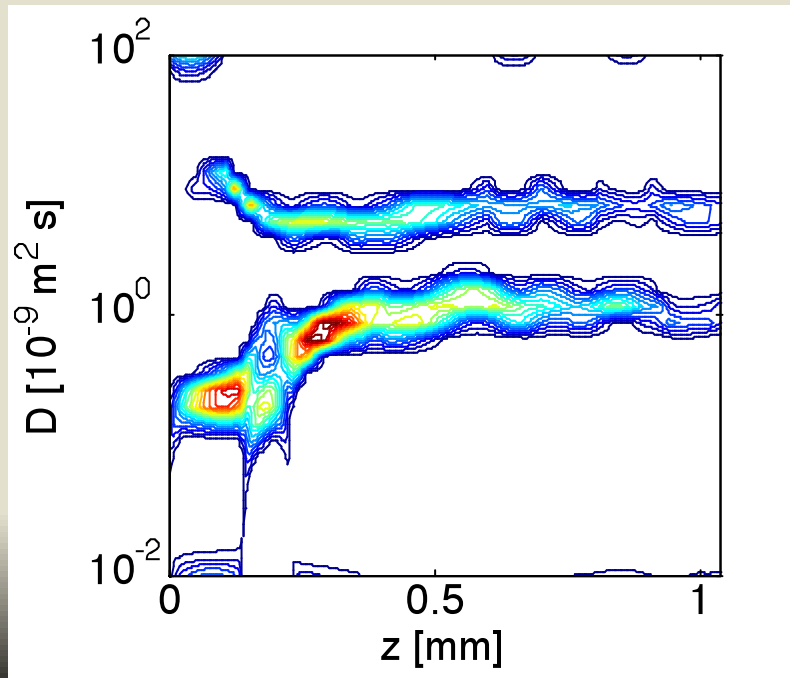
Reference



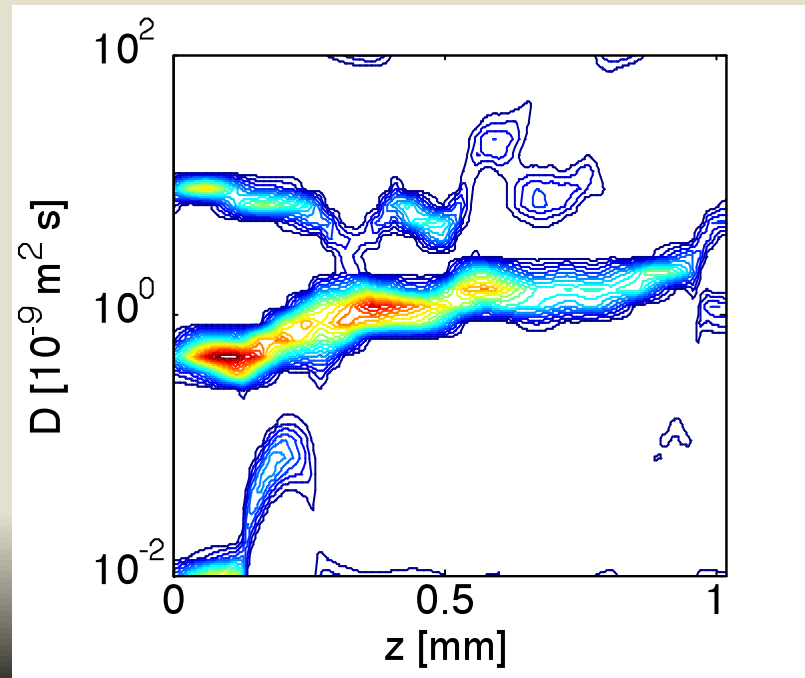
D Distributions Versus Depth

acquisition time:
less than 10 min.

Saturated with cream

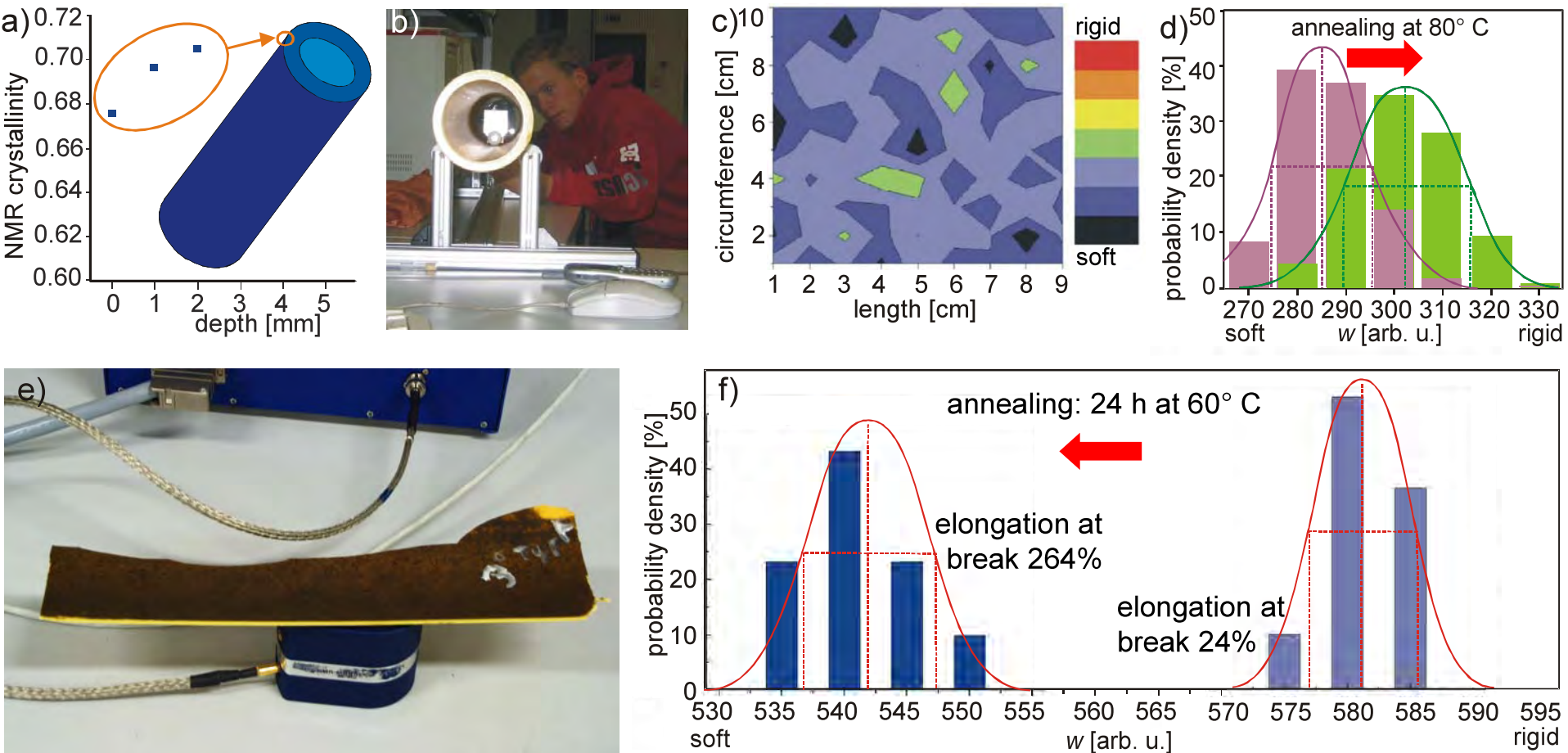


Saturated with water



Aging and Annealing of PE

PE100 pipes



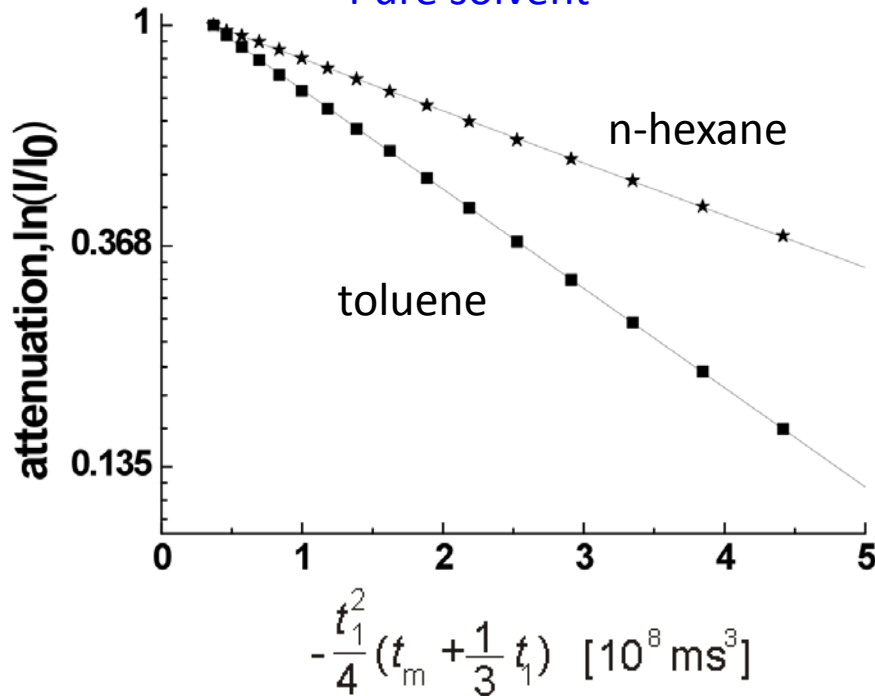
LDPE steel pipe shell, 20 – 30 years in the ground

Self-Diffusion of Solvents in PE Samples

Rance
Kwamen



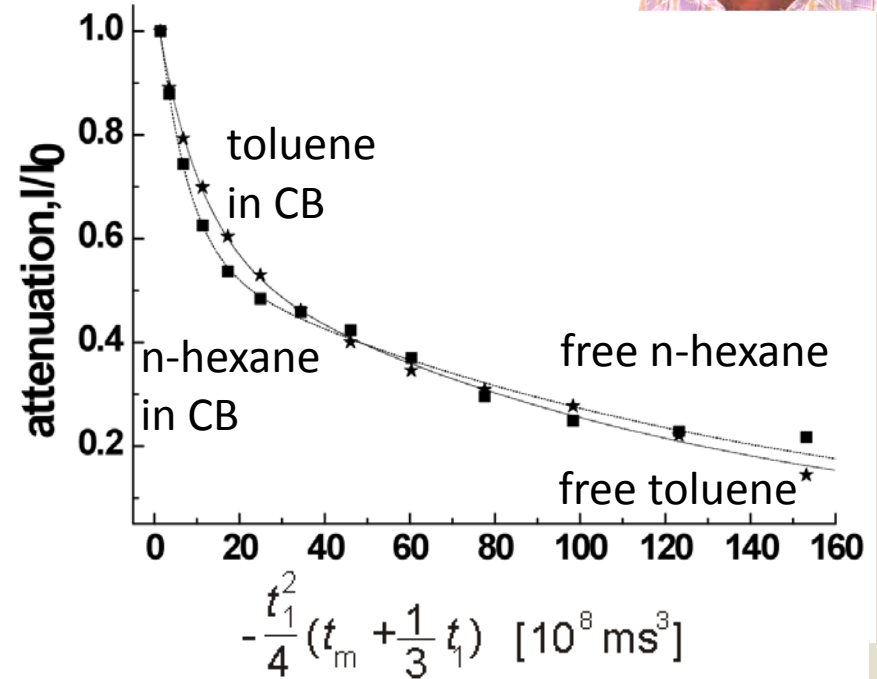
Pure solvent



$$D_0(\text{n-hexane}) = 4.5 \times 10^{-9} \text{ m}^2/\text{s}$$

$$D_0(\text{toluene}) = 2.37 \times 10^{-9} \text{ m}^2/\text{s}$$

Solvent in PE

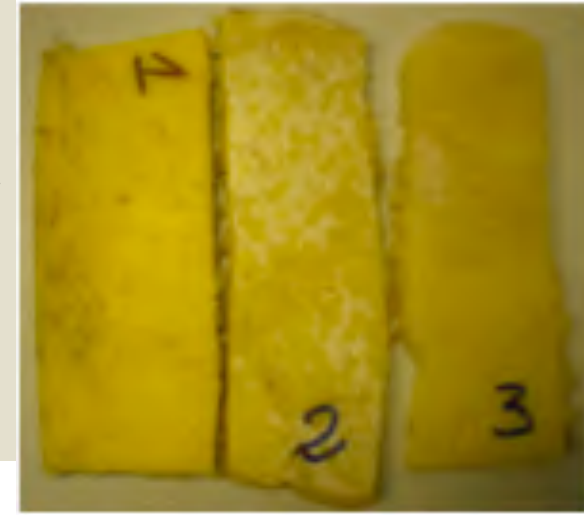
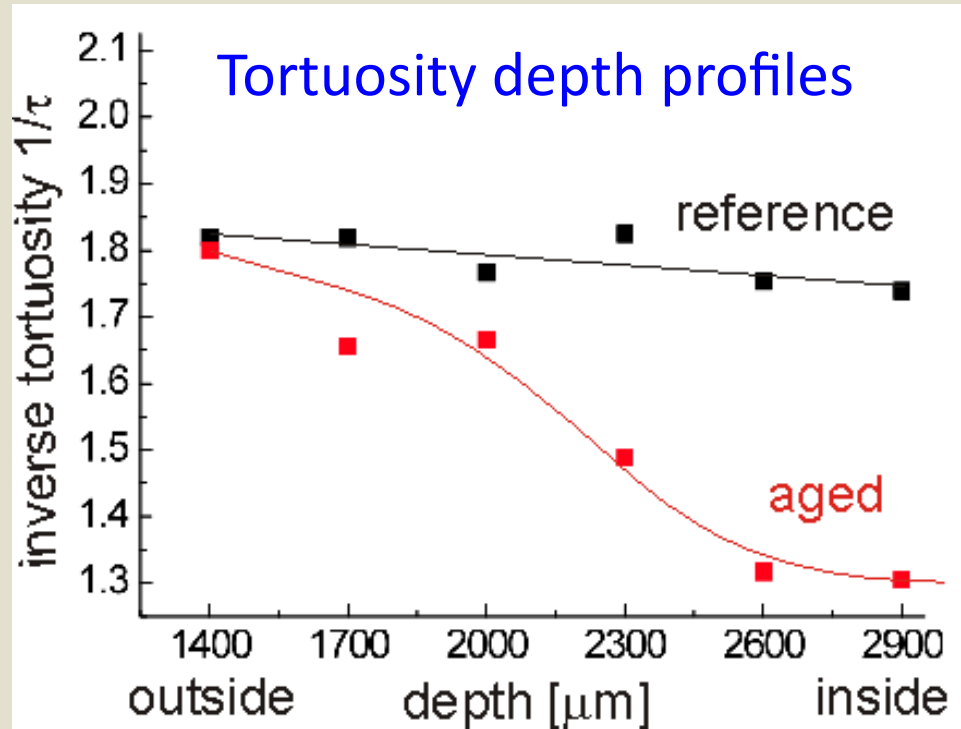


$$D_0(\text{hexane/CB}) = 7.35 \times 10^{-11} \text{ m}^2/\text{s}$$

$$D_0(\text{toluene/CB}) = 8.5 \times 10^{-11} \text{ m}^2/\text{s}$$

Stimulated echo for measurements of diffusion by unilateral NMR

Aged PE Pipes: Solvent Diffusion and Relaxation

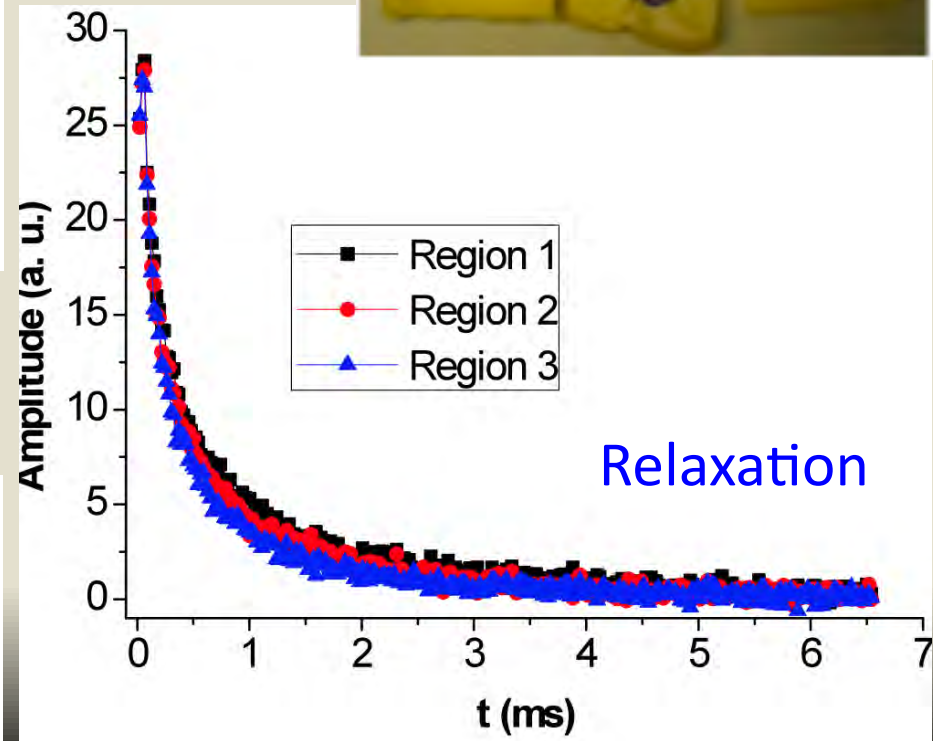


low crystallinity
large elongation at break

high crystallinity
low elongation at break

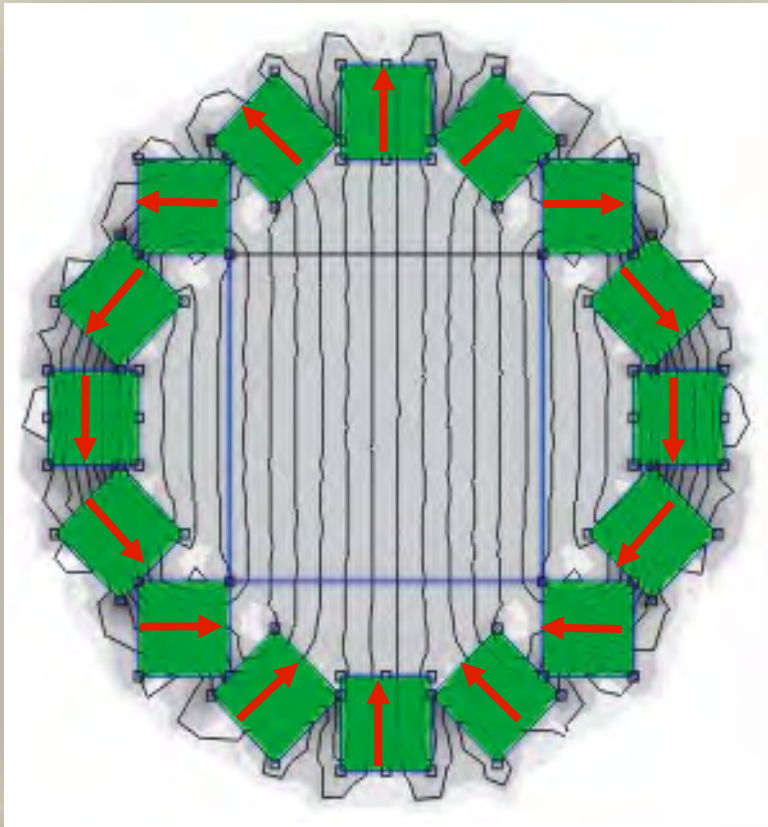
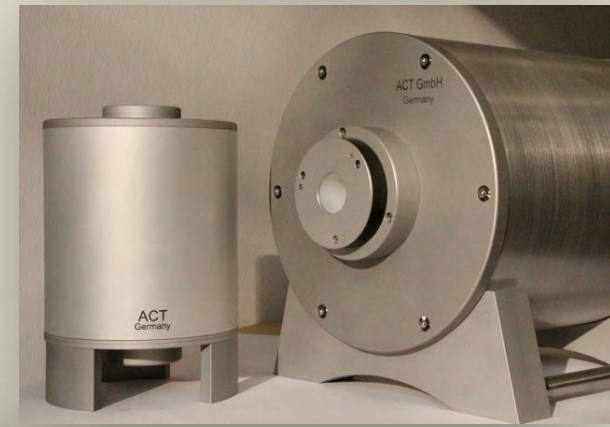


The solvent molecules diffuse in the amorphous regions



Halbach Magnets

$n = 16$



Klaus Halbach,
1925 - 2000

K. Halbach, *Design of permanent multipole magnets with oriented rare earth cobalt material*, *Nucl. Instrum. Methods* **169** (1980) 1–10; H. Raich and P. Blümler, *Design and construction of a dipolar Halbach array with a homogeneous field from identical bar magnets: NMR Mandhalas*, *Concepts Magn. Reson.* **B23** (2004) 16-25

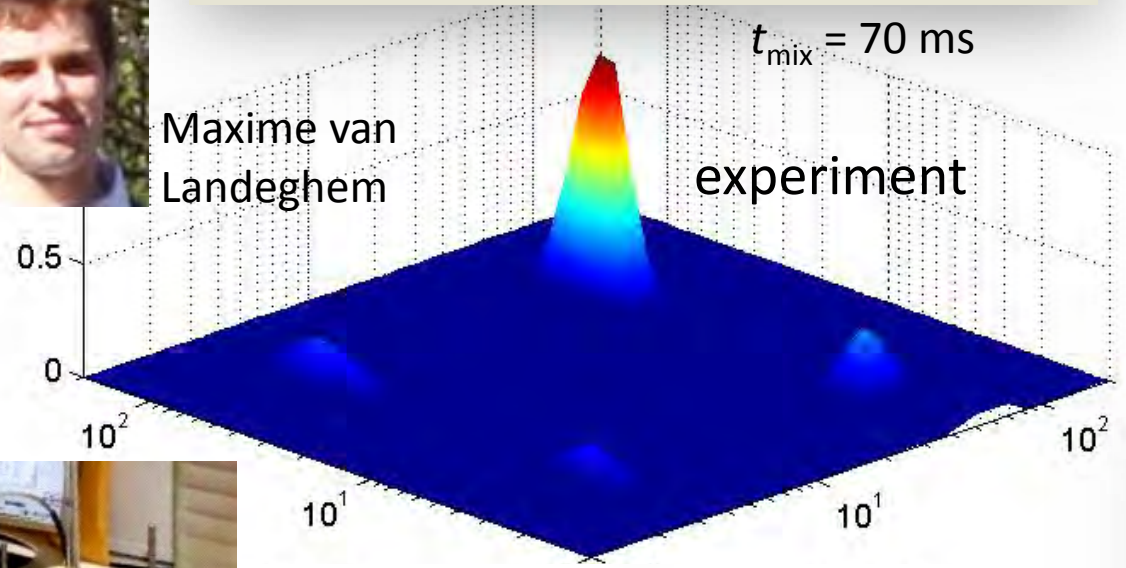


Pulse sequence: CPMG(t_1) - t_{mix} - CPMG(t_2)

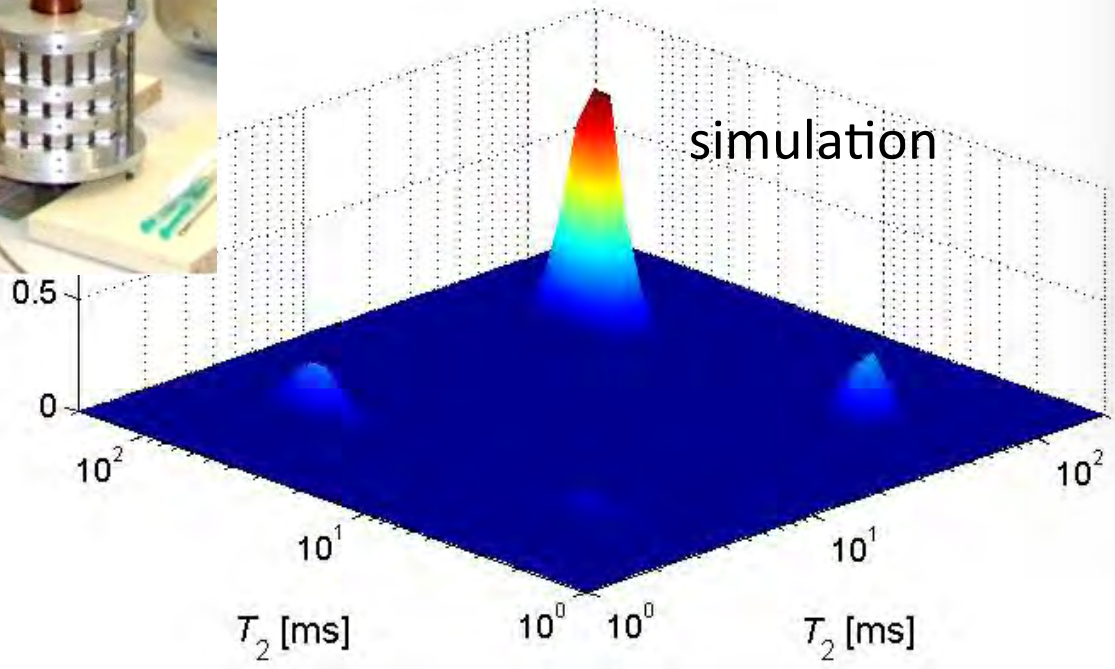
$t_{\text{mix}} = 70 \text{ ms}$

Maxime van Landeghem

experiment



simulation



2D Exchange NMR of Water in Silica Particles

Fit results

Parameter	Value
M^A	5.5
M^B	18.4
T_2^A	3.9 ms
T_2^B	103.5 ms
T_1^A	610.0 ms
T_1^B	630.0 ms
k	1/(110 ms)

M. Van Landeghem, A. Haber, J.-B. d'Espinose de Lacaillerie, B. Blümich, *Analysis of Multi-Site 2D Relaxation-Exchange NMR*, **Concepts Magn. Reson. 36A (2010)** 153-169

n -site exchange: $M(t) - M_0 = \exp\{-(R+K)(t - t_0)\} [M(t_0) - M_0]$

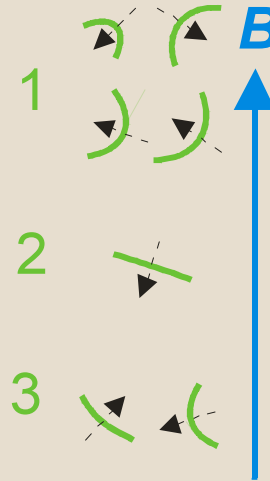
Distance Constraints from Exchange Rates

a working hypothesis

molecular diffusion in a fluid-filled pore



curvatures define relaxation times ??



distances between relaxation centers from exchange rates

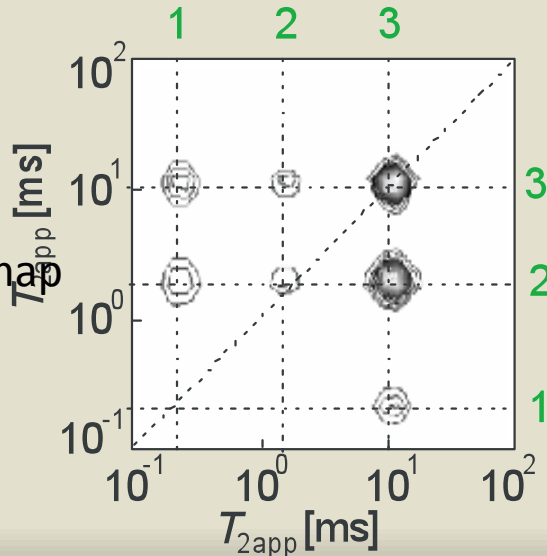
$$(\Delta R)^2 = 6 D t_D$$

$$k_{12}^{-1} = 400 \text{ ms} = (\Delta R_{12})^2 / 6 D_{\text{H}_2\text{O}}$$

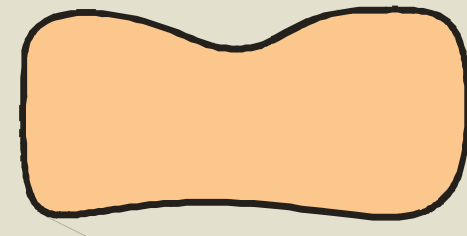
$$k_{13}^{-1} = 20 \text{ ms} = (\Delta R_{13})^2 / 6 D_{\text{H}_2\text{O}}$$

$$k_{23}^{-1} = 3000 \text{ ms} = (\Delta R_{23})^2 / 6 D_{\text{H}_2\text{O}}$$

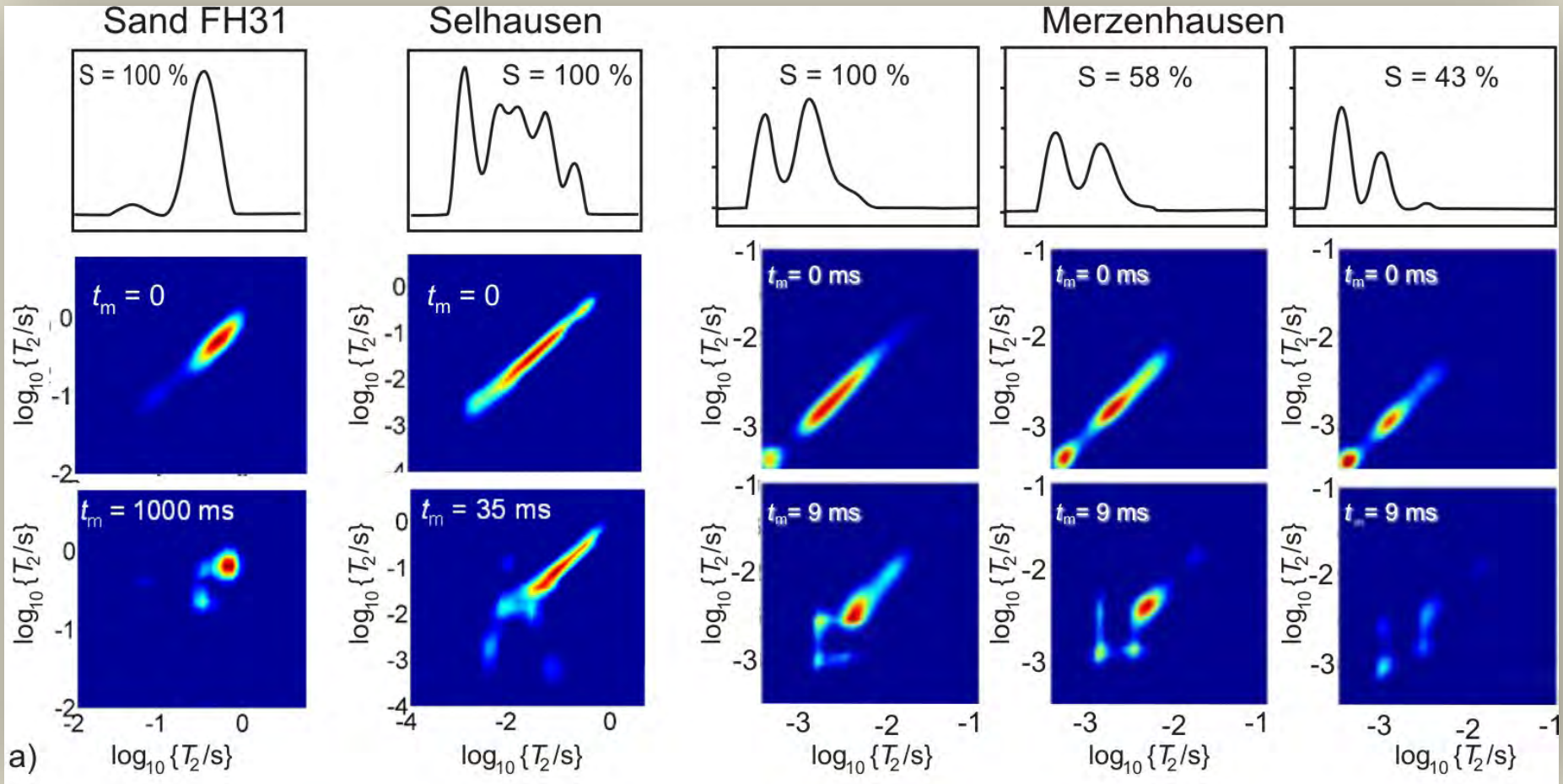
simulated relaxation exchange map



model of average pore to study drying processes



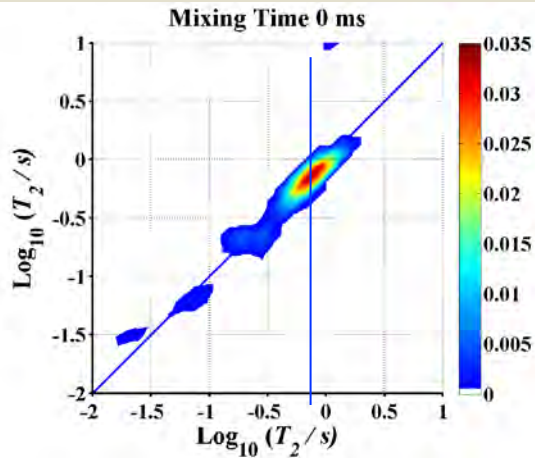
T_2 Distributions of Sand and Soil



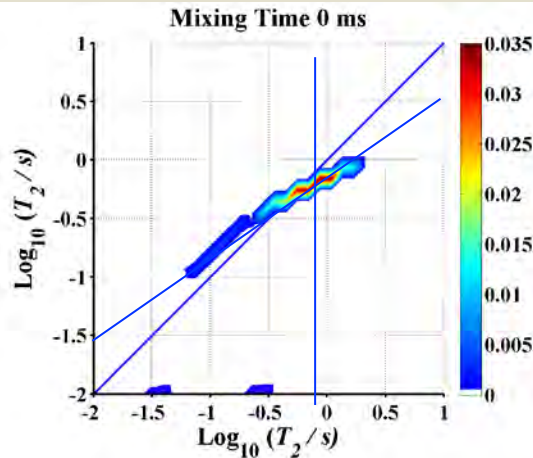


TR32

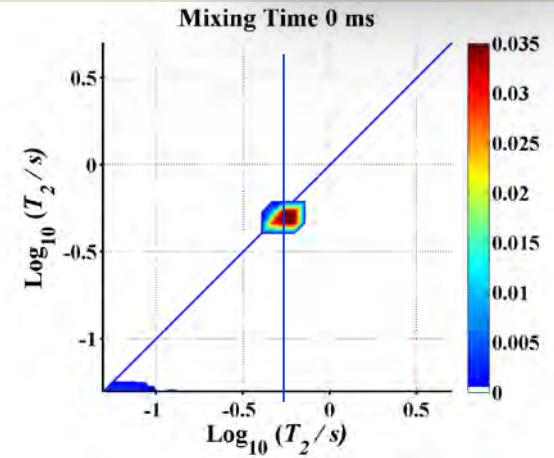
T_2 Exchange NMR of Diffusion and Advection



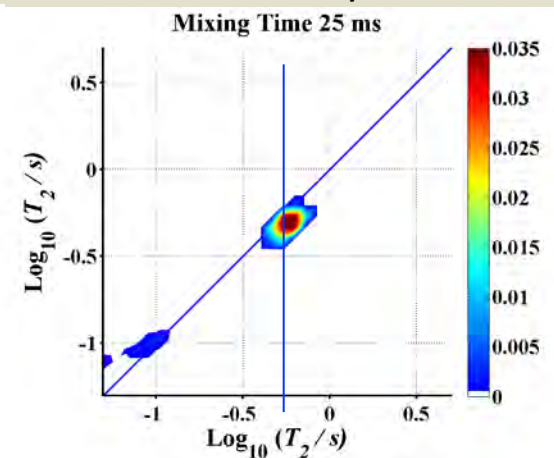
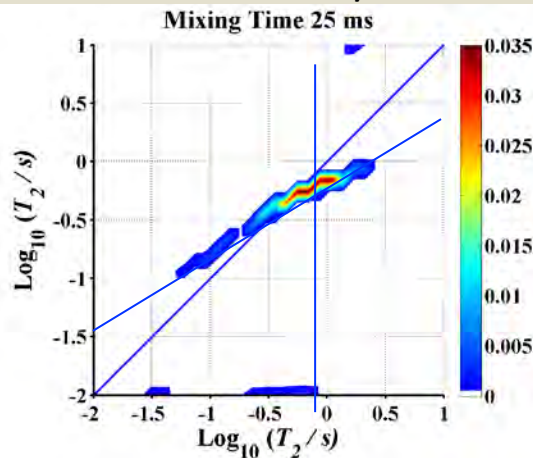
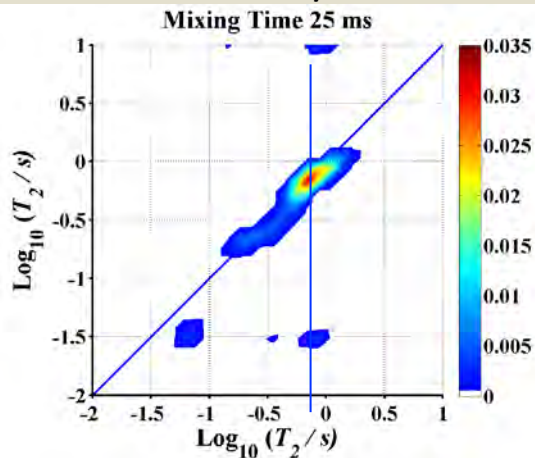
$v = 0$ ml/h



$v = 1.6$ ml/h



$v = 39$ ml/h



Modelling Diffusion and Advection

Julia Kowalski

Bloch-Torrey equation: Diffusion and Advection

$$\frac{\partial}{\partial t} \mathbf{M} = \underbrace{\gamma \mathbf{M} \times \mathbf{B}}_{\text{precession}} + \underbrace{\mathbf{R} (\mathbf{M} - \mathbf{M}_0)}_{\text{relaxation}} + \underbrace{\nabla \cdot \mathbf{D} \nabla \mathbf{M}}_{\text{self-diffusion}} - \underbrace{\nabla \cdot \mathbf{v} \mathbf{M}}_{\text{advection}}$$

Introduction of dimensionless parameters

$$\mathbf{t} = T_2^c \tilde{\mathbf{t}} \quad \mathbf{x} = L \tilde{\mathbf{x}} \quad \mathbf{y} = L \tilde{\mathbf{y}} \quad \mathbf{z} = L \tilde{\mathbf{z}} \quad \mathbf{M} = M_0 \tilde{\mathbf{M}}$$

$$\frac{\partial}{\partial \tilde{\mathbf{t}}} \tilde{\mathbf{M}} = \mathbf{R} (\tilde{\mathbf{M}} - \mathbf{e}_z) + N_d \Delta \tilde{\mathbf{M}} - N_v \mathbf{e}_v \nabla \tilde{\mathbf{M}}$$

Typical experimental parameters

Diffusion number Advection number

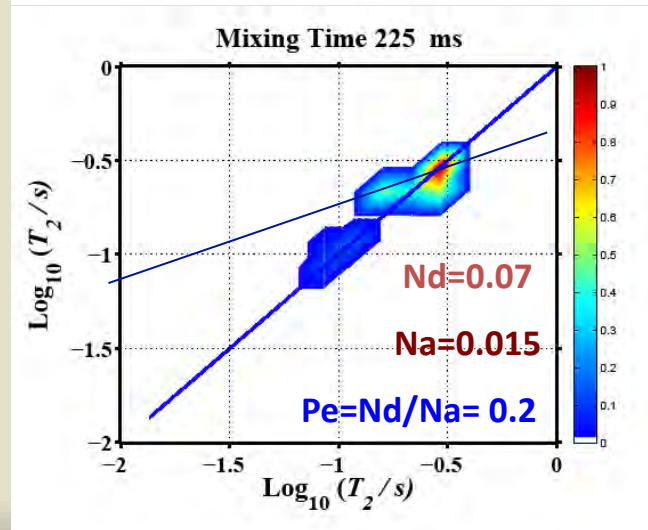
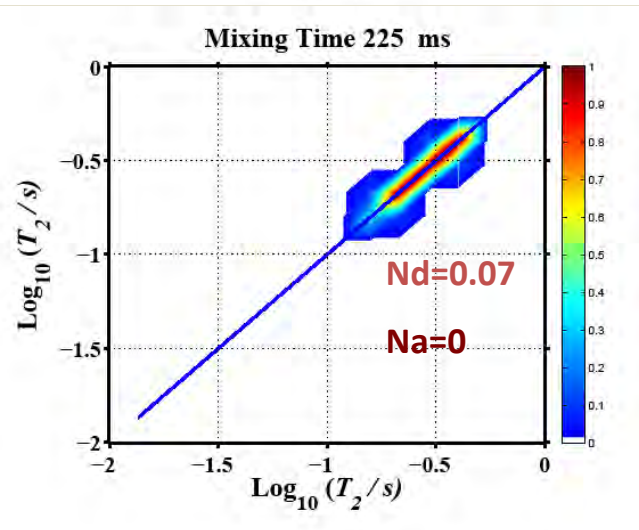
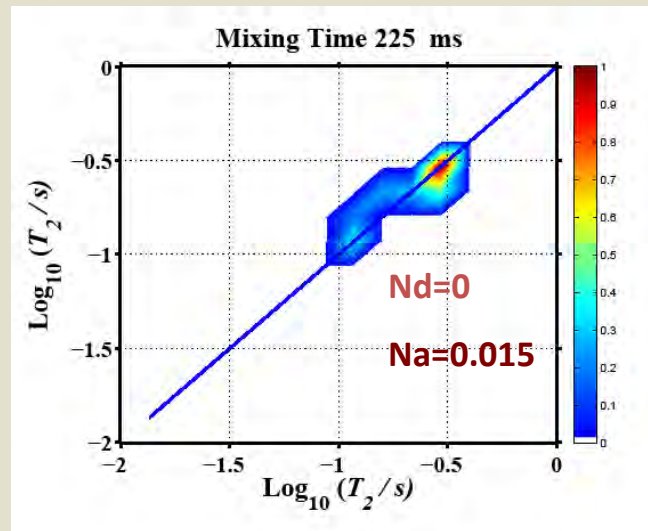
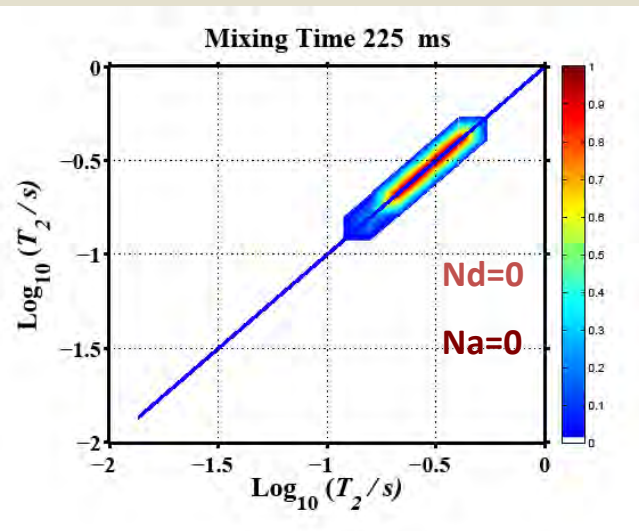
$$N_d = \mathbf{D} T_2^c / L^2 \quad N_a = \mathbf{v} T_2^c / L$$

$$N_d \approx 0.5 - 3 \quad N_a \approx 0 - 200$$

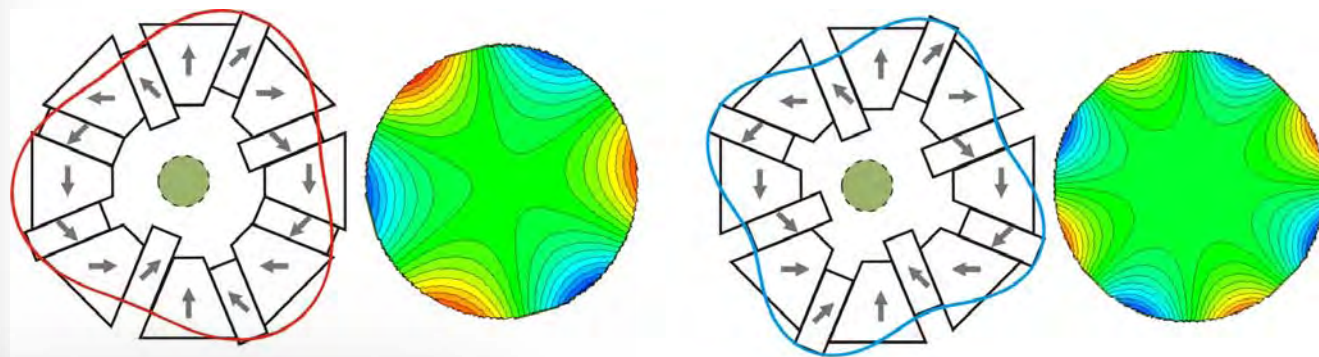
Peclet number: $Pe = N_a / N_d$

isotropic self-diffusion:	$2.2 \cdot 10^{-9} \text{ m}^2/\text{s}$
static field:	$\mathbf{B} = (0, 0, B_0)$
transverse relaxation rate:	100 – 700 ms
constant pump flow rate:	1-700 ml/h
void volume fraction:	35 %
average particle size:	0.2 mm

Modelling Diffusion and Flow Exchange

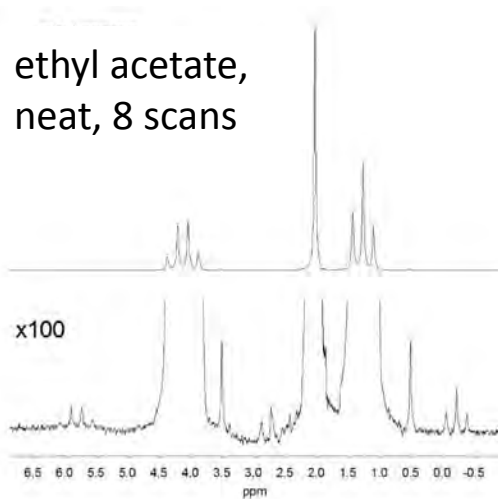


High Homogeneity, Large Volume, Small Magnet



SNR/scan > 32000

ethyl acetate,
neat, 8 scans



Commercial 40 MHz temperature controlled desktop ^1H NMR spectroscopy



Thank You

€€€: DFG
BMBF FCI
GIF Humboldt
DAAD